

PR12-20-011: Measurement of the high-energy contribution to the Gerasimov-Drell-Hearn sum

A. Deur, for the GlueX collaboration
08/11/2020

Spokespersons: M-M. Dalton (JLab), A.D. (JLab), J. Stevens (W&M) and S. Širca (U Ljubljana)

Proposal endorsed by the GlueX collaboration.

PAC 47 encouraged LOI to be developed into a full proposal.¹

Theory Report for PAC 48 concludes that “This an important measurement with impact on nuclear and particle physics”

TAC for PAC 48 reports that while the experiment requires new equipment “no real showstopper has been identified”

¹ The PAC recognizes the science case for this LOI and recommends preparation of a full proposal with focus on the extraction of the actual value of the GDH integral at high energies.

The Gerasimov-Drell-Hearn sum rule

Fundamental prediction linking **spin-dependent photoproduction cross-sections** to target **anomalous magnetic moment**:

$$\int_{v_{\text{thr}}}^{\infty} (\sigma^{3/2} - \sigma^{1/2}) \frac{dv}{v} = \frac{4\alpha S \pi^2 \kappa^2}{M^2}$$

Spin-dependent total photoproduction cross-sections

anomalous magnetic moment

spin

Photon energy

Mass

Validity of sum rule mainly **determined by large v behavior of $\sigma^{3/2} - \sigma^{1/2}$**
 \Rightarrow for nucleon target, **tests QCD/nucleon properties**.

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$$\int_{\nu_{\text{thr}}}^{\infty} (\sigma^{3/2} - \sigma^{1/2}) \frac{d\nu}{\nu} = \frac{4\alpha S \pi^2 \kappa^2}{M^2}$$

Diagram annotations:

- Spin-dependent total photoproduction cross-sections**: Points to $\sigma^{3/2} - \sigma^{1/2}$
- Photon energy**: Points to ν in the denominator
- anomalous magnetic moment**: Points to κ^2
- spin**: Points to S
- Mass**: Points to M^2

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Knowledge of large ν behavior is critical, yet existing data restricted to low energies:

- Proton: $\nu > 3$ GeV not measured yet.
- Neutron: $\nu > 1.8$ GeV not measured yet.

Polarized nucleon's behavior unknown at large ν . Expected to be described by Regge theory, but unverified, and photo- and electro-production **data in conflict with Regge expectation**.

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Diagram annotations:

- Spin-dependent total photoproduction cross-sections** (red text) points to $\sigma^{3/2} - \sigma^{1/2}$.
- Photon energy** (green text) points to v in the denominator.
- anomalous magnetic moment** (blue text) points to κ^2 .
- spin** (purple text) points to S .
- Mass** (black text) points to M^2 in the denominator.

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Hall D: tagger+large solid angle detector+high flux \Rightarrow **uniquely suited** to perform a large- v GDH measurement.

Motivations

Knowledge of large ν behavior is critical, yet existing data restricted to low energies:

