

# Measuring the charged pion polarizability in the $\gamma\gamma \rightarrow \pi^+\pi^-$ reaction

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# Motivation

- Electro ( $\alpha_\pi$ ) and Magnetic ( $\beta_\pi$ ) Polarizabilities represent fundamental properties of the charged pion in the low-energy sector of QCD
- $\alpha_\pi$  and  $\beta_\pi$  are related to the charged pion weak form factors  $F_V$  and  $F_A$ :

$$\alpha_\pi = -\beta_\pi = \frac{4\alpha_{EM}}{m_\pi F_\pi^2} (L_9^r + L_{10}^r) \propto \frac{F_A}{F_V}$$

where the low-energy constants  $L_{10}^r$  and  $L_9^r$  are part of the Gasser-Leutwyler effective Lagrangian

- Measuring the polarizabilities of the charged pion can be used to test the even-parity part of the Chiral Lagrangian  
(as opposed to the odd-parity sector which is tested via anomalous processes such as  $\pi^0 \rightarrow \gamma\gamma$ )
- Improved measurement of  $\alpha_\pi - \beta_\pi$  would reduce uncertainty contribution of hadronic light-by-light scattering to SM prediction of anomalous magnetic moment of the  $\mu$ :  $(g_\mu - 2)/2$   
(see K. Engel, H. Patel, M. Ramsey-Musolf, arXiv:1201.0809v2 [hep-ph])

- LO  $O(p^4)$  ChPT calculations give:

$$\alpha_\pi - \beta_\pi = 5.6 \pm 0.2 \times 10^{-4} \text{ fm}^3$$

with

$$\alpha_\pi + \beta_\pi = 0.0 \text{ fm}^3$$



*Donoghue and Holstein, 1989*

- NLO  $O(p^6)$  corrections are relatively small

$$\alpha_\pi - \beta_\pi = 5.7 \pm 1.0 \times 10^{-4} \text{ fm}^3$$

with

$$\alpha_\pi + \beta_\pi = 0.16 \pm 0.1 \times 10^{-4} \text{ fm}^3$$



*Bürgi 1996,  
Gasser et al. 2006*

- Dispersion Relations have been used to as well, but do not agree:

$$\alpha_\pi - \beta_\pi = 13.0^{+2.6}_{-1.9} \times 10^{-4} \text{ fm}^3$$

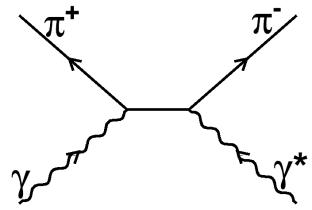
$$\alpha_\pi - \beta_\pi = 5.7 \times 10^{-4} \text{ fm}^3$$

*Fil'kov et al. 2006\**

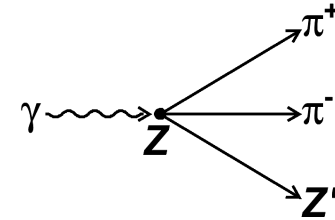
*Pasquini et al. 2008*

# Experimental Access

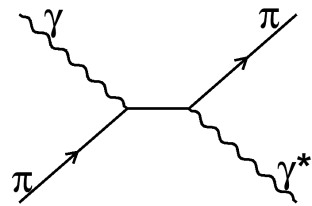
Primakoff effect



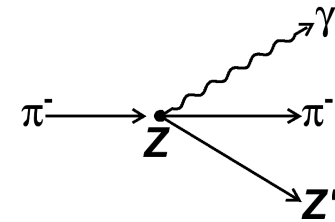
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*This experiment*

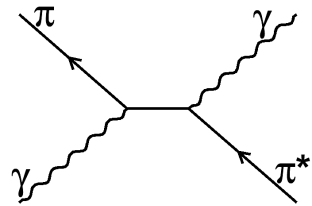


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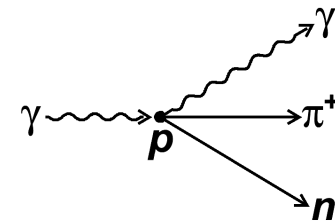


*SIGMA*

Radiative pion photo-production

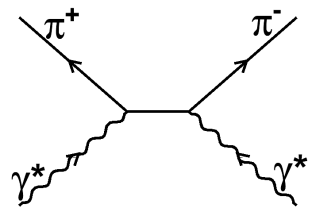


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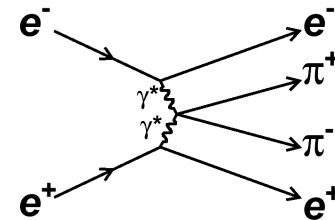


