

# Updates on $\eta \rightarrow \gamma\gamma\pi^0$

Igal Jaeglé

Thomas Jefferson National Accelerator Facility

for the GlueX Collaboration

May 3, 2024



# Table of contents

- 1 GAMS-2000 experiment and results
- 2 A2 experiment and results
- 3 GlueX/JEF Basic Selection Criteria
- 4 Physics-Informed Neural Network

# GAMS-2000 setup

## Electromagnetic decays of light mesons - L.G. Lansberg

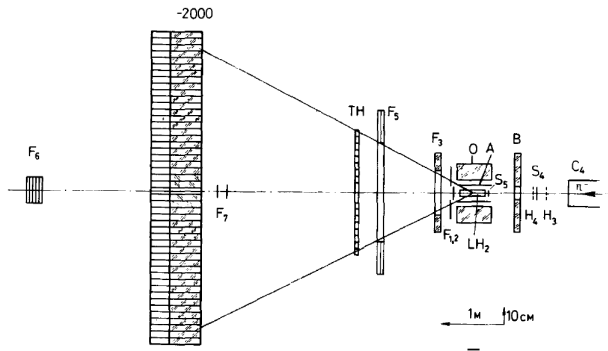


Fig. 6. The layout of GAMS-2000. The main unit of this apparatus is the hodoscope Čerenkov  $\gamma$ -spectrometer,  $48 \times 32$  matrix of total absorption lead-glass counters.  $S_4$ ,  $S_5$ ,  $H_3$ ,  $H_4$  - scintillation counters and hodoscopes of the  $\pi^-$ -beam;  $LH_2$  - liquid hydrogen target;  $A$ ,  $O$ ,  $F_{1,2}$ ,  $B$  - guard counters;  $F_{6,7}$  - beam-killing system;  $TH$  hodoscope was not used in the  $\eta \rightarrow \pi^0 \gamma \gamma$  search.

- 30 GeV  $\pi^-$  beam,  $\sim 3 \times 10^{11} \pi^-$  on target
- $\pi^- p \rightarrow \eta^{(\prime)} n$ ,  $6 \times 10^5 \eta$  produced via this process

# GAMS-2000 results

## Electromagnetic decays of light mesons - L.G. Lansberg

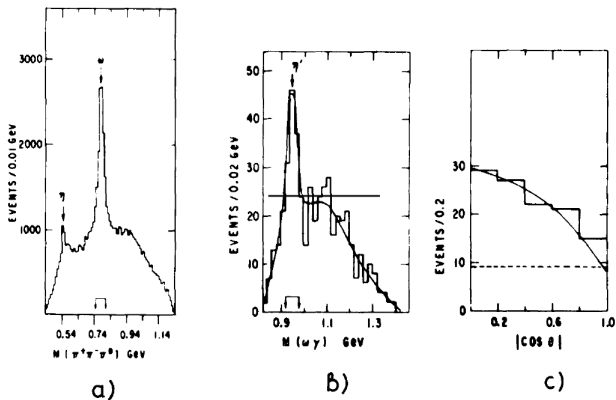


Fig. 5. (a)  $\pi^+\pi^-\pi^0$  effective mass spectrum (68962 events), showing the 750–810 MeV  $\omega$ -mass cut. (b)  $\omega\gamma$  effective mass distribution (478 events). The curve is the result of a two-parameter fit: (the  $\eta'$  peak is parametrized by a Gaussian of central mass 955 MeV and an instrumental width of 50 MeV) + (background represented by Monte-Carlo generated, acceptance corrected  $\omega\pi^0$  phase space events from which one  $\gamma$  out of the four was randomly detected). (c) Distribution in  $|\cos\theta|$  (corrected for acceptance) for 114 events between the arrows in (b). The solid line represents the best fit by the form:  $a + b(1 - \cos^2\theta)$ . The dotted line represents the background subtraction of 45 events obtained from the fit on (b).