- Proton: $\nu > 3$ GeV not measured yet.
- Neutron: $\nu > 1.8$ GeV not measured yet.
- Unpolarized version of GDH integral $\int (\sigma^{3/2} + \sigma^{1/2}) d\nu$ does not converge.
- Large- ν uncertainty dominates proton GDH test. No test possible on neutron yet: ν too low.
- Need to go beyond the resonance bumps to perform reliable Regge-based fit to:
 - Check Regge theory for the first time in the polarized case,
 - Provide a reliable basis for extrapolation to $\nu \rightarrow \infty$.
- Hall D's 3-12 GeV range: extend coverage by factor 4 for proton and 6 for neutron/deuteron.
 - Sensitive domain for sum rule violation; smooth cross-section allows Regge-based fit.
 - Regardless of the sum rule validity, it is an important domain to explore:
 - Constrains spin-dependent Compton *amplitude* f_2 . Test of Chiral Perturbation Theory.
 - No non-zero deuteron signal seen yet at large ν or in the diffractive domain.
 - Discrepancy between Regge expectation and DIS data.
 - $Q^2=0$ baseline for EIC diffractive measurements. Study transition between DIS and diffractive regimes.
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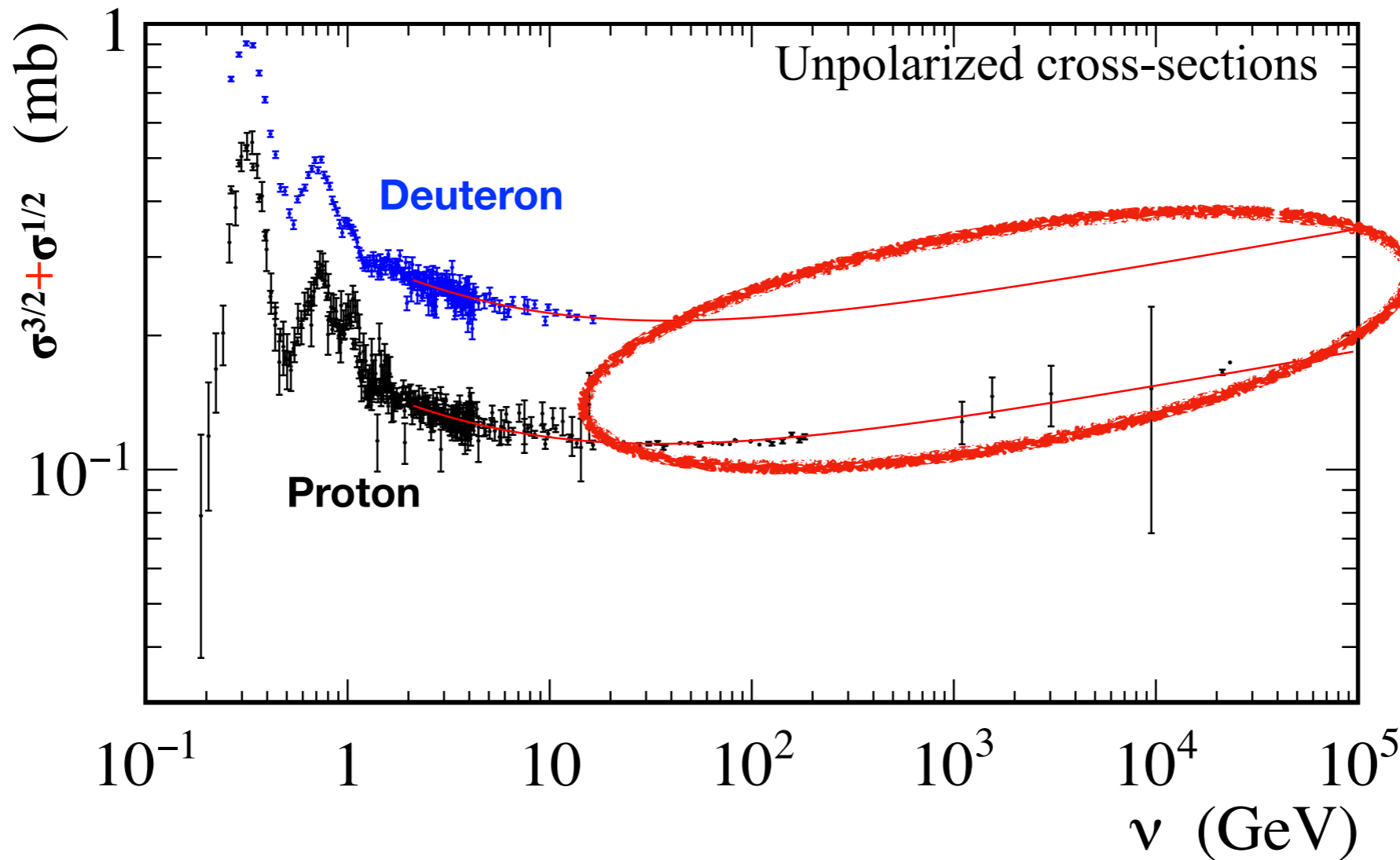
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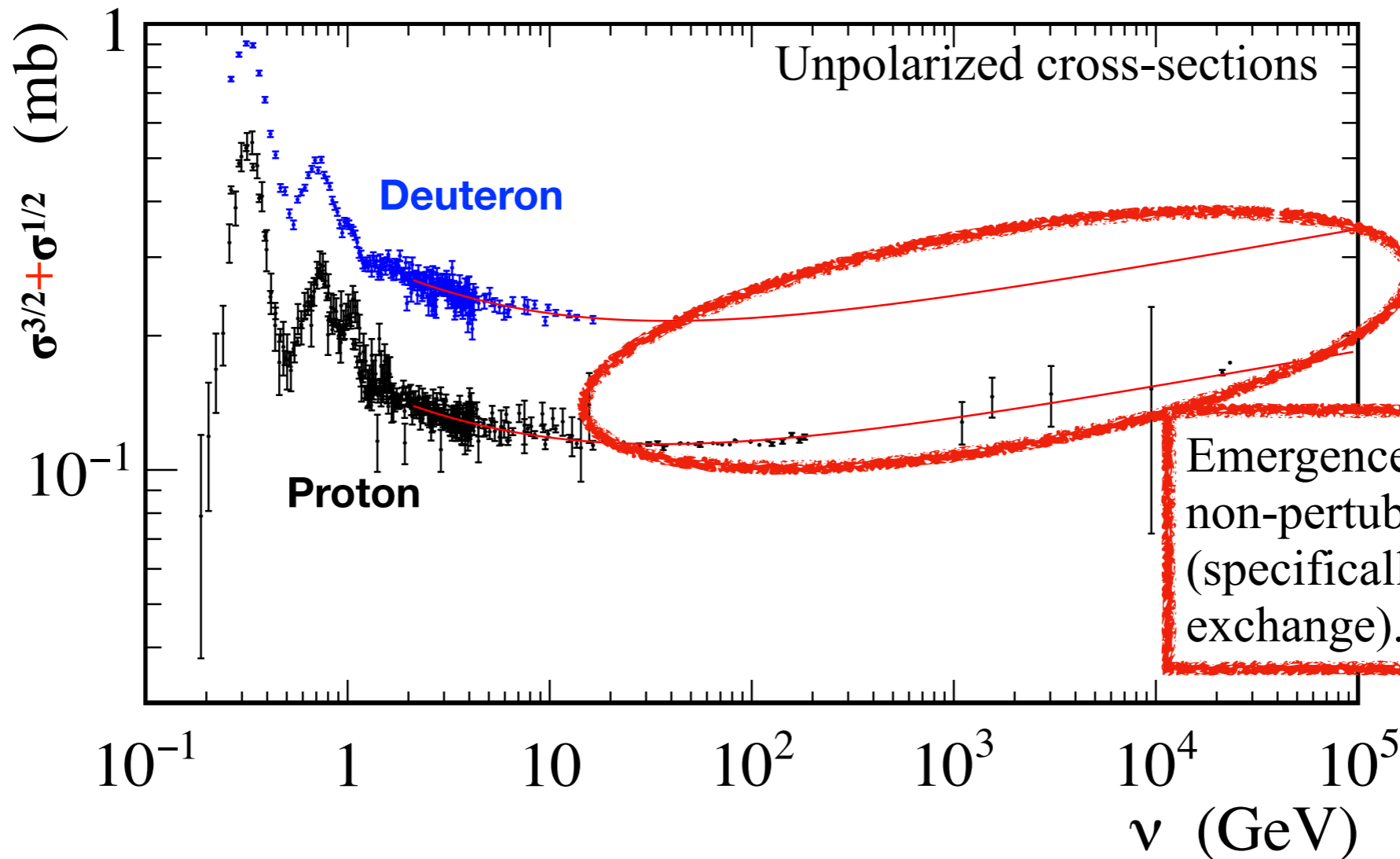
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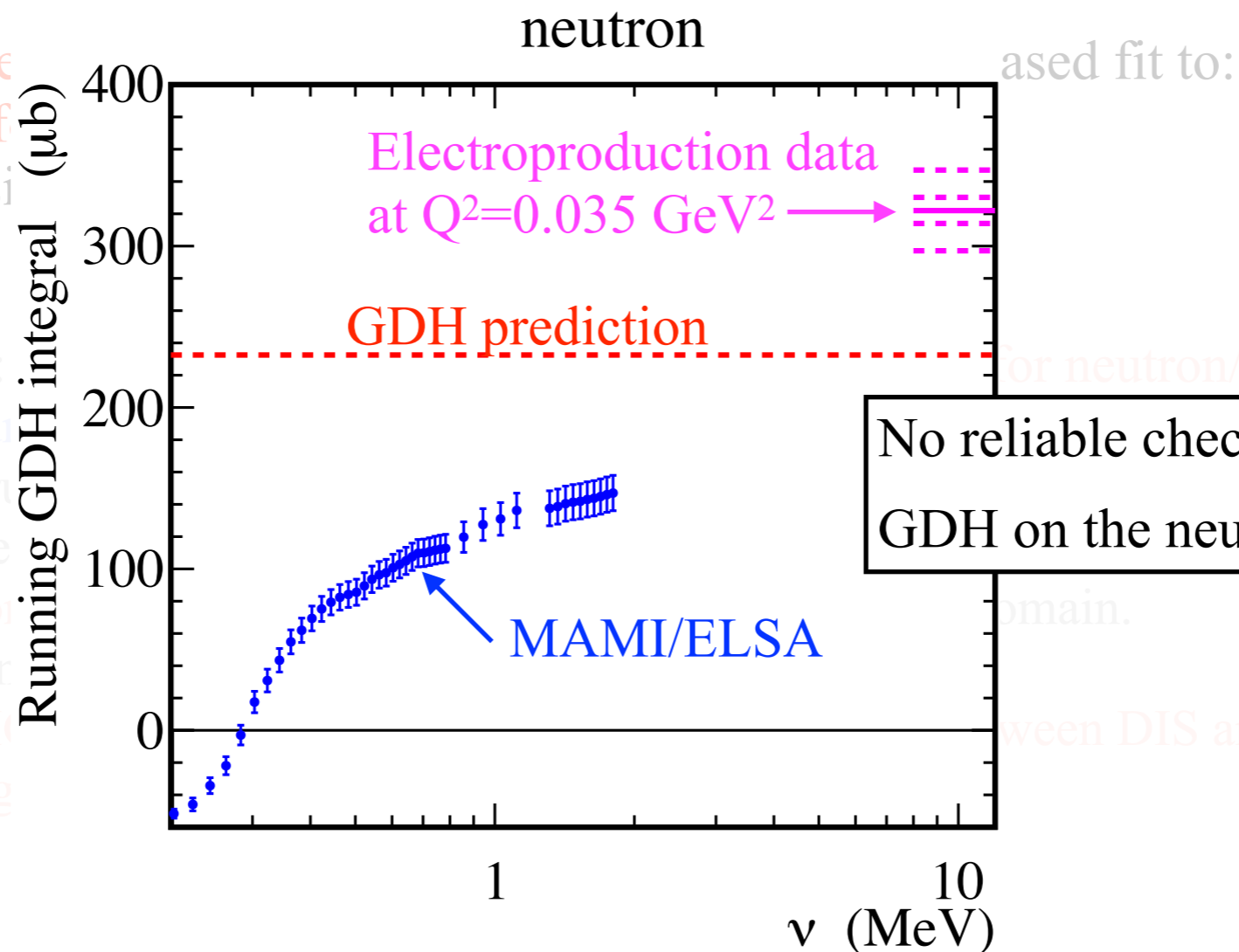
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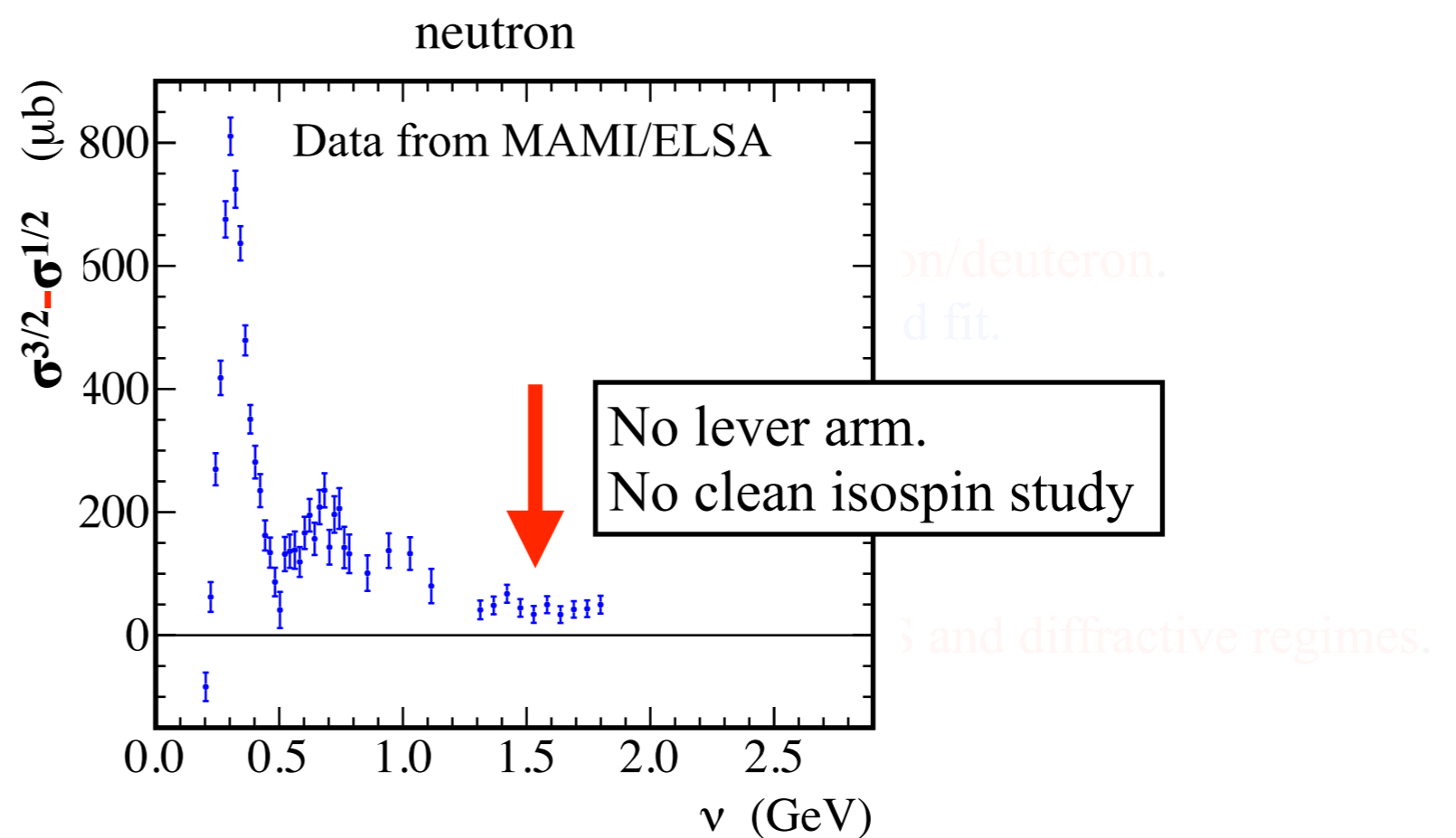
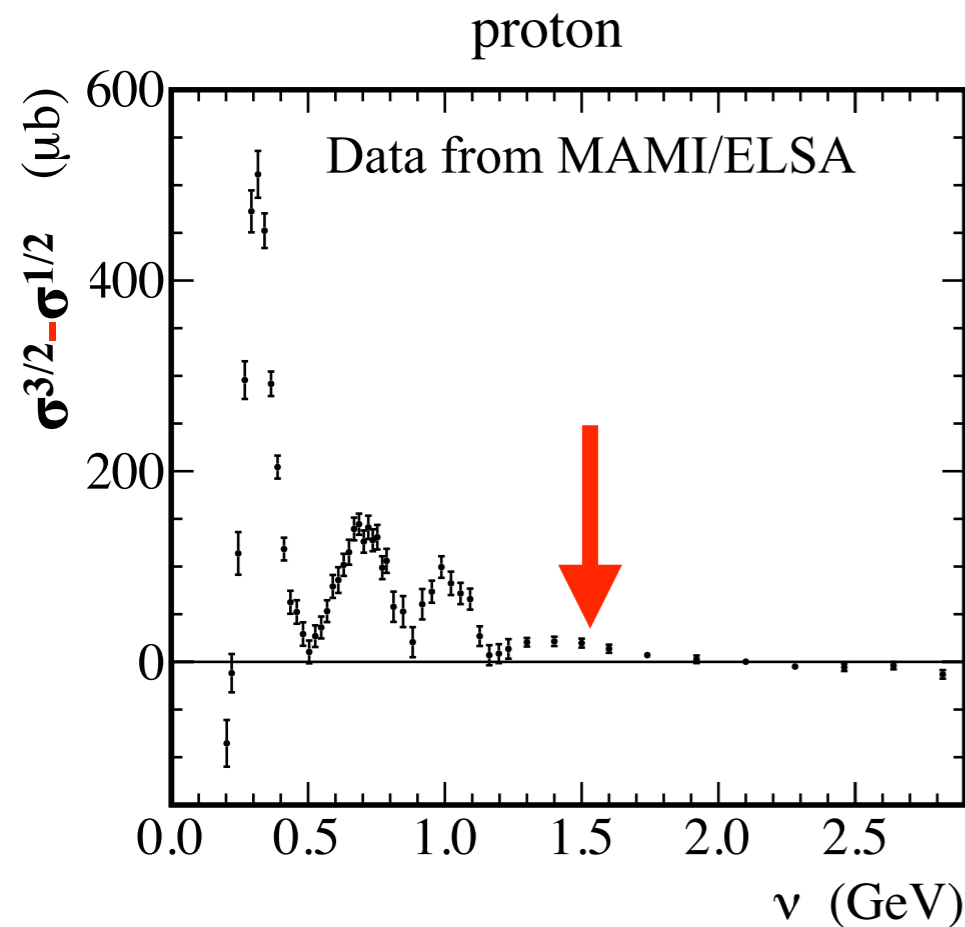