*MAMI  
PACHRA*

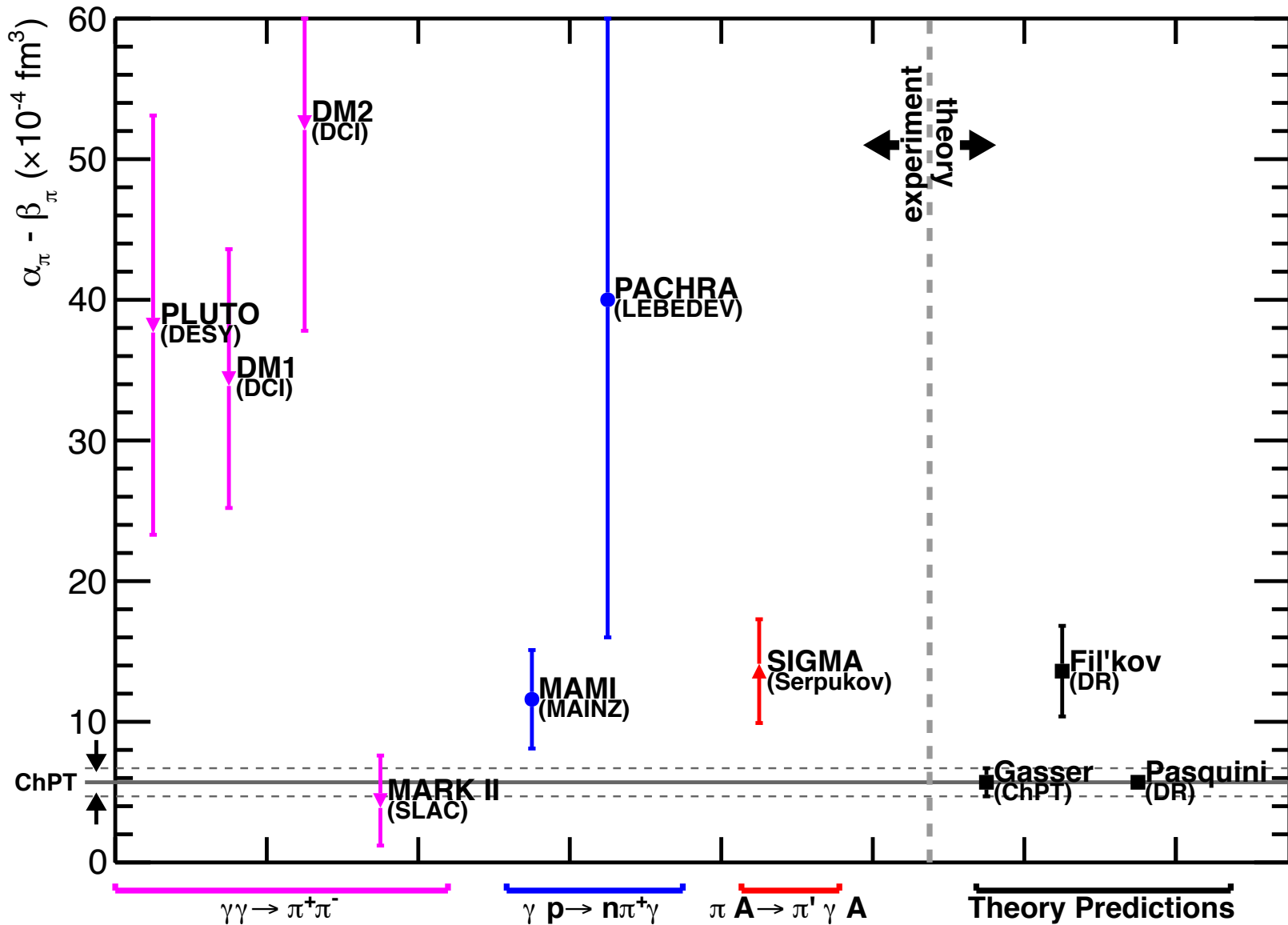
Light by light scattering  
(by crossing symmetry)



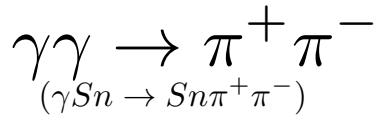
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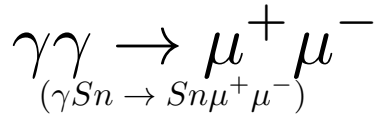
*PLUTO  
DM1  
DM2  
MARK-II*