- GAMS-2000  $\mathcal{B}(\eta' \rightarrow \omega\gamma) = 2.8 \pm 0.5\%$
- PDG-2022  $\mathcal{B}(\eta' \rightarrow \omega\gamma) = 2.52 \pm 0.07\%$

# GAMS-2000 results

## Electromagnetic decays of light mesons - L.G. Lansberg

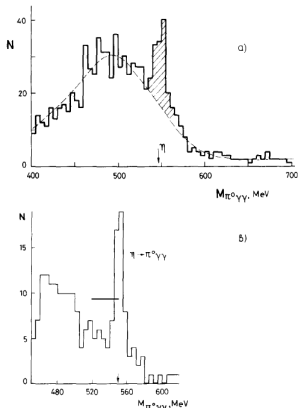


Fig. 7. (a) Mass spectrum of the  $\pi^0\gamma\gamma$  system measured in the reaction  $\pi^+\pi^-\rho \rightarrow \pi^0\gamma\gamma$ . The arrow points at the  $\eta$  mass. The background part of the spectrum (dashed curve) is largely due to the  $\eta \rightarrow 3\pi^0 \rightarrow 6\gamma$  (2.6) decay, with two "missed photons". (b) The same data, but analyzed with a new program for shower reconstruction. As a result the background from (2.6) with "missed photons" is greatly reduced.

- GAMS-2000  $\mathcal{B}(\eta \rightarrow \gamma\gamma\pi^0) = 0.07 \pm 0.016\%$
- PDG-2022  $\mathcal{B}(\eta \rightarrow \gamma\gamma\pi^0) = 0.0255 \pm 0.022\%$

No  $\omega \rightarrow \gamma\pi^0$  And no  $\eta' \rightarrow \gamma\omega$  with  $\omega \rightarrow \gamma\pi^0$  are shown,  $m_{\gamma\pi^0}$  cut applied?

$$\eta' \rightarrow \gamma\omega$$

Is a good reference channel candidate

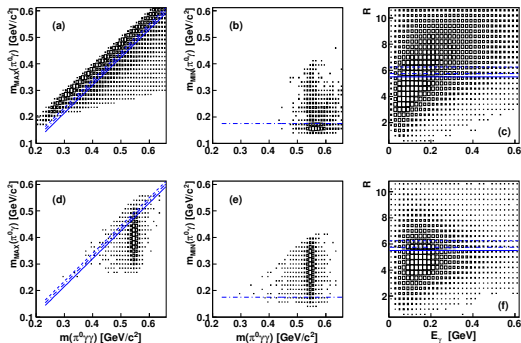
- $\mathcal{B}(\eta' \rightarrow \omega\gamma) = 2.52\%$ 
  - ▶  $\mathcal{B}(\omega \rightarrow \pi^0\pi^+\pi^-) = 89.2\%$
  - ▶  $\mathcal{B}(\omega \rightarrow \gamma\pi^0) = 8.28\%$
  - ▶  $\mathcal{B}(\pi^0 \rightarrow \gamma\gamma) = 98.823\%$
- $\mathcal{B}(\eta' \rightarrow \omega\gamma) = \mathcal{B}(\eta' \rightarrow \omega\gamma) \times \mathcal{B}(\omega \rightarrow \pi^0\pi^+\pi^-) \times \mathcal{B}(\pi^0 \rightarrow \gamma\gamma) = 2.247\%$
- $\mathcal{B}(\eta' \rightarrow \omega\gamma) = \mathcal{B}(\eta' \rightarrow \omega\gamma) \times \mathcal{B}(\omega \rightarrow \gamma\pi^0) \times \mathcal{B}(\pi^0 \rightarrow \gamma\gamma) = 0.204\%$
- Two decays can be reconstructed
- If  $\epsilon(\eta' \rightarrow \gamma\omega[\rightarrow \gamma\pi^0]) = \epsilon(\eta \rightarrow \gamma\gamma\pi^0)$ ,  $\frac{N(\eta' \rightarrow \gamma\omega[\rightarrow \gamma\pi^0])}{N((\eta \rightarrow \gamma\gamma\pi^0))} \sim 10$

In general, every rare decay studied should/must have a reference channel to validate the analysis

# A2 experiment

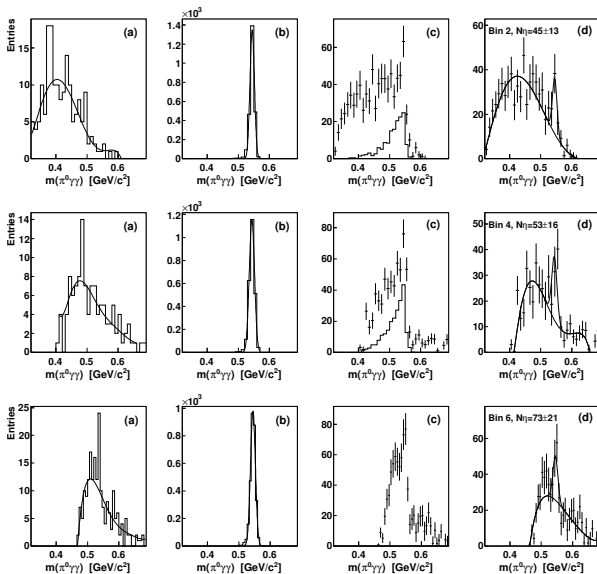
Key numbers and facts: [S. Prakhov et al. PRC 90, 025206 \(2014\)](#)