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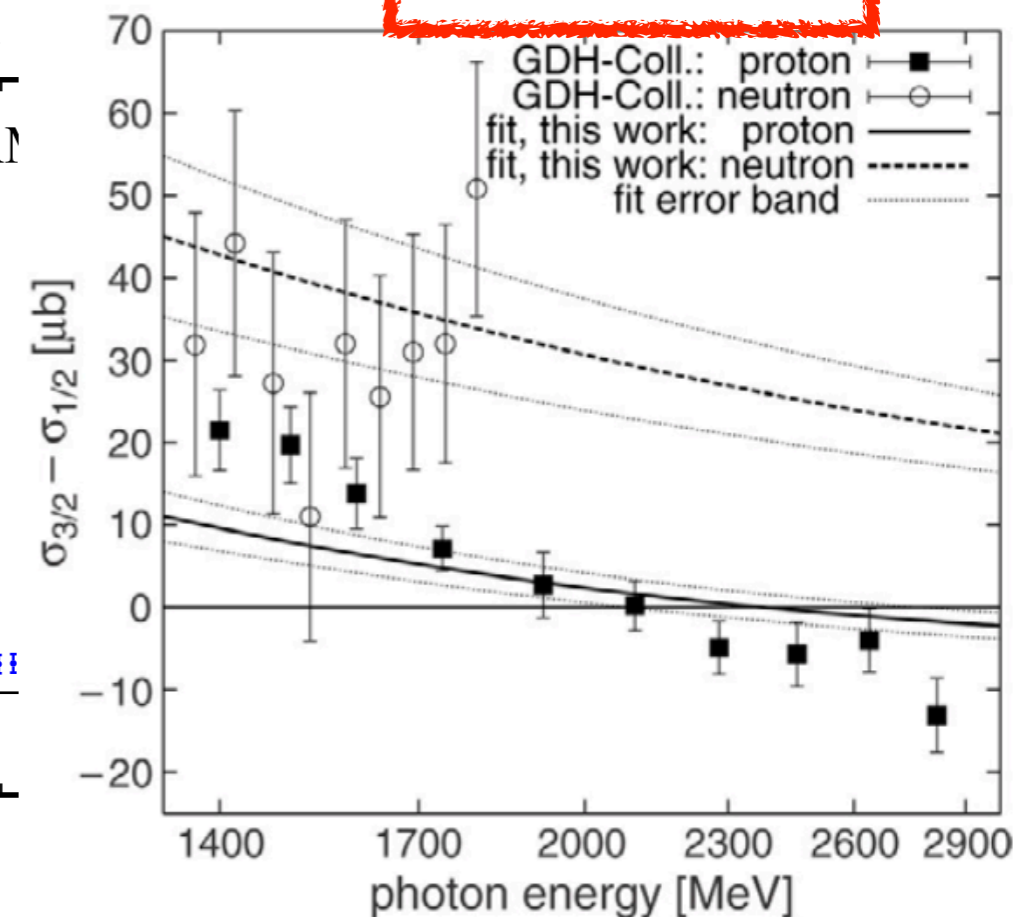
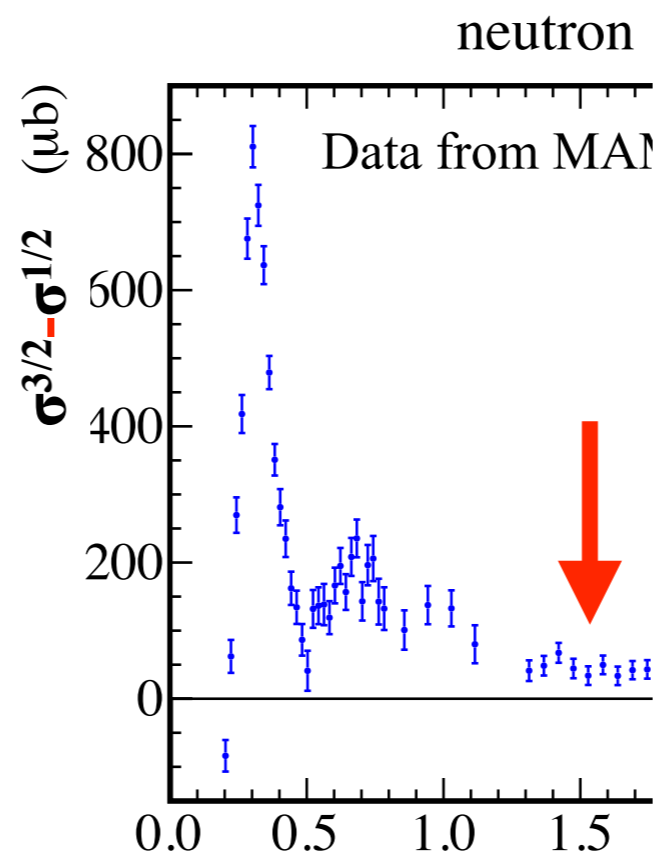
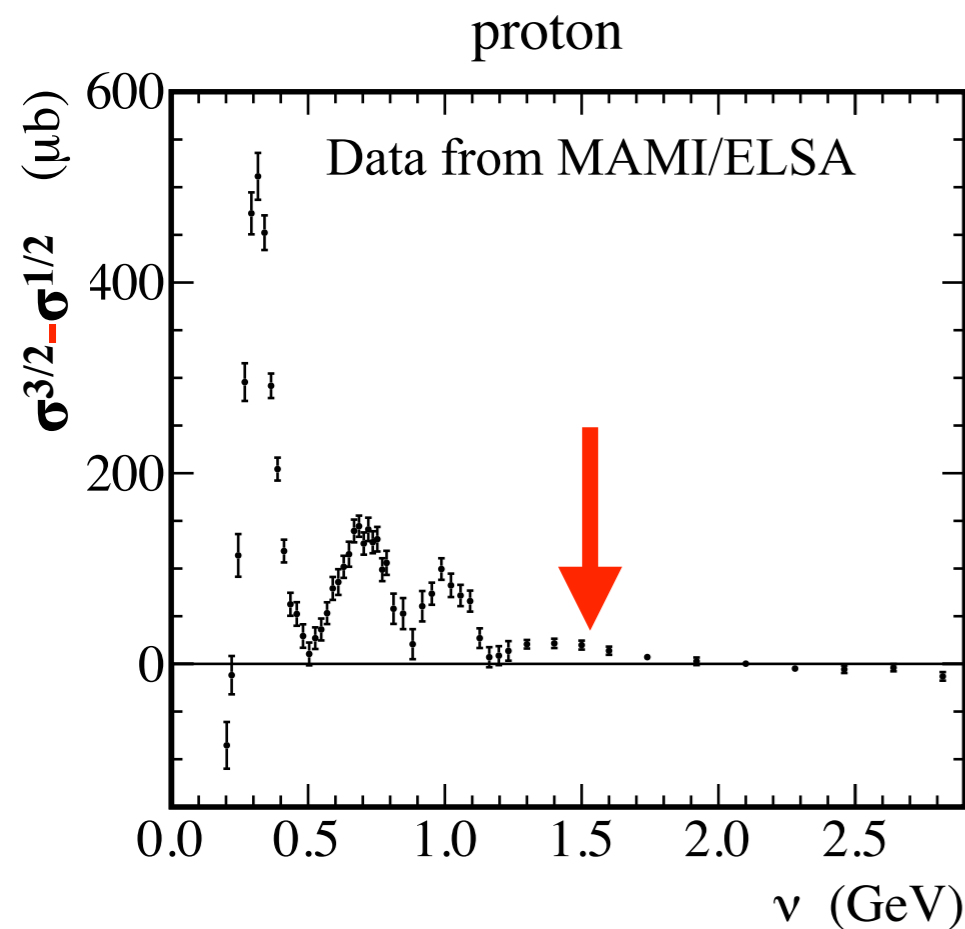
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Poor Regge fits for current world data.



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Experimental Setup

- Need both **proton** and **neutron** (deuteron) targets:
 - **Isospin separation**. Regge theory: **isoscalar** and **isovector** contributions to $(\sigma^{3/2}-\sigma^{1/2})$ come from different meson families (**f₁** and **a₁**, respectively).
 - **Deuteron**:
 - no non-zero $(\sigma^{3/2}-\sigma^{1/2})$ seen yet for D at large ν (both photo- and electro-production).
 - No neutron data above 1.8 GeV.
- Energy coverage:
 - **3 < ν < 12 GeV** Standard CEBAF at 12 GeV.
 - **1 < ν < 4 GeV** Requires CEBAF to run at 4 GeV, e.g. during low energy summer run.
- 3 main ingredients needed:
 - **Circularly polarized** tagged **photon** beam; • Polarized electron beam;
 - **Longitudinally polarized target**; FROST target. • Amorphous radiator.
 - **Large solid-angle detector**. Hall D
- Experimental configuration and trigger: same as GlueX.
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Analysis Strategy

- **First:**

Form **yield difference** $\Delta y(v) = N^{3/2} - N^{1/2}$. Sufficient to study **GDH convergence**.

⇒ **Normalization factors not important**

For example, if $\sigma^{3/2} - \sigma^{1/2} = av^b$, we obtain ***b*** without need to extract an accurate ***a***.

- **Suppress normalization factor uncertainties.**
- **Unpolarized backgrounds** (e.g. target dilution) **cancel.**

- **Later on:**

Extract **absolute cross-section** $\sigma^{3/2} - \sigma^{1/2}$: Study GDH SR **validity** for both nucleons + **other goals**

Time request

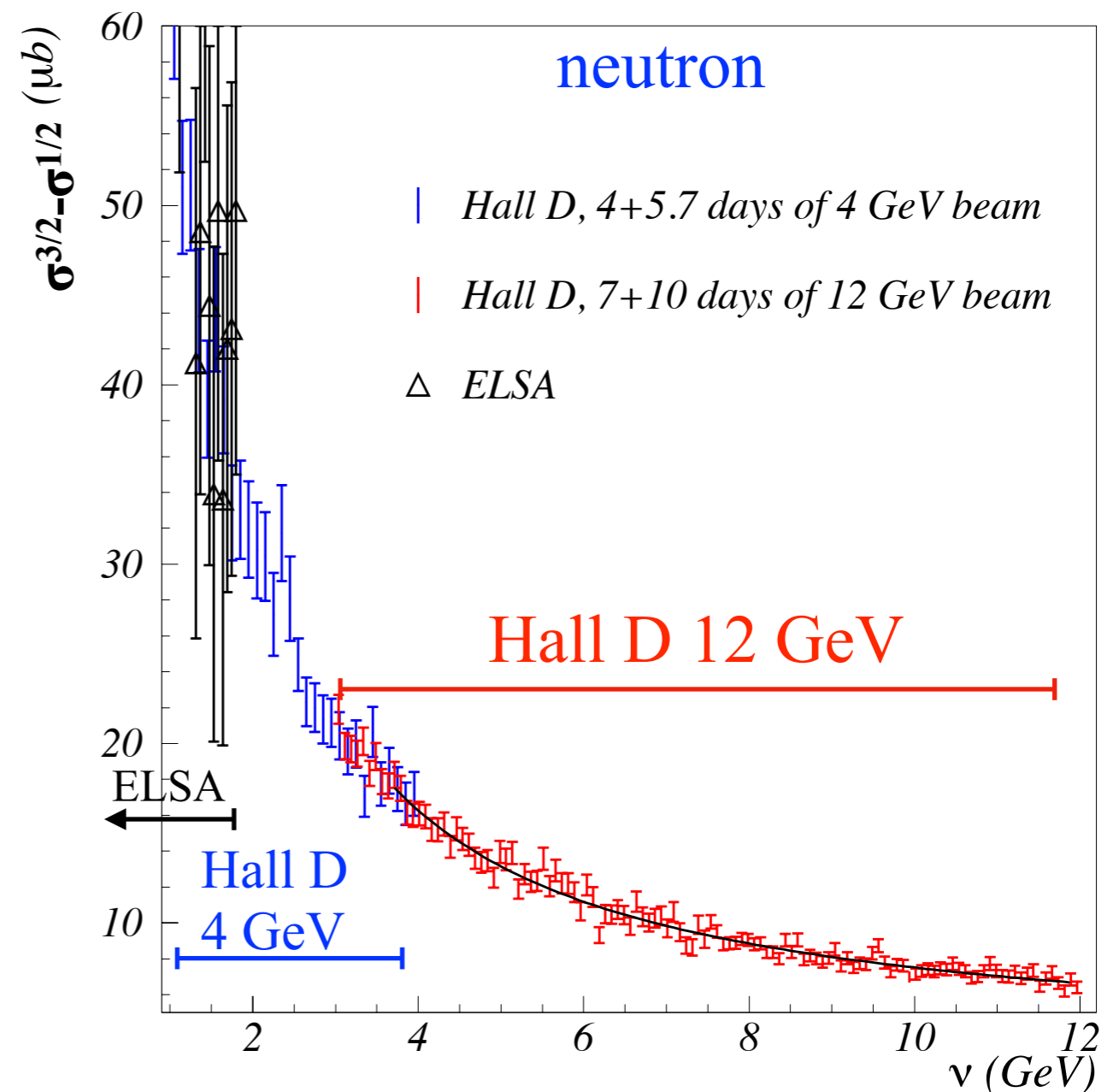
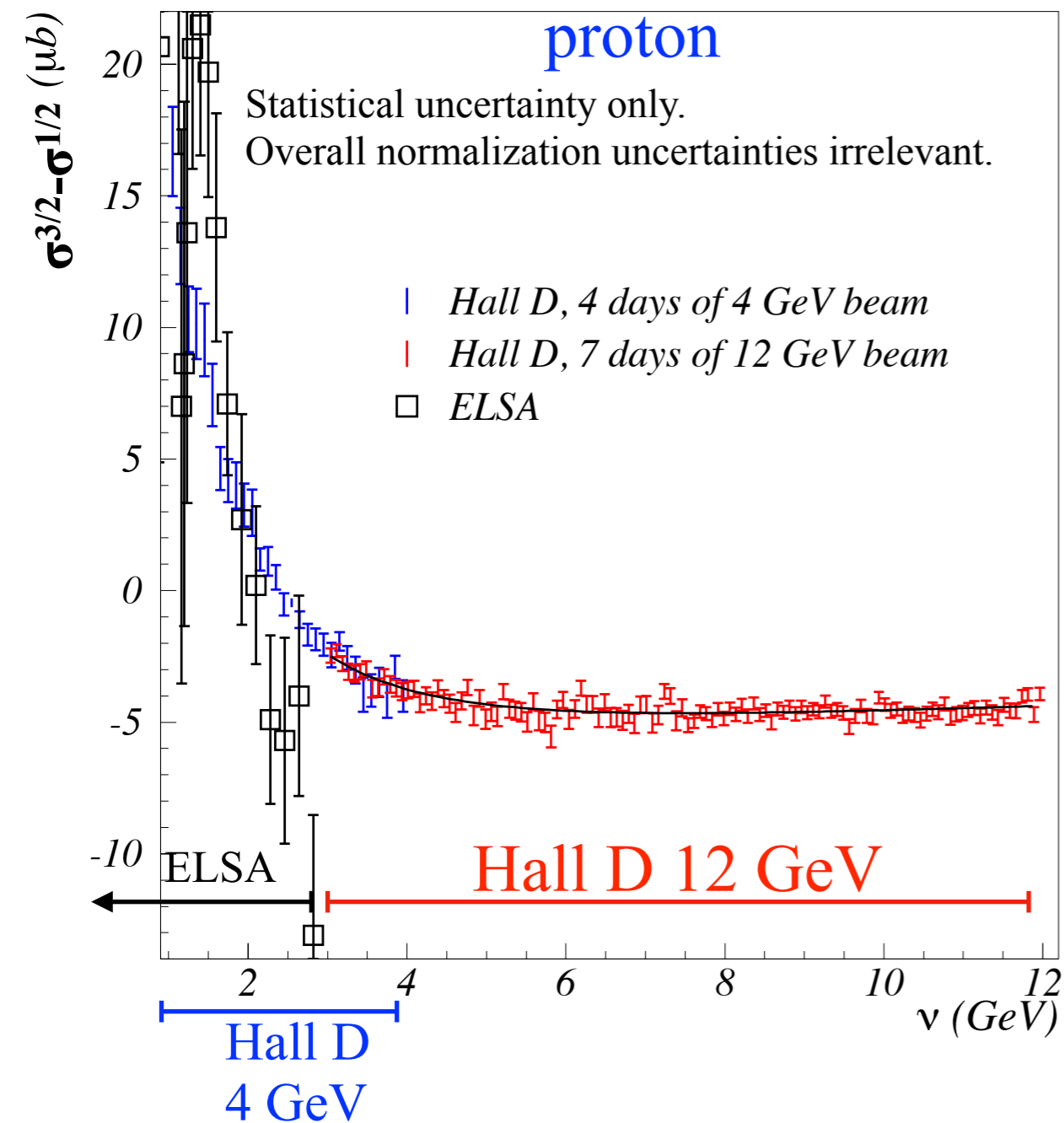
Time (day)	Target	Goal/Remarks
10	Deuteron	Main production at 12 GeV
0.3	Deuteron	Spin dance done during above task
1	Deuteron	Target spin-flip/repol./NMR calib. No beam, done at middle of production
0.5	^4He	For background subtraction. Includes target change overhead
1	Deuteron \rightarrow proton switch	No beam. NMR calib.
7	Proton	Main production at 12 GeV
1	Proton	Target spin-flip/repol./NMR calib. No beam, done at middle of production
0.5	Pair. Spec. converter	Absolute flux calib.
12 GeV: 21.3		total time at 12 GeV
5.7	Deuteron	Production 4 GeV
0.3	Deuteron	Spin dance done during above task
0.3	^4He	For background subtraction. Includes target change overhead
1	Deuteron \rightarrow proton switch.	No beam. NMR calib.
4	Proton	Production at 4 GeV
0.5	Pair. Spec. converter	Absolute flux calib.
4 GeV: 11.8		total time at 4 GeV
Total: 33.1		total experiment time