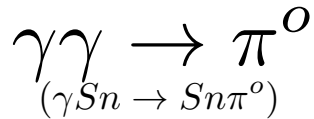
# Experimental Setup



Signal reaction

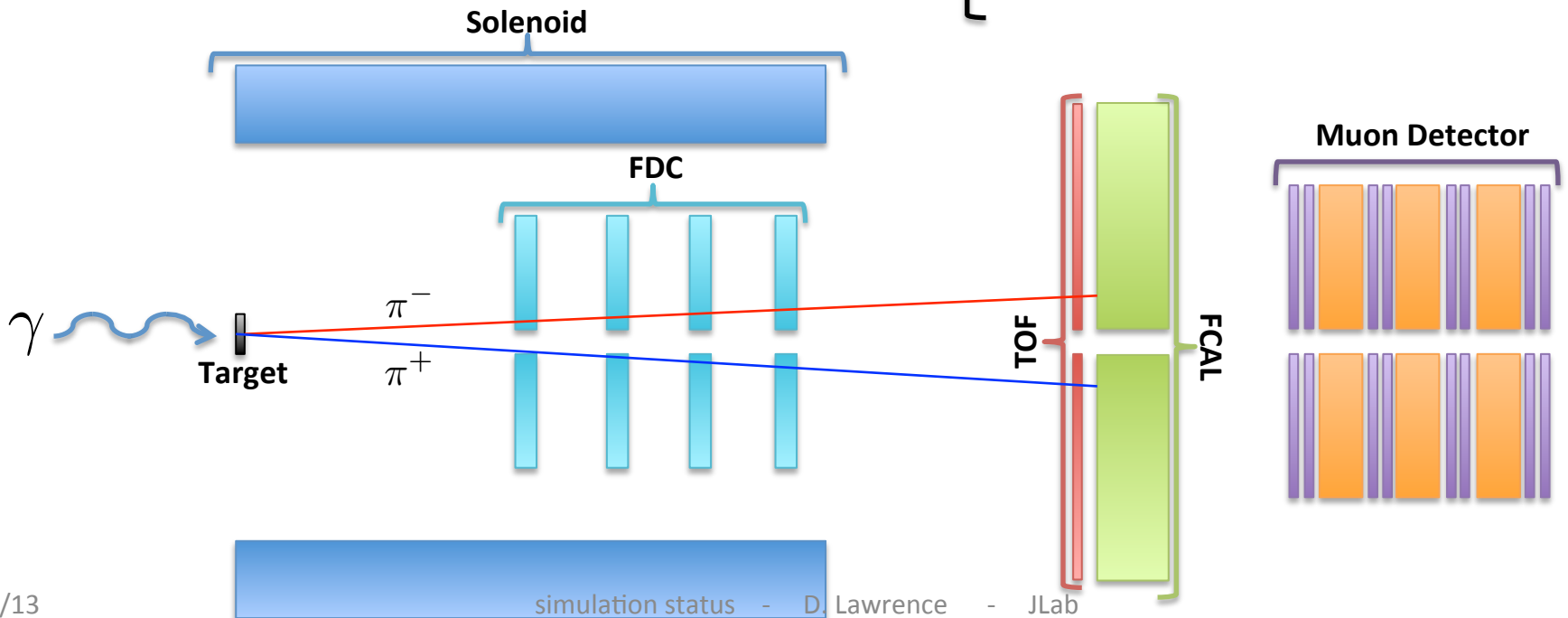


Normalization



Beam polarization

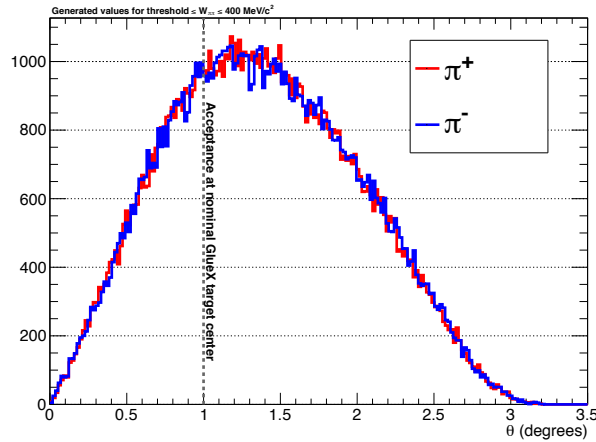
- All occur via the Primakoff effect (interaction with the Coulomb field of nucleus)
- All result in very forward going particles
- Low  $t$  ( $-t < 0.005 \text{ GeV}^2$ )