- $6 \times 10^7 \eta$  produced in  $\gamma p \rightarrow \eta p$  between threshold and 800 MeV
- 1200  $\eta \rightarrow \gamma\gamma\pi^0$  observed
- $\epsilon(\eta \rightarrow \gamma\gamma\pi^0)$  varies between 7 and 14 %
- $\frac{S}{B}$  varies between 30 and 50%
- Main backgrounds:
  - ▶ (a)  $\gamma p \rightarrow \pi^0\pi^0 p$ ,  $\pi^0\pi^0$  veto applied, cut applied similar to cutting  $\pi^0$ -peak in  $m_{\gamma\gamma}$
  - ▶ (b)  $\eta \rightarrow \gamma\gamma$ , peaking background produced mostly by shower splitting, eliminated by a  $m(\gamma\pi^0)$  cut
  - ▶ (c)  $\eta \rightarrow \pi^0\pi^0\pi^0$ , peaking background produced mostly by shower merging, strongly reduced by a cut on the shower effective radius



Currently testing shower effective radius cut

# A2 yield extraction



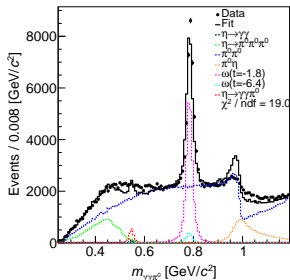
Best analysis on the market so far!



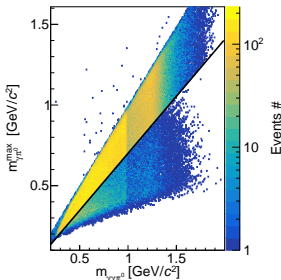
# GlueX/JEF Basic Selection Criteria

- 4 “photon” hypotheses DNeutral\_Shower with
  - $|t_{\gamma}^{\text{CAL}} - t_{\text{RF}}| \leq 2 \text{ ns}$
  - $E_{\text{cluster}} \geq 250 \text{ MeV}$
- $\chi_{\text{test}}^2$  to select best  $\gamma\gamma\pi^0$  combination and discriminate other possible final states ( $\pi^0\pi^0$ ,  $\pi^0\eta$ ,  $\eta\eta$ ,  $\pi^0\eta'$ ,  $\eta\eta'$ ,  $\eta'\eta'$ )
- $\chi_{\text{test}}^2$  to select best track coplanar to  $\gamma\gamma\pi^0$
- BCAL veto: allow only one “hadronic” shower and zero neutral shower both with
  - $|t_{\text{shower}}^{\text{BCAL}} - t_{\text{RF}}| \leq 6 \text{ ns}$
- $E_{\gamma} \geq 8.3 \text{ GeV}$

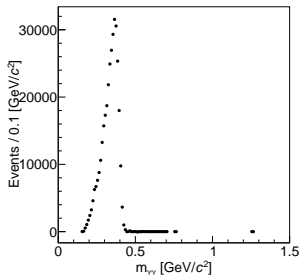
▶ As is



▶ MC simu  $\pi^0\pi^0$  background



▶ After A2- $\pi^0\pi^0$ -veto for  $\eta \rightarrow \gamma\gamma\pi^0$  MC signal



A2 veto not applicable as is

# GlueX/JEF Basic Selection Criteria

- 4 “photon” hypotheses DNeutral\_Shower with

- ▶  $|t_{\gamma}^{\text{CAL}} - t_{\text{RF}}| \leq 2 \text{ ns}$
- ▶  $E_{\text{cluster}} \geq 250 \text{ MeV}$

- ▶  $\chi_{\text{test}}^2$  to select best  $\gamma\gamma\pi^0$  combination and discriminate other possible final states ( $\pi^0\pi^0$ ,  $\pi^0\eta$ ,  $\eta\eta$ ,  $\pi^0\eta'$ ,  $\eta\eta'$ ,  $\eta'\eta'$ )

- ▶  $\chi_{\text{test}}^2$  to select best track coplanar to  $\gamma\gamma\pi^0$

- ▶ BCAL veto: allow only one “hadronic” shower and zero neutral shower both with