12 GeV

4 or 5 GeV

Expectations

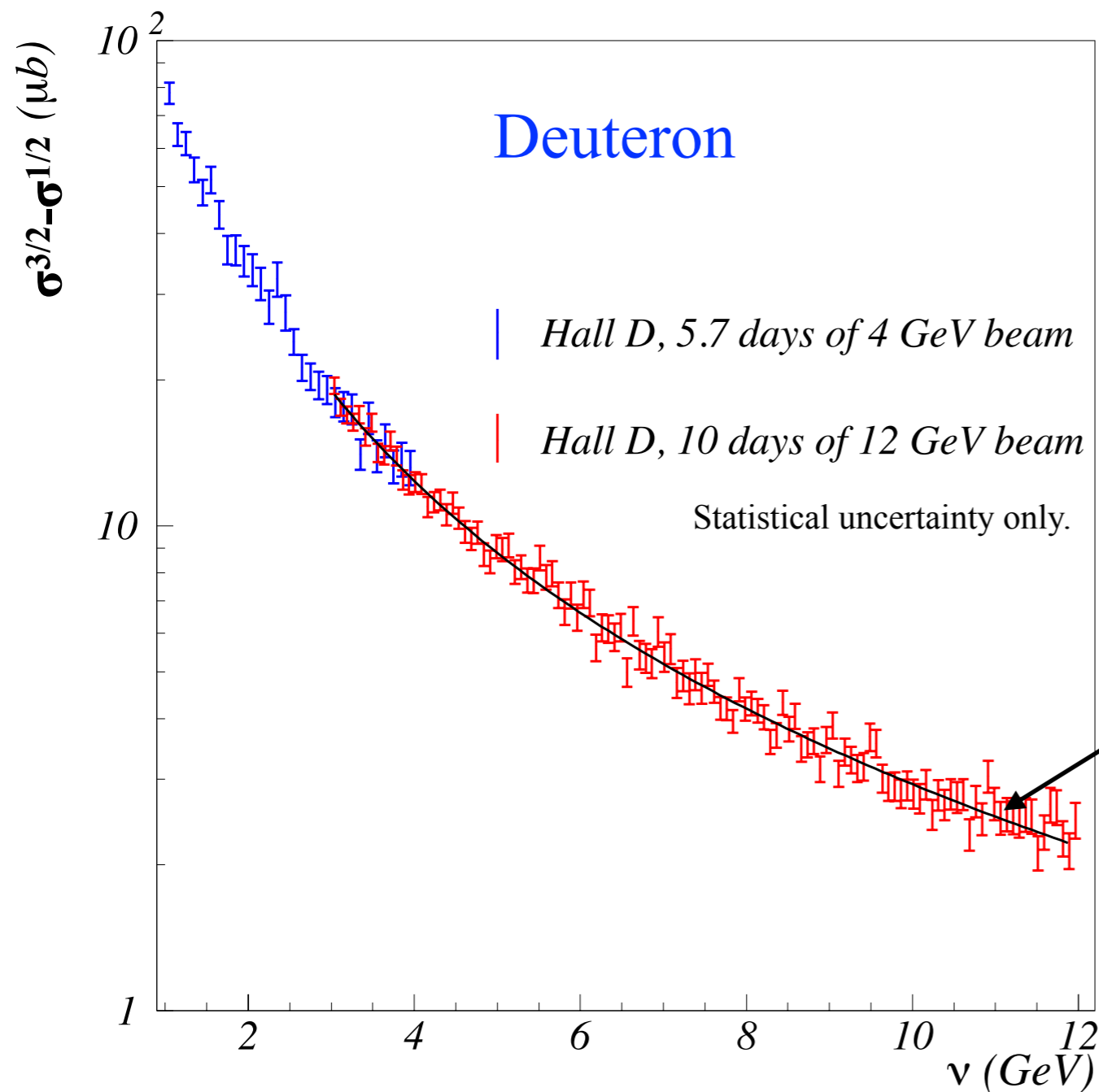
Simulated data:



- Statistical accuracy greatly improve compared to previous experiments.
- Much extended energy reach.
- low energy data: overlap with word data. Bridge gap for neutron data.

Expectations

Simulated data:



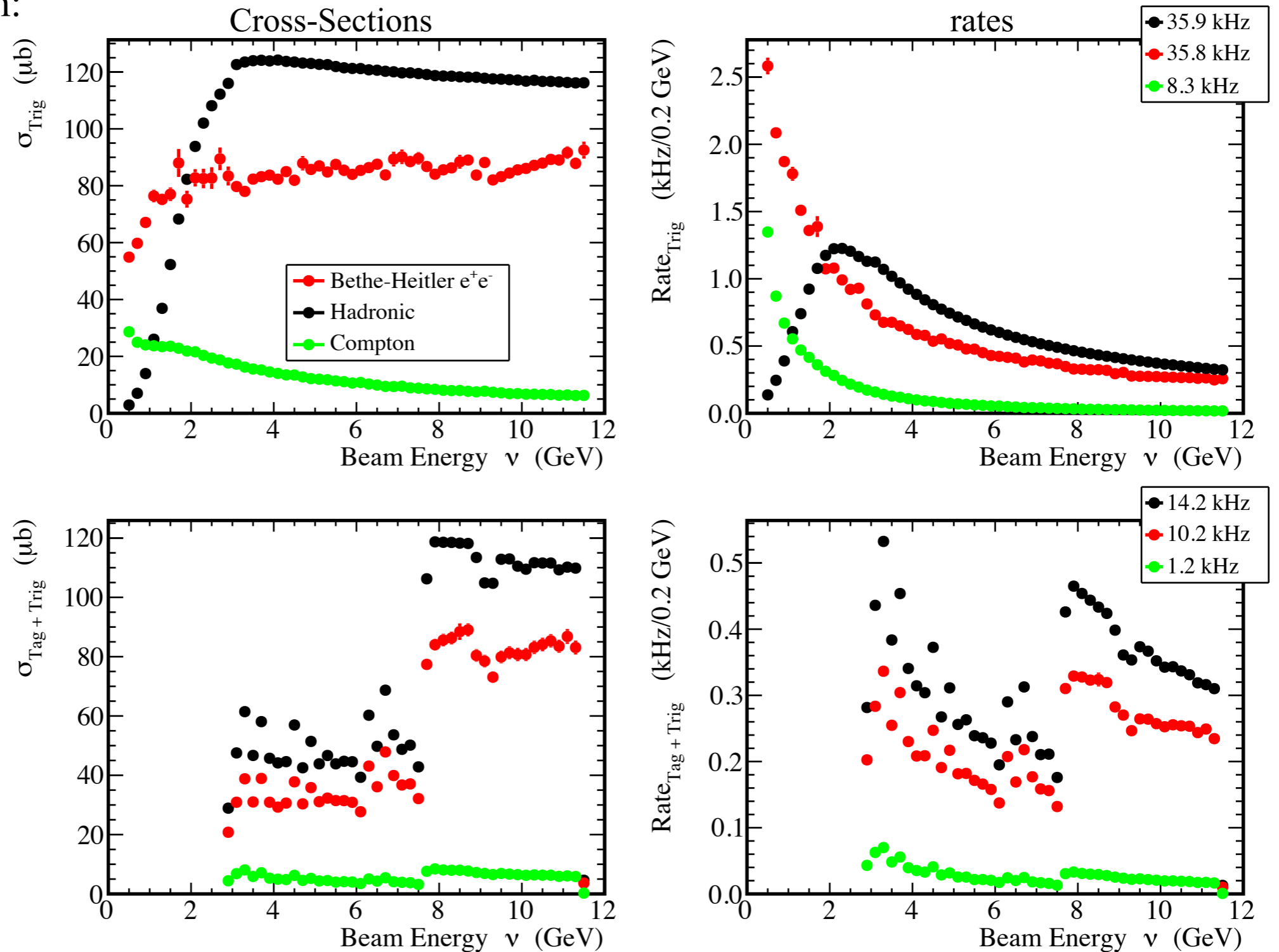
Fit: $\sigma^{3/2} - \sigma^{1/2} = (450 \pm 34) s^{-0.691 \pm 0.029}$

Should measure well the first non-zero deuteron signal at large ν .

Rates and backgrounds

Unpolarized backgrounds: cancel in yield or cross-section difference.
However, may still affect the experiment by saturating DAQ.