# Kinematics of Experiment

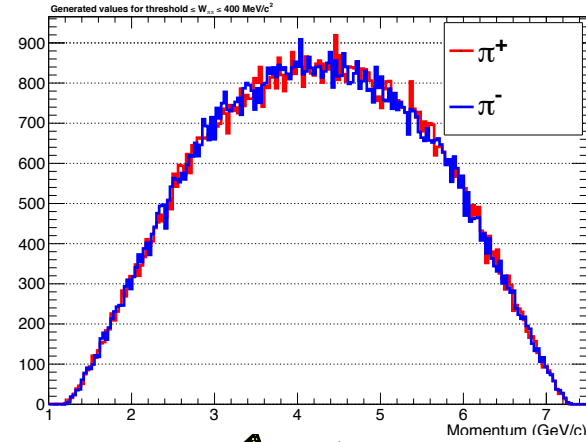
$\pi^\pm$  polar angle distribution in lab frame

August 3, 2012 DL



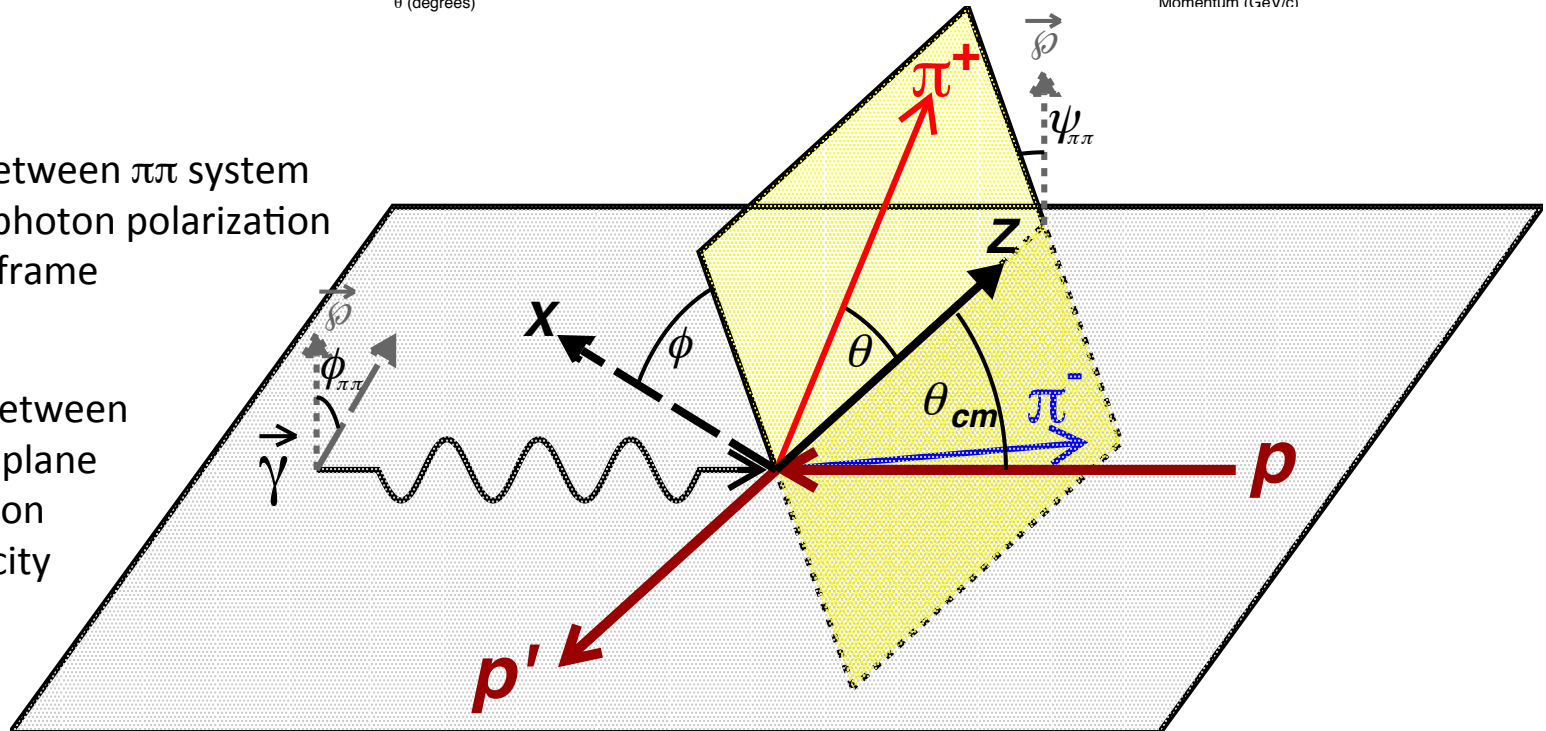
$\pi^\pm$  momentum distribution in lab frame