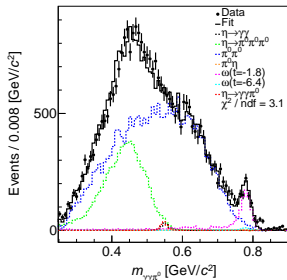
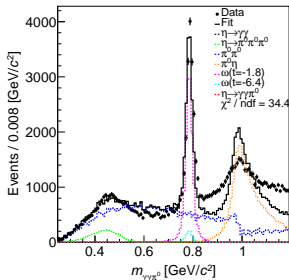
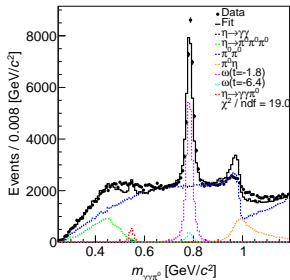
$$|t_{\text{shower}}^{\text{BCAL}} - t_{\text{RF}}| \leq 6 \text{ ns}$$

- ▶  $E_{\gamma} \geq 8.3 \text{ GeV}$

▶ As is

▶  $\pi^0\pi^0$ -veto ie  
!( $110 \leq m_{\gamma\gamma} \leq 160 \text{ MeV}/c^2$ )

▶  $\pi^0\pi^0$ - and  $\omega \rightarrow \gamma\pi^0$ -vetos ie  
 $m_{\gamma\pi^0} \leq 600 \text{ MeV}/c^2$



Compare to A2 does the boost really decreases the background?  $B \gg S!$

# $\eta \rightarrow \gamma\gamma$ background

Two sources:

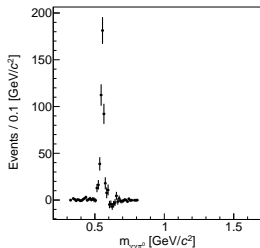
- $\gamma$  conversion mostly removed by TOF veto
- Shower splitting, latest Island Algorithm strongly reduced the splitting compared to Default Algorithm

TOF veto removed for 2017-01 run period MC simulation:

- $\sim 50\%$  of the  $\eta \rightarrow \gamma\gamma$  background
- $\sim 30\%$  of the  $\eta \rightarrow \gamma\gamma\pi^0$  signal

Splitting:

- Default Algorithm:  $\sim 0.04\%$  chance of splitting resulting to half of the peaking  $\eta \rightarrow \gamma\gamma$  background
- Island Algorithm: ? % chance of splitting resulting to ? of the peaking  $\eta \rightarrow \gamma\gamma$  background



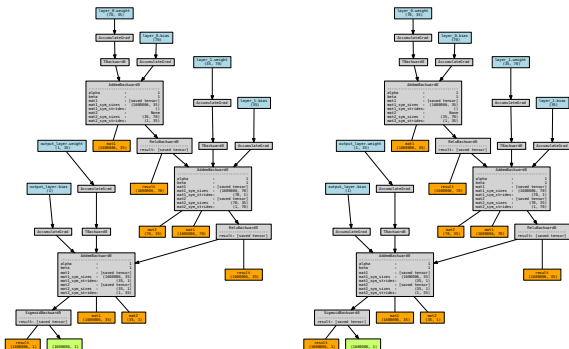
Kinematic fit is making the mass peak

# Physics-Informed Neural Network (PINN)

Based on P. Feichtinger et al. EPJC 82 (2022) 2, 121 and D. Lersch et al.

35 features or inputs:

- Process thrust,  $E_\gamma$ ,  $m_{\gamma\gamma\gamma\gamma}$ , and
- For each FCAL showers: SumV, SumU, E1E9, E5E29, cluster size in block number unit

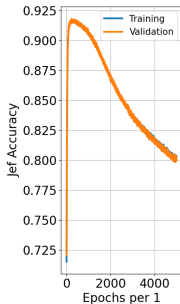
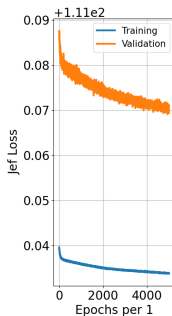
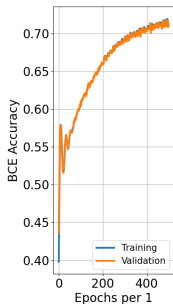
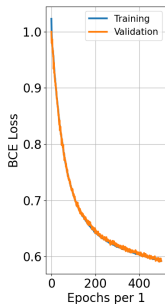


