Coherent sources of $\pi^+\pi^-$

- 1. Primakoff $\gamma A \rightarrow \gamma \gamma A \rightarrow \pi^+ \pi^- A$
- 2. σ photo-production $\gamma A \rightarrow \sigma A \rightarrow \pi^+ \pi^- A$
- 3. ρ^0 photo-production $\gamma A \rightarrow \rho^0 A \rightarrow \pi^+ \pi^- A$

These process will interfere since they have identical final states

Incoherent sources of $\pi^+\pi^-$

1.
$$\gamma N \rightarrow \rho^0 N \rightarrow \pi^+ \pi^- N$$

2. $\gamma N \to \pi \Delta \to \pi^+ \pi^- N$ called the "Drell" process in the literature

In a nucleus Pauli blocking suppresses these processes at low t

Inelastic sources of $\pi^+\pi^-$

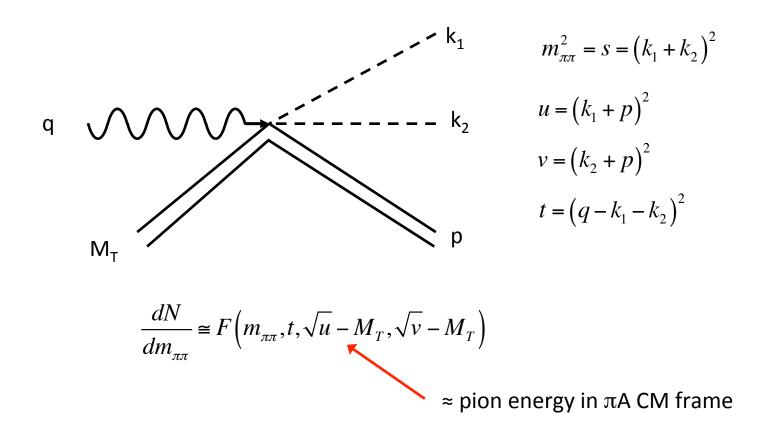
1.
$$\gamma A \rightarrow \omega A \rightarrow \pi^+ \pi^0 \pi^- A$$

2.
$$\gamma N \rightarrow \rho^0 \Delta \rightarrow \pi^+ \pi^- \pi N$$

3.
$$\gamma N \rightarrow \pi N^* \rightarrow \pi \pi \Delta \rightarrow \pi^+ \pi^- \pi N$$

Expect the first to be largest, since it's a coherent process

Final state interactions can occur in the $\pi^+\pi^-$, π^+A , and π^-A scattering states. Changes the distribution of events in 3-body phase space.



Experimentalists have used many different distributions to parameterize the $m_{\pi\pi}$ dependence of cross sections in the ρ^0 region

$$\frac{dN}{dm_{\pi\pi}} = F_{BW}\left(m_{\pi\pi}, m_{\rho}, \Gamma(m_{\pi\pi})\right) + F_{BKG}\left(m_{\pi\pi}\right)$$

 ${\sf F}_{\sf BW}$ is often taken as a relativistic Breit-Wigner, skewed, with an energy dependent width.

F_{BKG} is a non-resonant background: could have contributions from any of the coherent, incoherent or inelastic reactions, and from final state interactions.

• Bulos, McClellan and Zeus(Breitweg et al.) use this parameterization for the resonant part. Described as "relativistic p-wave Breit-Wigner", I believe originally derived by J.D. Jackson. Used in the CPP proposal development.

$$\Gamma = \Gamma_0 \frac{m_\rho}{m_{\pi\pi}} \left[\frac{m_{\pi\pi}^2 - 4m_\pi^2}{m_\rho^2 - 4m_\pi^2} \right]^{3/2} = \Gamma_0 \frac{m_\rho}{m_{\pi\pi}} \left(\frac{p_{cm}}{p_{cm@\rho^0 peak}} \right)^3$$

$$F_{BW}(m_{\pi\pi}) = \frac{m_{\pi\pi} \Gamma}{\left(m_\rho^2 - m_{--}^2 \right)^2 + m_\rho^2 \Gamma^2}$$

 Bulos et al. takes this for the backgound term: described as a FSI where the pion scatters diffractively (elastically) from the nucleus

$$F_{BKG}(m_{\pi\pi}) = c_1 \frac{m_{\rho}^2 - m_{\pi\pi}^2}{\left(m_{\rho}^2 - m_{\pi\pi}^2\right)^2 + m_{\rho}^2 \Gamma^2} + c_2$$