HD GEANT simulation:



Total rate; 80 kHz (Hall D present DAQ capacity)

Useful hadronic rate: 35 kHz

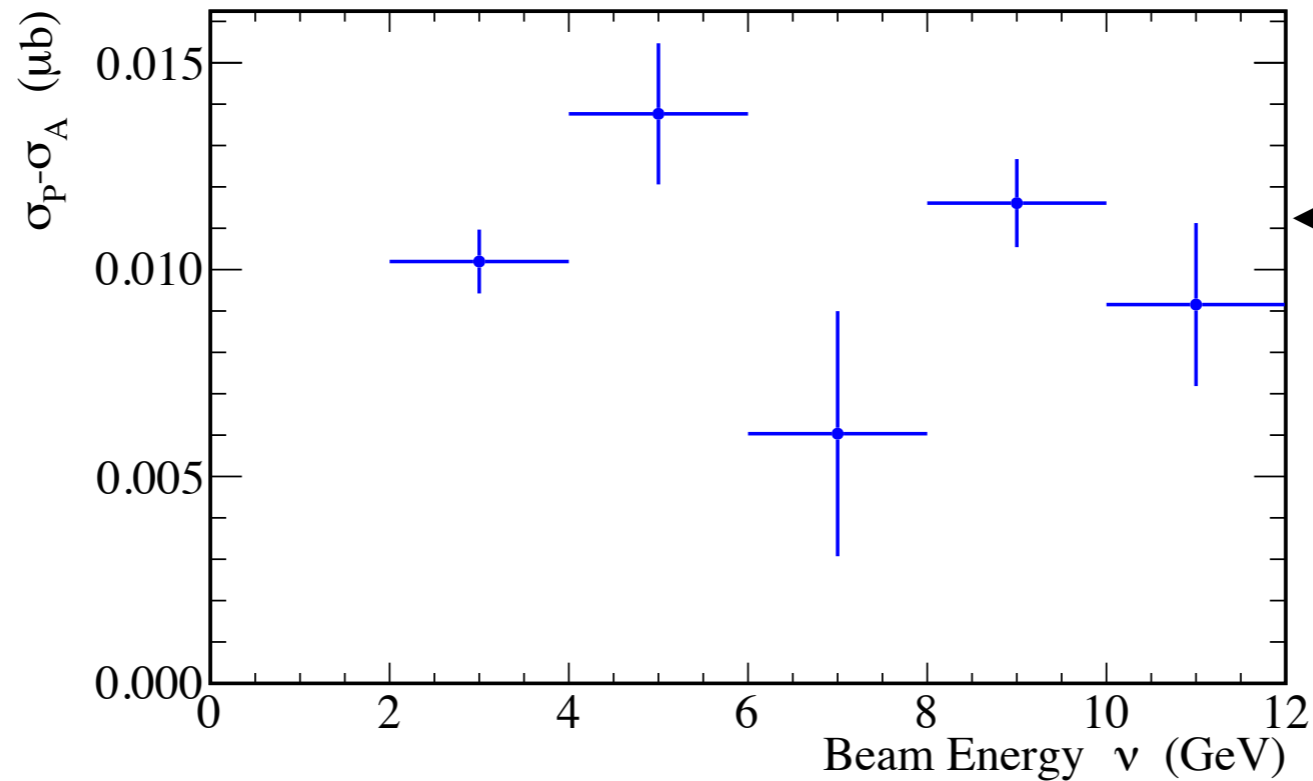
Confirmed with GlueX data (Kapton data from empty target run. Kapton thickness scaled to 10 cm yields ~ 50 kHz)

Rates and backgrounds

Polarized backgrounds: contribute, but very small ($\sim 0.2\%$ contamination).

Bethe-Heitler Cross-Section difference

HD GEANT simulation:



Compare $\sim 0.01 \mu\text{b}$ (B-H)
with $\sim 5 \mu\text{b}$ (hadronic)

No polarized Compton contribution (FROST electrons unpolarized).

Impact

- Measuring high ν -behavior will test **the convergence of GDH sum** (fast and robust analysis: **early goal**)
 - First measurement well outside resonance region: **first clean test of Regge theory for polarized case.**
 - If Regge theory works: **$\Delta\alpha_{a1} = \pm 0.007$ & $\Delta\alpha_{f1} = \pm 0.029$** . Compare to $\Delta\alpha_{a1} = \pm 0.23$ & $\Delta\alpha_{f1} = \pm 0.22$ from ELSA. This will enable a **reliable assessment of the contribution up to $\nu \rightarrow \infty$** .
 - First measurement of non-zero polarized signal for deuteron at large ν .
- Obtaining cross-section (more difficult: **longer term goals**) will:
 - Improve accuracy of **proton GDH Sum Rule determination** by $\sim 25\%$
 - Allow for the **first neutron GDH Sum Rule determination**
 - Allow the **determination of Compton amplitude f_2** .
 - **Improve calculation of atomic hyperfine splitting** by determining spin structure function $g_1(Q^2=0)$.
 - **$Q^2=0$ baseline for g_1 for EIC.** \implies study of the **transition between DIS and diffractive regimes.**
- Once Hall D has a polarized target, **a rich program opens**. Sensible to initiate it with **simplest experiment and a robust observable**.

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This will be precise enough to resolve the discrepancy between DIS data and Regge theory.
 - First measurement of Regge theory predicts $\alpha_{a1} \cong -0.34$, while
Several DIS fits yield $\alpha_{a1} \cong +0.45$.
- Obtaining a robust observable
 - Improve accuracy of proton GDH Sum Rule determination by $\sim 25\%$
 - Allow for the first neutron GDH Sum Rule determination
 - Allow the determination of Compton amplitude f_2 .
 - Improve calculation of atomic hyperfine splitting by determining spin structure function $g_1(Q^2=0)$.
 - $Q^2=0$ baseline for g_1 for EIC. \implies study of the transition between DIS and diffractive regimes.
- Once Hall D has a polarized target, a rich program opens. Sensible to initiate it with simplest experiment and a robust observable.

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$$\int_{v_{\text{thr}}}^{\infty} (\sigma^{3/2} - \sigma^{1/2}) \frac{dv}{v} = \frac{2\alpha\pi^2 \kappa^2}{M^2}$$

Thank you

One-slide summary

$$\int_{v_{\text{thr}}}^{\infty} (\sigma^{3/2} - \sigma^{1/2}) \frac{dv}{v} = \frac{2\alpha\pi^2 k^2}{M^2}$$

- First measurement of the high- v behavior of GDH integrand $(\sigma^{3/2} - \sigma^{1/2})/v$
- Hall D + FROST target (H and D) + polarized electron beam on a amorphous radiator.
- Hall D is uniquely suited for such measurement.
- High- v is where a failing of the sum rule would be revealed.
- Early goal: map yield difference $N^{3/2} - N^{1/2}$ for the proton and neutron. This will elucidate the convergence of GDH integrals.
 - Point-to-point correlated errors cancel.
 - Unpolarized background cancel.
- 21-days 12 GeV measurement provides α_{f1} and α_{a1} at 2% level (present uncertainties: 50%)
- 12-days at 4 GeV bridge gap between 12 GeV and low energy data. Data overlap: much improved precision + cross-check of experiments.
- Solve discrepancy between DIS data and Regge theory prediction.
- Provide first non-zero data on $\sigma^{3/2} - \sigma^{1/2}$ at high- v for the deuteron.
- Longer term goals (regardless of the convergence and sum rule validity):
 - Verify proton GDH sum rule within 6% & allows first verification of neutron GDH sum rule.
 - Allow extraction of complex Compton amplitude f_2 and new test of Chiral Perturbation Theory.
 - Improve knowledge of atomic hyperfine splitting.
 - Polarized diffractive scattering phenomenology essentially unknown. $Q^2=0$ baseline for g_1 for EIC.
 \implies study of the transition between DIS and diffractive regimes.
- Once Hall D has a polarized target, a rich program opens. Sensible to initiate it with simplest experiment and a robust observable.

$$\int_{v_{\text{thr}}}^{\infty} (\sigma^{3/2} - \sigma^{1/2}) \frac{dv}{v} = \frac{2\alpha\pi^2 \kappa^2}{M^2}$$

Back-up slides

Why is Hall D uniquely suited for a large- ν GDH measurement?

PRO:

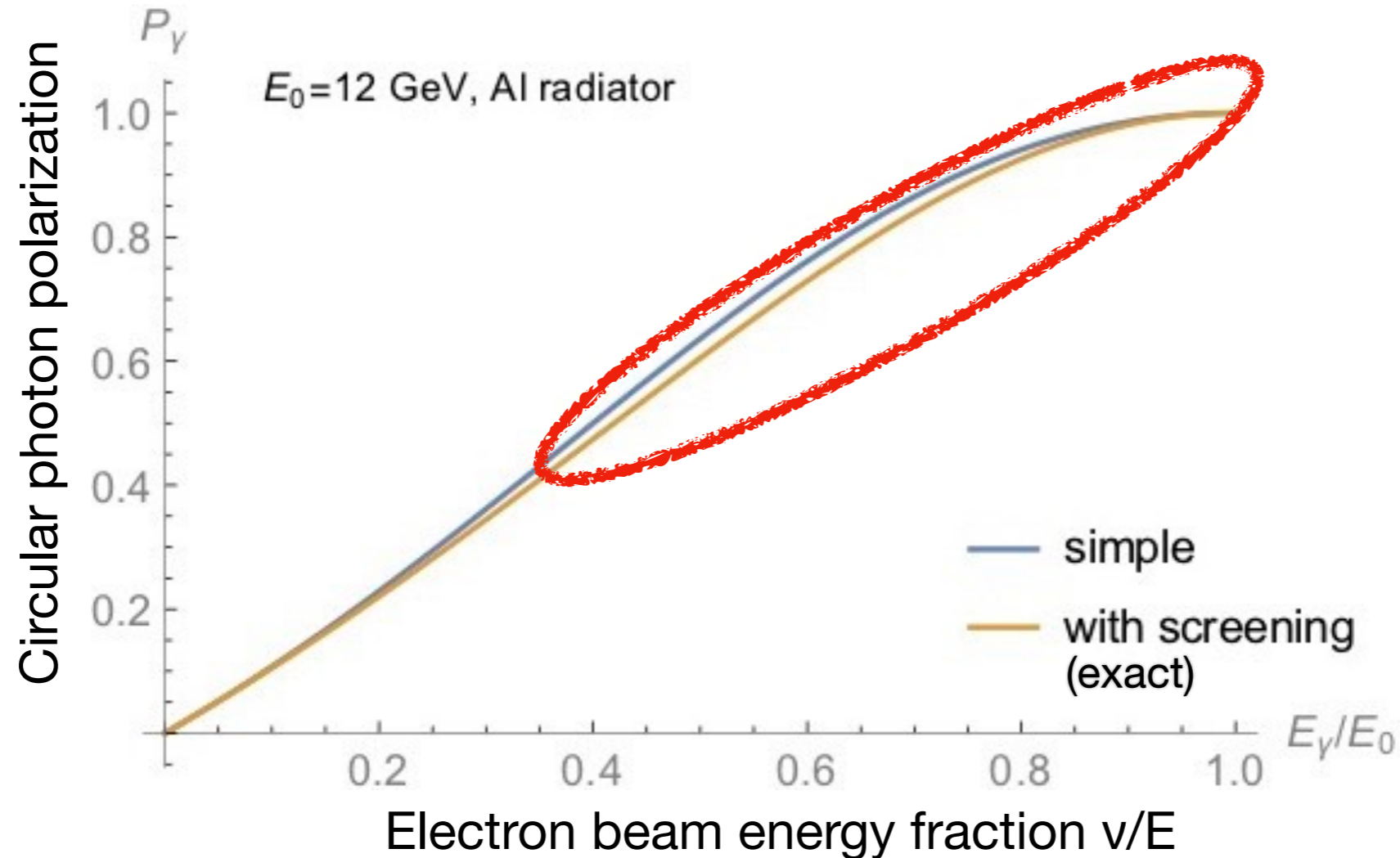
- Hall D: only Hall with photon tagging capability,
- A GDH measurement via electroproduction is not adapted to its study at large ν :
 - Would need to be done at low enough Q^2 ($< 0.02 \text{ GeV}^2$) to reliably extrapolate to $Q^2 = 0$.
 - At 11 GeV, low enough $Q^2 \Rightarrow$ scattering angles smaller than 0.8° .
 - No hall has this capability (CLAS12 forward tagger is limited to 2.5°).
 - Elastic radiative tails are prohibitively large. They will furthermore saturate the DAQ.
- g_1 cannot be separated from g_2 in Hall B without a transverse target. Need model input but g_2 behavior at very low Q^2 and large ν is not known.
- The largest ν reachable in Hall B for inclusive data is 8 GeV, compared to 12 GeV in Hall D.
- No possible $Q^2 = 0$ extrapolation: 8 GeV and $2.5^\circ \Rightarrow Q^2 = 1 \text{ GeV}^2$.

CON:

Hall D does not have a polarized target. However, its cost is moderate ($\sim \$600\text{K}$) and it opens an opportunity for new physics program.

Circularly polarized beam

- Polarized electron beam;
- Amorphous radiator.



- Needed
 - Electron beam helicity reporting;
 - Beam charge asymmetry control.
- Not needed
 - Polarimetry (can still be done with injector's Mott polarimeter+spin precession);
 - High photon energy resolution (present < 0.5% more than enough).