- 2 hidden layers with 70 and 35 neurons, respectively activated by RELU
- 1 sigmoid output

Training done into two steps: pre-training with BCE & final training with PINN per  $m_{\gamma\gamma}^i$ -slice and with a customized loss function

# Loss and accuracy

Customized loss function compares signal with overall statistical uncertainty in short  $\frac{\sqrt{S+B}}{S}$



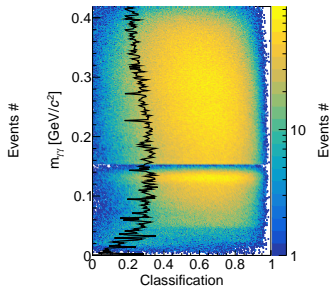
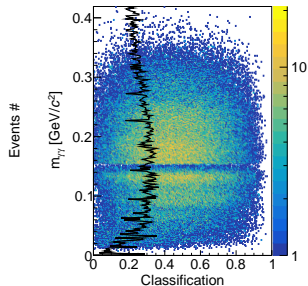
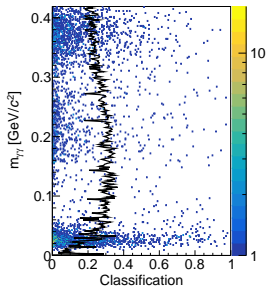
- Slice size,  $2\sigma - m_{\gamma\gamma}^i \leq m_{\gamma\gamma}^i \leq 2\sigma + m_{\gamma\gamma}^i$
- Trainings for every other slices, 5 $\sigma$  step
- Net architecture, activation function, loss rate, and number of epoch not tune yet via the HyPerparameter Optimization technique
- Loss function is also not optimized yet, different class of Figure-Of-Merit can be tested

Goal find set of cuts to get the smallest  $\frac{\sqrt{S+B}}{S}$  value or highest sensitivity

# Pre-training BCE

Results after the BCE pre-training

- 39.31M  $\gamma p \rightarrow \eta p$  with  $\eta \rightarrow \gamma\gamma$ , labeled as background
- 32.57M  $\gamma p \rightarrow \eta p$  with  $\eta \rightarrow \pi^0\pi^0\pi^0$ , labeled as background
- 10M  $\gamma p \rightarrow \eta p$  with  $\eta \rightarrow \gamma\gamma\pi^0$ , labeled as signal

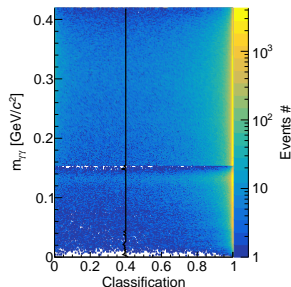
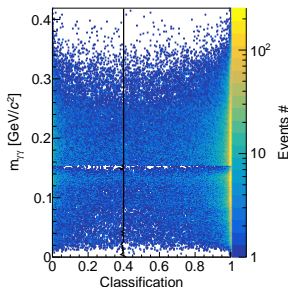
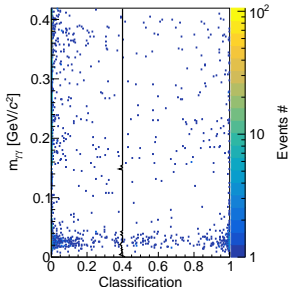


- Black line is the optimal threshold or smallest  $\frac{\sqrt{S+B}}{S}$  value
- BCE net output is in average  $0.25 \pm 0.1$

BCE model used as starting point for PINN training

## Results after the PINN training

- 39.31M  $\gamma p \rightarrow \eta p$  with  $\eta \rightarrow \gamma\gamma$ , labeled as background
- 32.57M  $\gamma p \rightarrow \eta p$  with  $\eta \rightarrow \pi^0\pi^0\pi^0$ , labeled as background
- 10M  $\gamma p \rightarrow \eta p$  with  $\eta \rightarrow \gamma\gamma\pi^0$ , labeled as signal

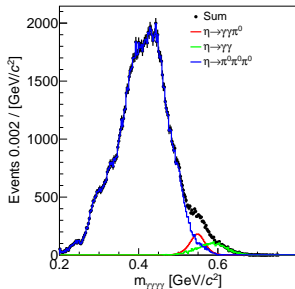


- Black line is the optimal threshold or smallest  $\frac{\sqrt{S+B}}{S}$  value
- PINN output is  $0.4 \pm 0.01$