• Zeus(Breitweg et al.) assumes a constant background that's coherent with ρ^0 electro-production, and an incoherent background

$$\frac{dN}{dm_{\pi\pi}} = \left| \frac{\sqrt{m_{\pi\pi}m_{\rho}\Gamma}}{m_{\rho}^{2} - m_{\pi\pi}^{2} + im_{\rho}\Gamma} + C_{1} \right|^{2} + C_{2} \left(1 + 1.5m_{\pi\pi} \right)$$

 McClellan et al. includes a background term called the "Drell" term, and interference with Breit-Wigner. Since this looks like an incoherent process, so I'm not sure why there's an interference term

• Alvensleben et al. used five different parameterizations for dN/dm $_{\pi\pi}$

$$\begin{split} &\Gamma = \Gamma_0 \frac{m_\rho}{m_{\pi\pi}} \left[\frac{m_{\pi\pi}^2 - 4m_\pi^2}{m_\rho^2 - 4m_\pi^2} \right]^{3/2} & \text{Isn't the usual definition for this term} \\ &\frac{dN_1}{dm_{\pi\pi}} = \frac{m_\rho \Gamma}{\left(m_\rho^2 - m_{\pi\pi}^2\right)^2 + m_\rho^2 \Gamma^2} \left(\frac{m_\rho}{m_{\pi\pi}} \right)^4 + poly(m_{\pi\pi}) poly(k_\rho) poly(q_\perp) \\ &\frac{dN_2}{dm_{\pi\pi}} = \frac{m_\rho \Gamma}{\left(m_\rho^2 - m_{\pi\pi}^2\right)^2 + m_\rho^2 \Gamma^2} + c_1 \frac{1}{m_{\pi\pi}} \frac{m_{\pi\pi}^2 - m_\rho^2}{\left(m_\rho^2 - m_{\pi\pi}^2\right)^2 + m_\rho^2 \Gamma^2} + poly(m_{\pi\pi}) poly(k_\rho) poly(q_\perp) \\ &\frac{dN_3}{dm_{\pi\pi}} = \frac{m_\rho \Gamma}{\left(m_\rho^2 - m_{\pi\pi}^2\right)^2 + m_\rho^2 \Gamma^2} \left(\frac{m_\rho}{m_{\pi\pi}} \right)^4 + c_1 \frac{1}{m_{\pi\pi}} \frac{m_{\pi\pi}^2 - m_\rho^2}{\left(m_\rho^2 - m_{\pi\pi}^2\right)^2 + m_\rho^2 \Gamma^2} + poly(m_{\pi\pi}) poly(k_\rho) poly(q_\perp) \\ &\frac{dN_4}{dm_{\pi\pi}} = \frac{m_\rho \Gamma_0}{\left(m_\rho^2 - m_{\pi\pi}^2\right)^2 + m_\rho^2 \Gamma^2} + poly(m_{\pi\pi}) poly(k_\rho) poly(q_\perp) \\ &\frac{dN_5}{dm_{\pi\pi}} = \frac{m_\rho \Gamma}{\left(m_\rho^2 - m_{\pi\pi}^2\right)^2 + m_\rho^2 \Gamma^2} + poly(m_{\pi\pi}) poly(k_\rho) poly(q_\perp) \end{split}$$

• Zeus(Adloff et al.) assumes a $m_{\pi\pi}$ dependent background that's incoherent with ρ^0 electro-production:

$$\Gamma = \Gamma_0 \frac{m_{\rho}}{m_{\pi\pi}} \left(\frac{p_{\pi-cm}}{p_{\pi-cm@\rho^0 peak}} \right)^3 \frac{2}{1 + \left(\frac{p_{\pi-cm}}{p_{\pi-cm@\rho^0 peak}} \right)^2}$$

$$\frac{dN}{dm_{\pi\pi}} = \frac{m_{\pi\pi} \Gamma}{\left(m_{\rho}^2 - m_{\pi\pi}^2 \right)^2 + m_{\rho}^2 \Gamma^2} \left(\frac{m_{\rho}}{m_{\pi\pi}} \right)^{1.4} + \alpha_1 \left(m_{\pi\pi} - 2m_{\pi} \right)^{\alpha_2} e^{-\alpha_3 m_{\pi\pi}}$$

What can we expect to see in the low s region?

- Non-resonant backgrounds are a fact-of-life in hadronic physics, this is well known from photo-pion studies in the $\Delta(1232)$ region.
- Can reasonably expect that $dN/dm_{\pi\pi}$ should smoothly approach zero as $m_{\pi\pi} \rightarrow 2m_{\pi}$ over an interval of 100's of MeV, without a peaking at low $m_{\pi\pi}$. Not sure if all the models presented here obey this.
- Incoherent processes can be modeled with a Fermi-gas model type simulations. This would give predictions for the s,u,v, and t dependence of the reactions, but not absolute cross sections.
- The inelastic contribution from ω decay could be simulated.