Polarized target

Options are polarized **HDice** or **FROST**

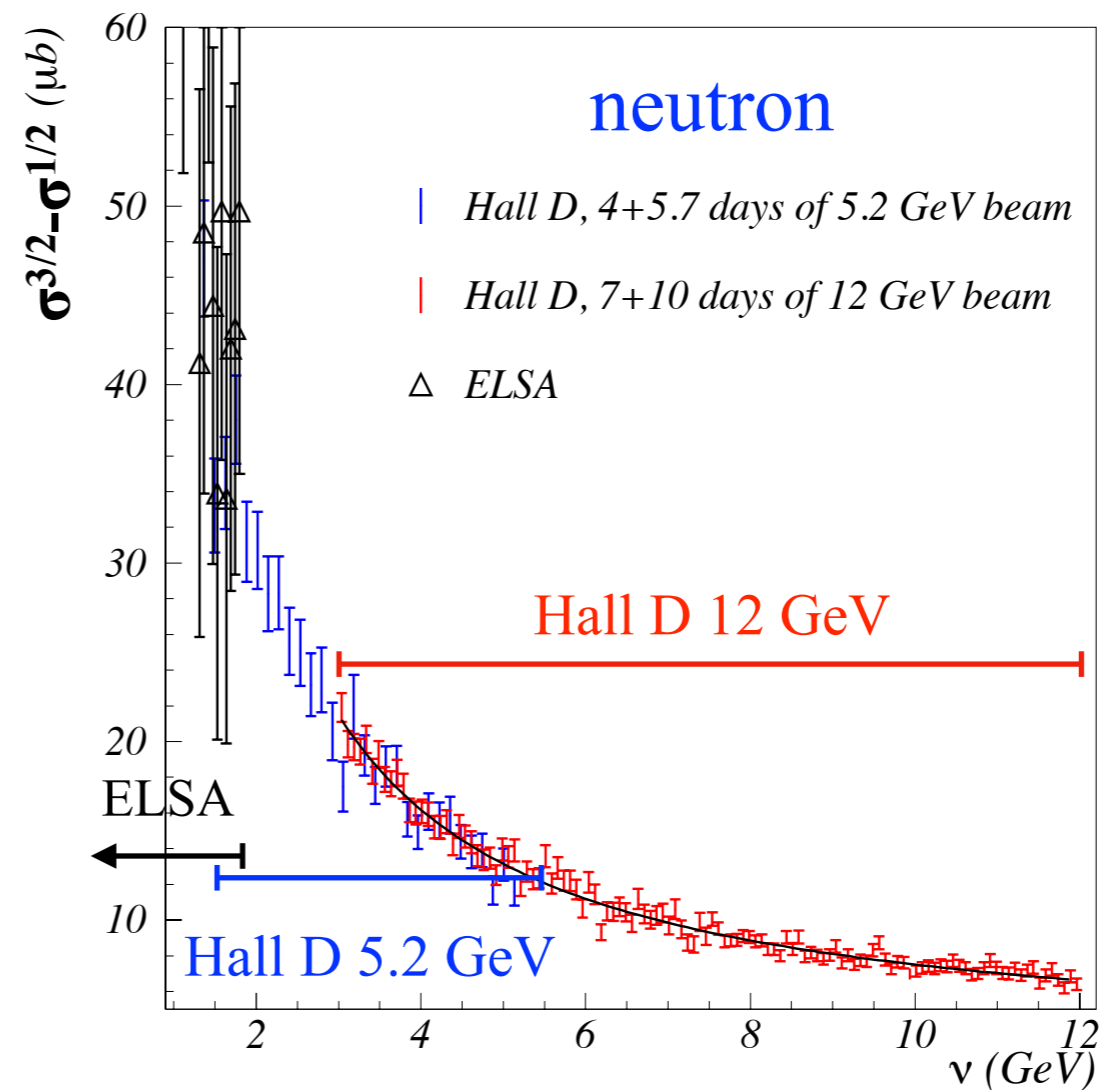
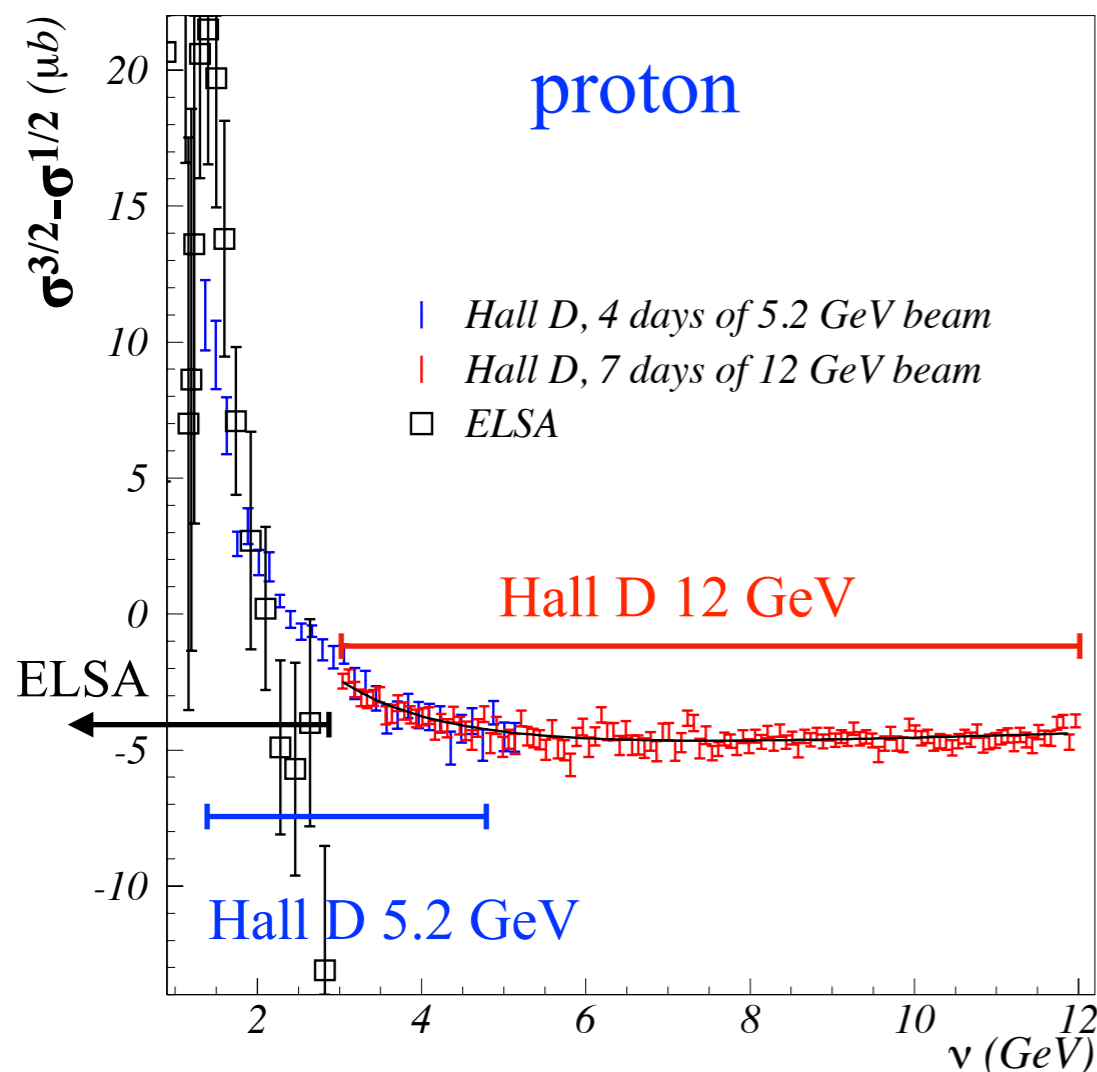
- **HDice**: best figure of merit (low dilution, high sustainable photon flux), but **complex to prepare and use**.
- **FROST**: best polarization, easier to use, but **high dilution and lower maximum flux**.
- Running one **short experiment**: not enough to **invest in HDice**.
- **FROST dilution not an issue** for GDH thanks to **high rate Hall D DAQ**. Also, **dilution cancels** in physics analysis: $(N^{3/2}+N^0) - (N^{1/2}+N^0) = N^{3/2} - N^{1/2}$
 \Rightarrow **use FROST**
- Target group prefers to build dedicated Hall D FROST target rather than to import Hall B one.
- Two months to install the target. No commissioning needed.
- Cost estimate: ~\$600k

FROST characteristics:

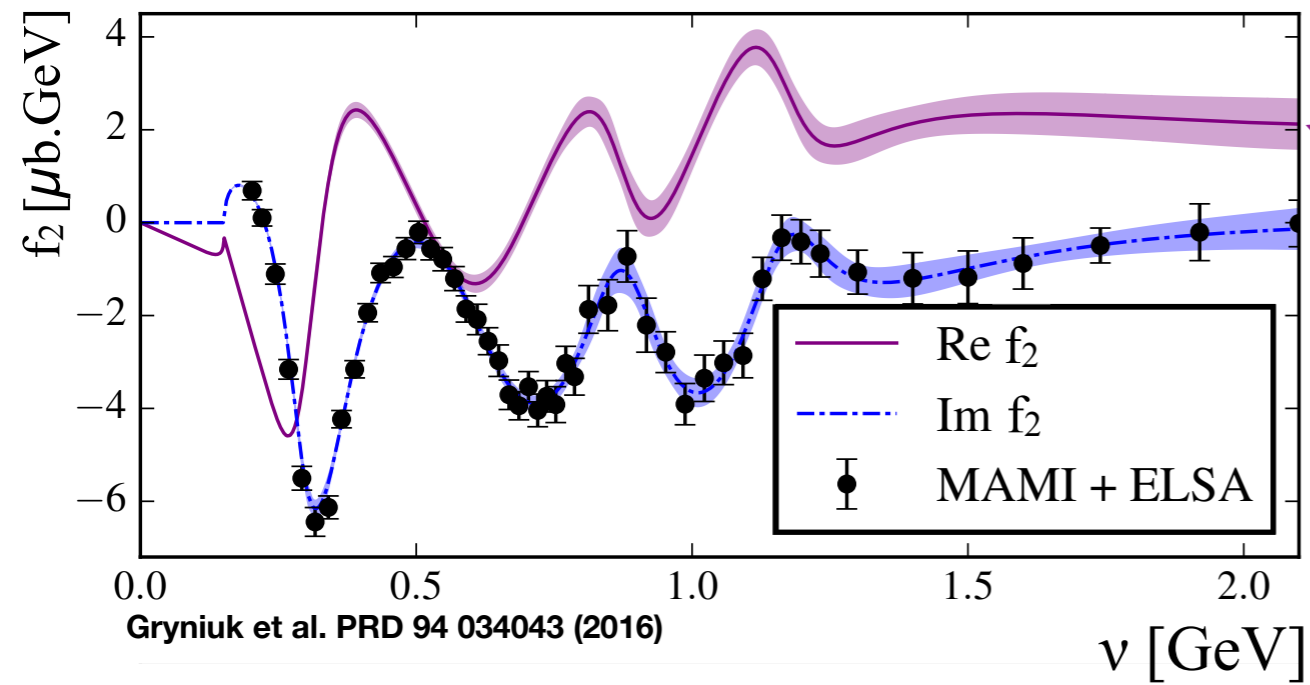
- Dynamical Nuclear Polarization on Butanol (**C₄H₉OH** or **C₄D₉OD**)
- P and D **polarizations: up to 90%**. Need to be re-polarized every 5-7 days (5h process).
- **Only longitudinal polarization needed**. Anti-parallel polarization possible. Not required for GDH.
- Need to install cryogen lines (or dewars) for cooling.
- Sustainable *total* photon flux $\sim 10^8 \text{ s}^{-1}$. Could be up to 10^9 s^{-1} (need additional small magnet on target nose).

Low energy run

- Allows to **overlap/bridge gap** between ELSA and Hall D data.
- 12 days. Nominal energy: **4 GeV**.
- Consulted with accelerator experts (J. Benesh, T. Satogata). **Feasible**, with two solutions:
 - 1: **Run at lower linac energy**:
 - Advantage: **simplest solution**.
 - Issues:
 - Invasive to other halls high energy runs \Rightarrow Scheduled during a **low energy summer run**?
 - Operate somewhat below CEBAF dipoles mapping \Rightarrow Beam **set-up will take longer**.
 - 2: **Run at less than 5.5 passes**:
 - Issue: Never done before. **Require R&D and tests**.
 - Advantages:
 - **Non-invasive**.
 - **Expand Hall D capabilities**.
- If the above is too difficult, **5.2 GeV** possible. Same as Summer 2019: known configuration. Only a scheduling matter.