August 3, 2012 DL



$\phi_{\pi\pi}$  is angle between  $\pi\pi$  system and incident photon polarization vector in CM frame

$\psi_{\pi\pi}$  is angle between  $\pi\pi$  scattering plane and polarization vector in helicity frame



# Backgrounds

- Experiment will measure reaction:



- Primary backgrounds will be:

- coherent  $\rho^0$  production followed by  $\rho \rightarrow \pi\pi$  decay

- Will use angular distributions to separate Primakoff from coherent  $\rho^0$  production (*see later slides*)

- Electromagnetic  $\mu^+\mu^-$  production

- Will use dedicated detector to identify hadron showers

- Currently gathering list of other potentially relevant backgrounds including:

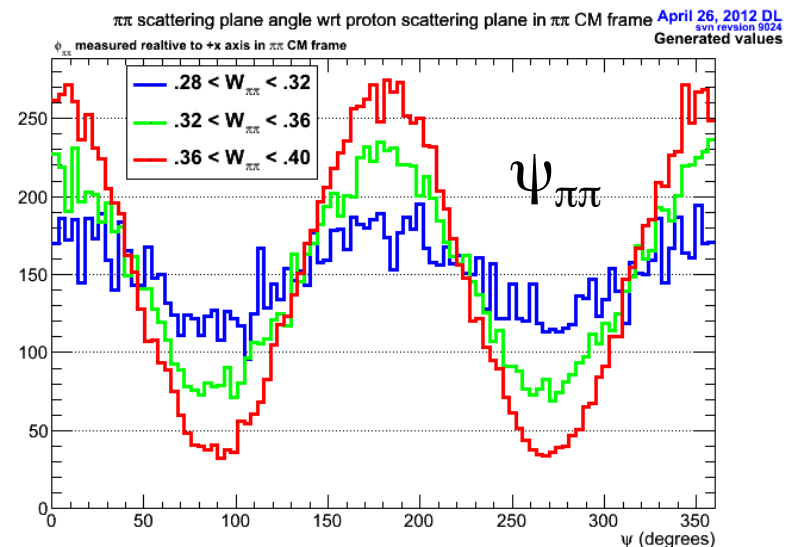
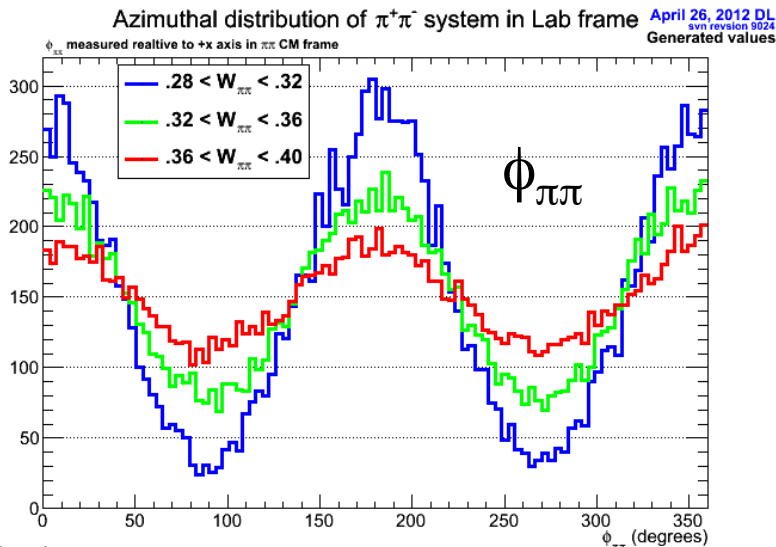
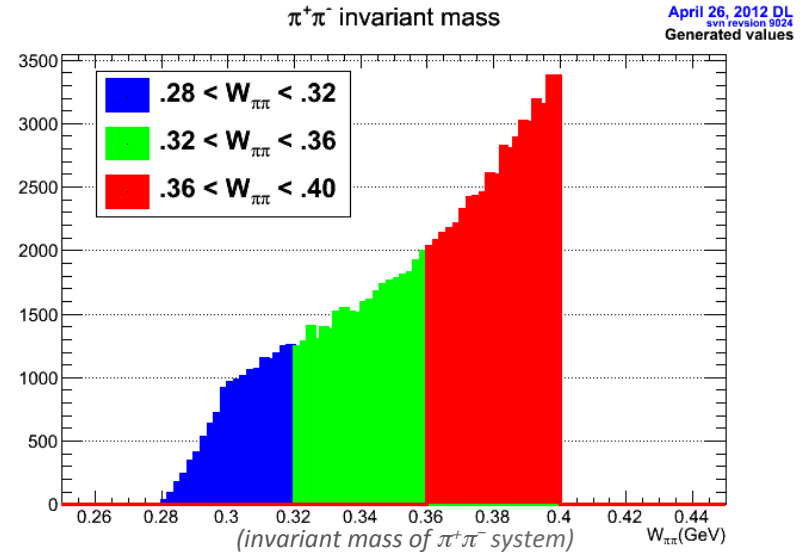
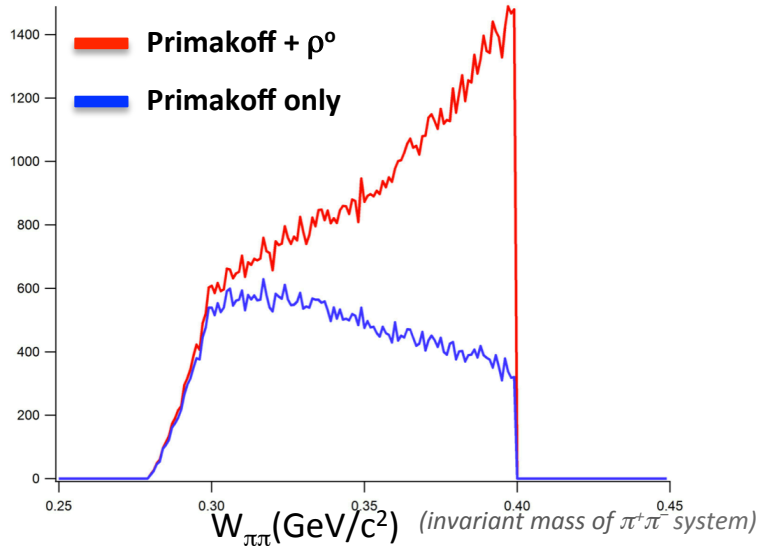
- $\sigma$  meson production (*angular distributions same as Primakoff*)