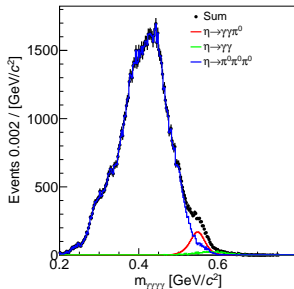
Use one value for all masses

# Testing samples

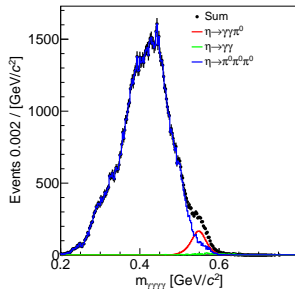
● Hand Crafted Cut (HCC)



● BCE



● PINN

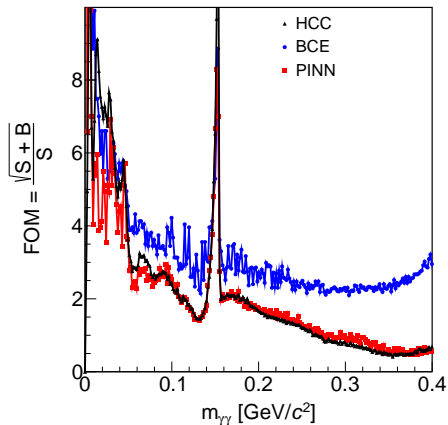


- PINN starts after the basic selection criteria described in slide 9
- Use reconstructed variables
- No TOF veto used,  $\eta \rightarrow \gamma\gamma$  background suppress by an order of magnitude w/o any cuts on  $m_{\gamma\gamma}$
- Working on including  $\pi^0\pi^0$  and  $\omega$  backgrounds



# FOM comparison

Between the HCC, BCE, and PINN:



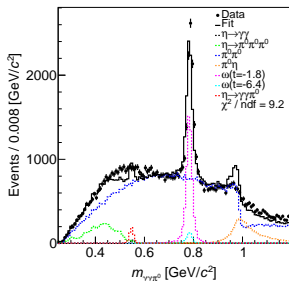
Ideally, PINN significance  $\gg$  HCC significance and PINN systematic error (not calculated yet)  $\sim$  HCC systematic error (also not calculated yet). But, it is not always the case.

# GlueX/JEF Advance Selection Criteria

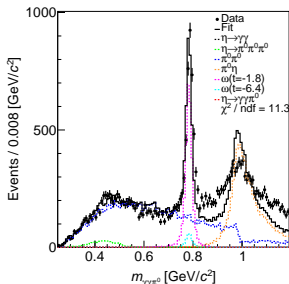
Basic selection criteria applied

- TOF-veto applied
- Only 4 FCAL clusters
- CL > 0.01%
- One photon in the insert

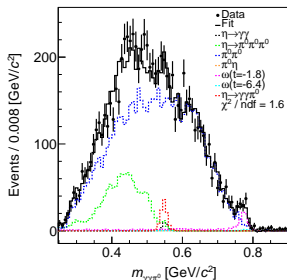
▶ As is



▶  $\pi^0\pi^0$ -veto ie  
!( $110 \leq m_{\gamma\gamma} \leq 160 \text{ MeV}/c^2$ )



▶  $\pi^0\pi^0$ - and  $\omega \rightarrow \gamma\pi^0$ -vetos ie  
 $m_{\gamma\pi^0} \leq 600 \text{ MeV}/c^2$



- $N_{\eta \rightarrow \gamma\gamma\pi^0}^{\text{expected}} \sim 550$  for  $53 \text{ pb}^{-1}$
- $N_{\eta \rightarrow \gamma\gamma\pi^0}^{\text{fit}} \sim 100$  for  $53 \text{ pb}^{-1}$
- If true,  $\mathcal{B} \sim 2.7 \times 10^{-4}/5$

# Conclusion

Reviewed GAMS-2000 and A2 results

- GAMS-2000 results on  $\eta \rightarrow \gamma\gamma\pi^0$  are completely off from the world average
- A2 results are the best on the market but so far were not reproduced

GlueX/JEF status

- A2-cuts are not working as is
- With HCC, GlueX/JEF S/B much worse than A2!
- As is we are leading toward an UL

PINN with customized loss function

- Require to understand fairly well the backgrounds
- Works fairly well on reduced background test samples, reduced  $\eta \rightarrow \gamma\gamma$  peaking background by an order of magnitude
- Start with a minimum set of HCC, this minimum has not been determined yet
- Significance and systematic errors must be competitive compared to HCC to be usable
- Less complicate model will also be explored