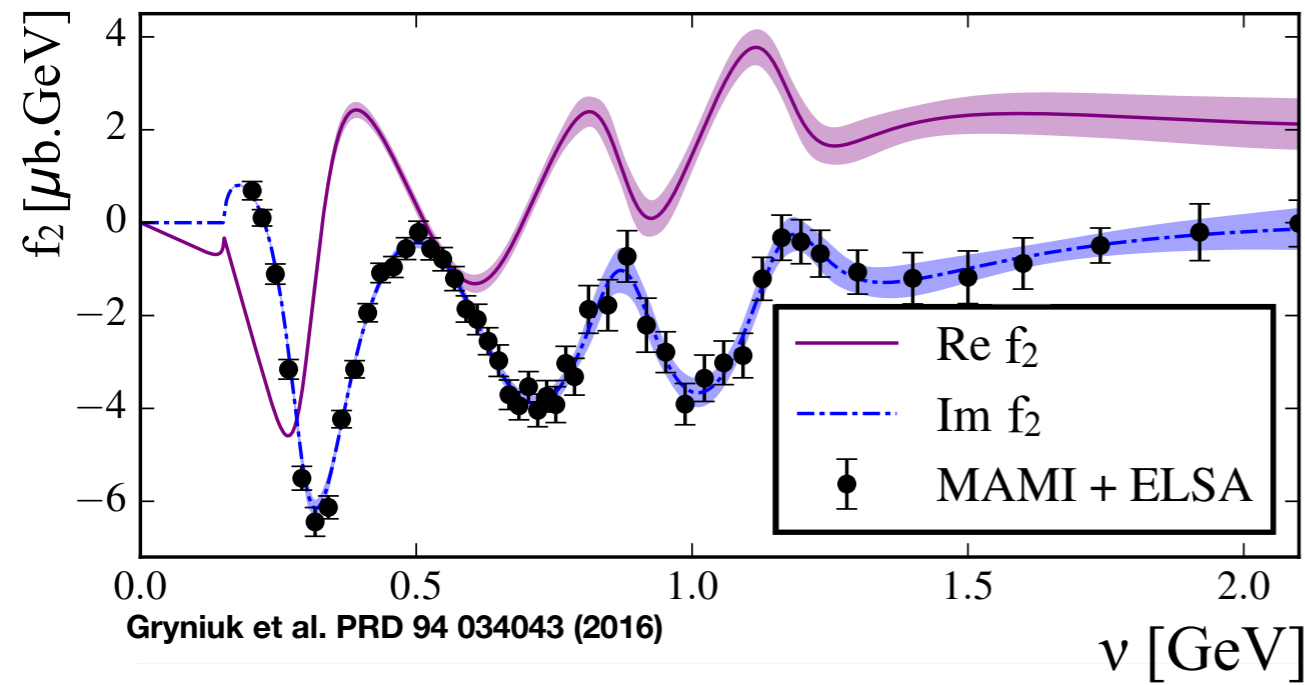


Extraction of the real and imaginary parts of Compton amplitude f_2

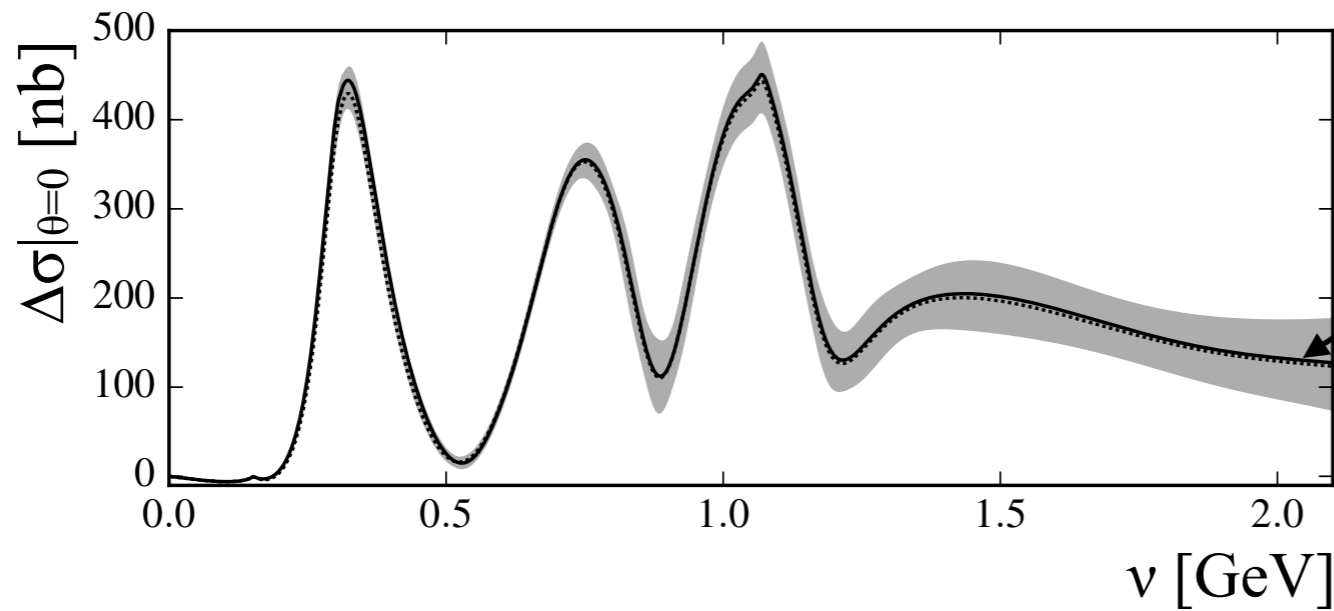


Dispersive analysis from $\text{Im}(f_2)$ data. Large v data will constrain both $\text{Re}(f_2)$ and $\text{Im}(f_2)$ error bands.

Extraction of the real and imaginary parts of Compton amplitude f_2

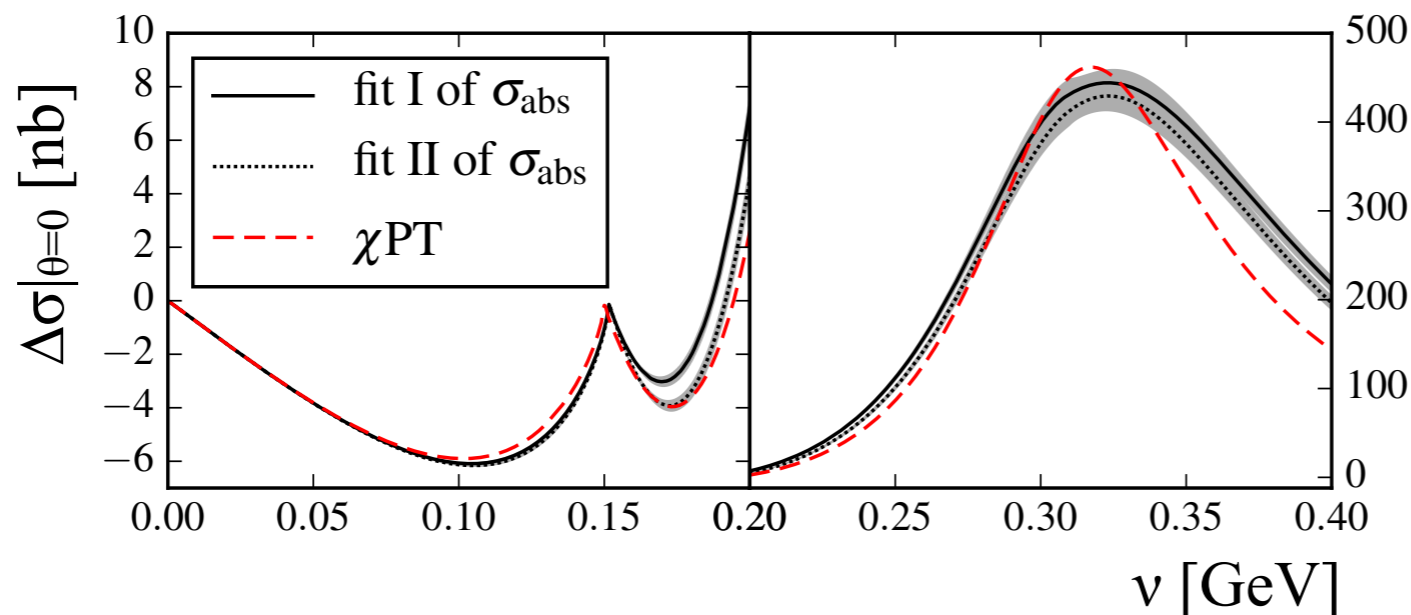
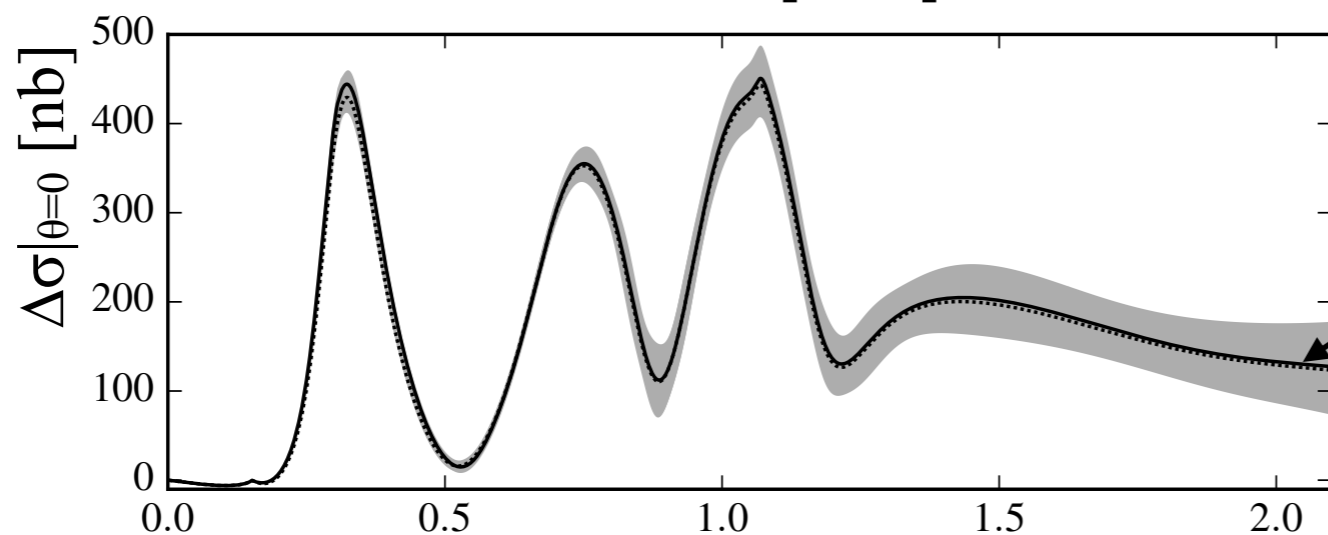
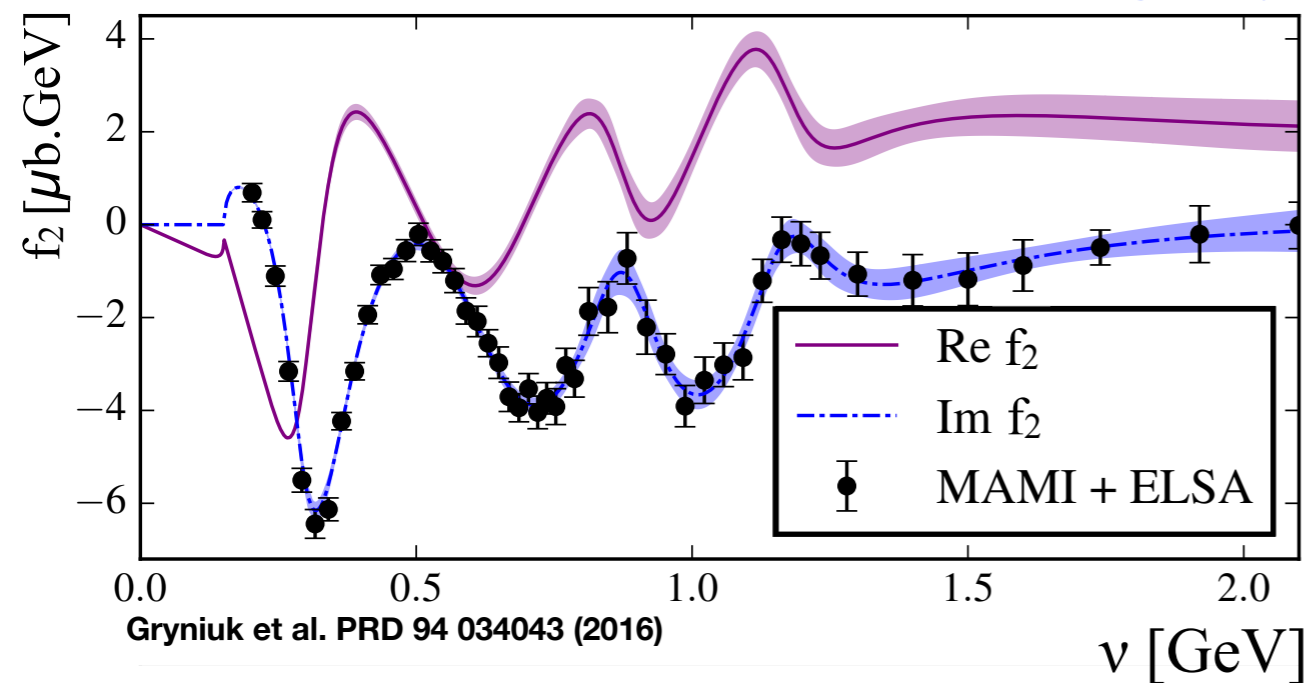


From $\text{Re}(f_2)$ and $\text{Im}(f_2)$ and the well measured unpolarized f_1 , one gets $\sigma^{3/2} - \sigma^{1/2} \stackrel{\text{def}}{=} \Delta\sigma$ in the forward limit.