- incoherent  $\pi^+\pi^-$  production

- ...

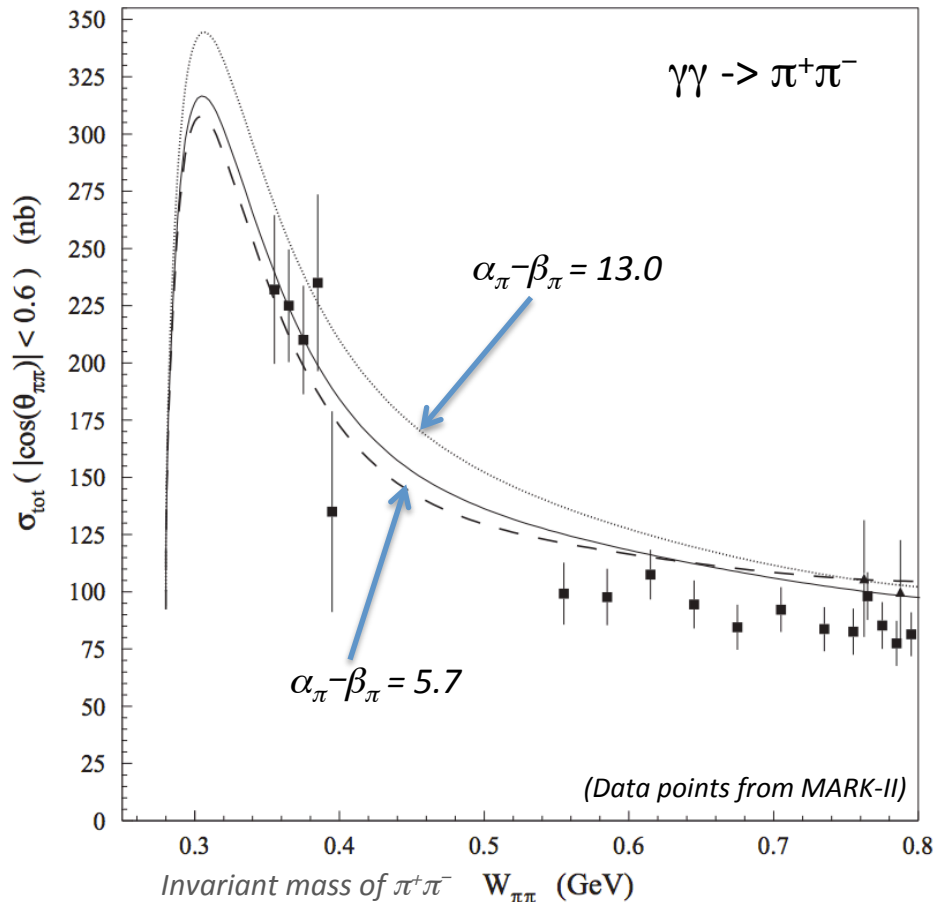


# Linear Polarization of incident photon beam helps distinguish Primakoff from coherent $\rho^0$ production



# Relating cross-section to $\alpha_\pi - \beta_\pi$

Figure 5. from Pasquini et al. Phys. Rev. C 77, 065211 (2008)



- dotted:** subtracted DR calculation with  $\alpha_\pi - \beta_\pi = 13.0$
- dashed:** subtracted DR calculation with  $\alpha_\pi - \beta_\pi = 5.7$
- solid:** unsubtracted DR calculation with  $\alpha_\pi - \beta_\pi = 5.7$

Cross-section for  $\gamma\gamma \rightarrow \pi^+\pi^-$  calculated based on two values of  $\alpha_\pi - \beta_\pi$ :

$$\alpha_\pi - \beta_\pi = 13.0 \times 10^{-4} \text{ fm}^3 \text{ (top, dotted line)}$$

$$\alpha_\pi - \beta_\pi = 5.7 \times 10^{-4} \text{ fm}^3 \text{ (solid and dashed lines)}$$

Cross-section varies by  $\sim 10\%$  for factor of 2 variation in  $\alpha_\pi - \beta_\pi$

Need measurement of  $\sigma(\gamma\gamma \rightarrow \pi^+\pi^-)$  at few percent level

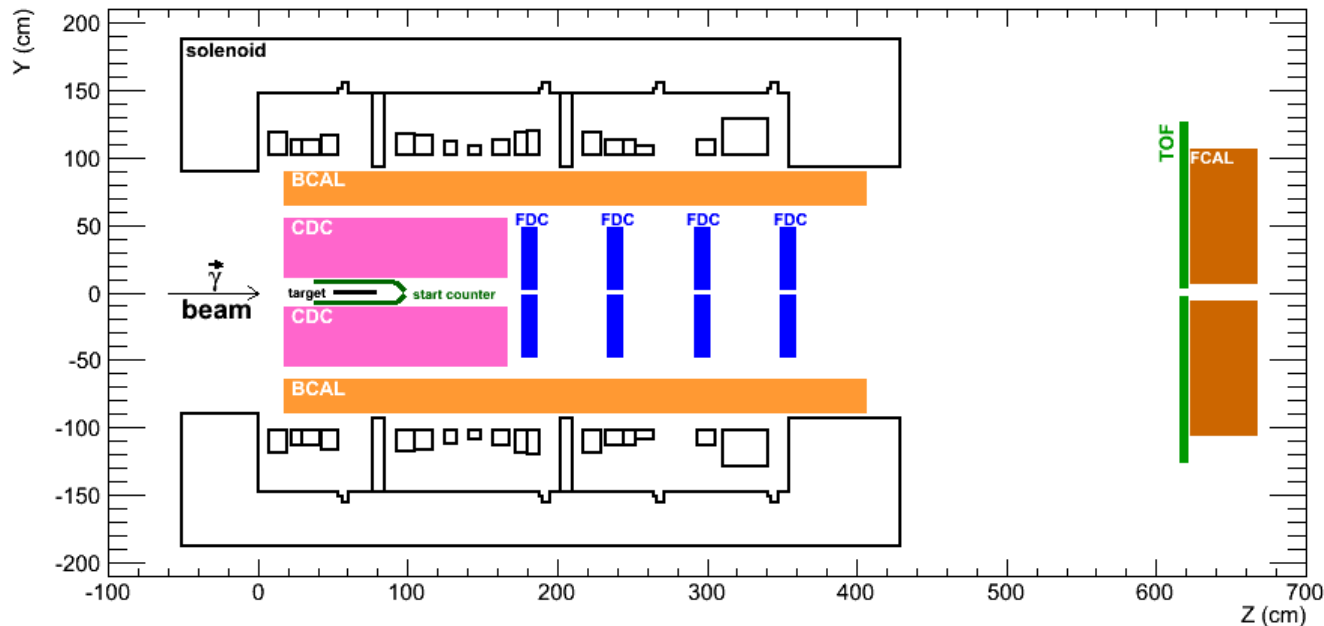
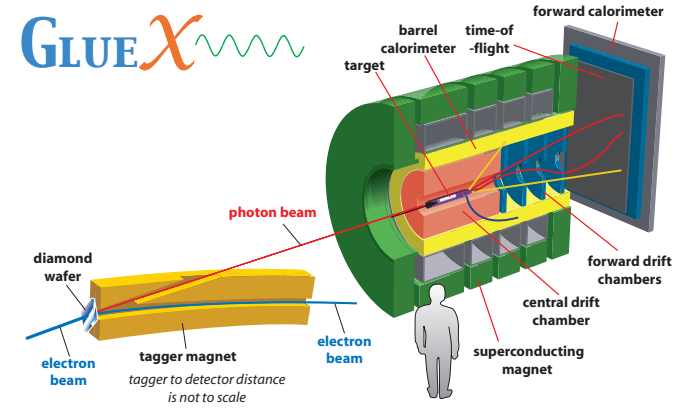
# The GlueX Detector in Hall-D