Large v data will constrain increasing error band.

Extraction of the real and imaginary parts of Compton amplitude f_2



Chiral Perturbation Theory (χpT) calculation available.

$\Delta\sigma|_{\theta=0}$ very sensitive to chiral loops.

\Rightarrow Test of χpT at $Q^2=0$.

Complement JLab program GDH at low Q^2 that tested and challenged χpT in the polarized sector.

The Gerasimov-Drell-Hearn sum rule

$$\int_{\nu_{\text{thr}}}^{\infty} (\sigma^{3/2} - \sigma^{1/2}) \frac{d\nu}{\nu} = \frac{4\alpha S \pi^2 \kappa^2}{M^2}$$

Spin-dependent total photoproduction cross-sections
Photon energy
anomalous magnetic moment
spin

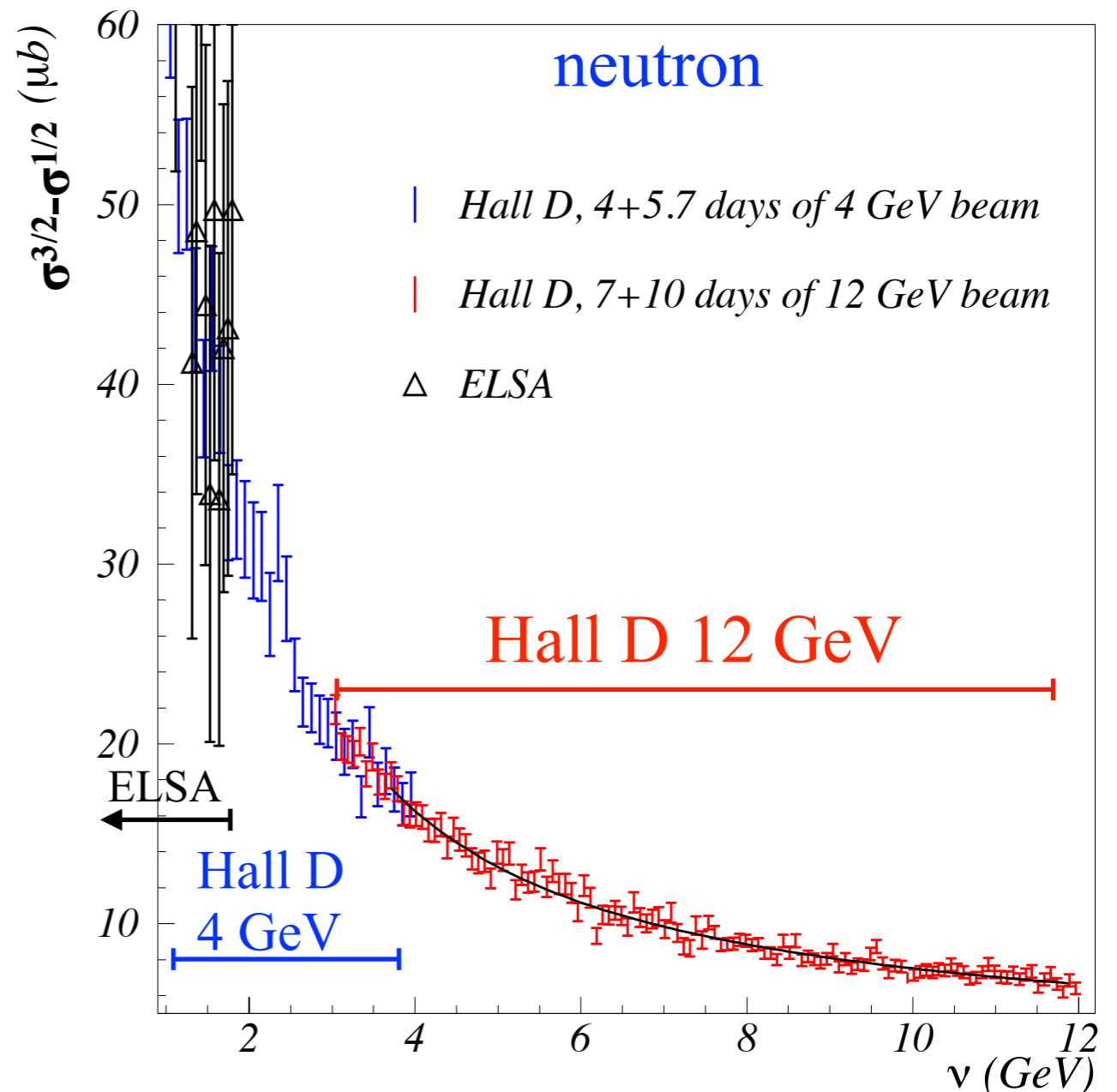
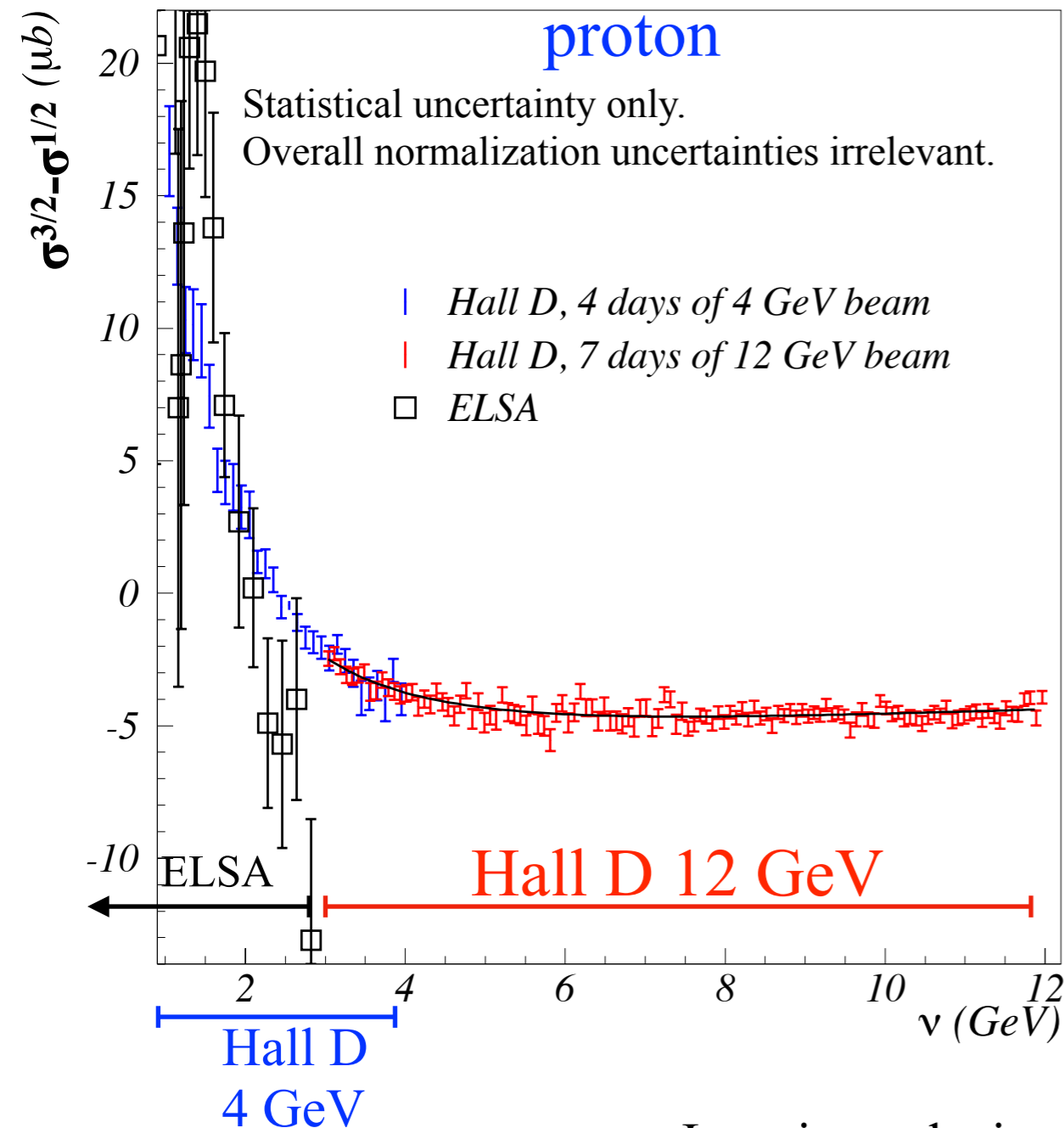
- **Fundamental Quantum Field Theory prediction.** Applicable to any type of target.
 - Different targets test different properties of Nature:
 - Electron target: QED test, electron compositeness.
 - Nucleon target: QCD, nucleon structure.
- Conditions for the sum rule to be valid:
 - **Spin-dependent forward Compton amplitude $f_2(\nu)$ must vanish at large ν** (no-subtraction hypothesis).
 - Imaginary part of f_2 , **$(\sigma^{3/2} - \sigma^{1/2})$ must decrease with ν faster than $\sim 1/\ln(\nu)$** (for the integral to converge).
- GDH on nucleons: Integral gets most contribution for $\nu < 2$ GeV, but **if the sum rule fails, it would happen at high energy.**
 - Proton: $\nu > 3$ GeV not measured yet.
 - Neutron: $\nu > 1.8$ GeV not measured yet.
- Nucleon **polarized cross-section unknown at large ν .** Expected to be described by Regge theory.
- Relatively simple experiment and analysis.
- With its tagger, large solid angle detector and high flux, **Hall D is uniquely suited to perform a GDH experiment.**

Possible mechanisms that could invalidate the GDH sum rule

- GDH: Fundamental QFT prediction.
- for GDH on hadron: QCD determines convergence of integral and sum rule validity.
 - Possible violation mechanisms:
 - A $J=1$ pole of the nucleon Compton amplitude;
 - Chiral anomaly;
 - Quark substructure (non-zero quark anomalous moment);
 - Other, more exotic possibilities, have been proposed, e.g. local break-down of EM gauge invariance

Expectations

- **1 week of running on proton**: Minimum reasonable time, given overhead \Rightarrow **10 days on deuteron**.
- Valuable to also take data at lower energy: **1 week (p+n) at 4 GeV**.
- For simulating expected data, use Regge theory: $\sigma^{3/2}-\sigma^{1/2} = c_2 s^{\alpha_{f_1}-1} \pm c_1 s^{\alpha_{a_1}-1}$
 $s=2Mv+M^2$, α_{f_1} , α_{a_1} : **Regge intercepts** of $f_1(1285)$ and $a_1(1260)$ trajectories, and $c_{2,1}$: parameters.
- $7 \times 10^7 \text{ s}^{-1}$ collimated flux ($3 < v < 12 \text{ GeV}$), **Pb=80%, Pt=80%**.
- **10 cm** target on usual butanol density



Isospin analysis \Rightarrow $\Delta\alpha_{a_1}=\pm 0.007$ & $\Delta\alpha_{f_1}=\pm 0.029$