## New Proposal will use GlueX detector in Hall-D:

- Linearly polarized photon source ( $\sim 9\text{GeV}$ )
- 2T solenoidal magnetic field ( $\delta p/p = \text{few } \%$ )
- Drift chambers
- High resolution Time-of-flight detector

## Modifications to standard GlueX setup:

- Replace LH2 target with thin Pb target
- Move target upstream to improve low-angle acceptance
- Alternate start-counter?



# Detector Rates/Acceptance

- $10^7$  tagged photons/second on 5% radiation length Pb target
- 500 hours of running
- $W_{\pi\pi}$  acceptance down to  $\sim 320 \text{ MeV}/c^2$   
(*working to improve acceptance to even lower  $W_{\pi\pi}$* )
- Estimated  $\sim 36\text{k}^*$  Primakoff events  
(*contrast this with the  $\sim 400$  events in the acceptance of the MARK-II measurement*)

\* before detector acceptance

# Summary

- Next to leading order ChPT prediction of  $\alpha_\pi - \beta_\pi$  is  $5.7 \pm 1.0 \times 10^{-4} \text{ fm}^3$
- Previous measurements of  $\alpha_\pi - \beta_\pi$  range from  $4.4 - 52.6 \times 10^{-4} \text{ fm}^3$
- A new proposal to measure the charge pion polarizability  $\alpha_\pi - \beta_\pi$  via the  $\gamma\gamma^* \rightarrow \pi^+\pi^-$  reaction is being developed that will use the GlueX detector at Jefferson Lab
- Letter of Intent submitted to PAC in June 2012. PAC has encouraged development of full proposal
  - will be submitted in next PAC, spring/summer 2013
- Work is ongoing to identify relevant backgrounds and determine detector acceptance
- An improved measurement of  $\alpha_\pi - \beta_\pi$  would improve the SM prediction of the anomalous magnetic moment of the  $\mu$ :  $(g_\mu - 2)/2$



# Anomalous magnet moment of the $\mu$ : $(g_\mu - 2)/2$

- Experimental uncertainty of  $\sim 63 \times 10^{-11}$
- SM calculation has uncertainty of  $\sim 49 \times 10^{-11}$ 
  - Hadronic light-by-light (HLBL) scattering is one of two major contributors to SM uncertainty  
(other is hadronic vacuum polarization)
  - $\pi$  polarizability is potentially significant contribution to HLBL that is currently omitted from current SM calculation
- g-2 collaboration at Fermilab is preparing a measurement that will reduce experimental uncertainty by a factor of 4
- A measurement of the  $\pi$  polarizability could help reduce the SM uncertainty significantly

*For detailed info on planned Fermi-lab experiment, see [http://gm2.fnal.gov/public\\_docs/proposals/Proposal-APR5-Final.pdf](http://gm2.fnal.gov/public_docs/proposals/Proposal-APR5-Final.pdf)*