

Amplitude analysis of GlueX ($p\eta'\pi^0$) data

Florida International University 2020

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Using mass constrained data for η and π^0
and Q-factor signal-background separation

1. Fitting only data for γ polarization plane angle relative to horizontal of 0° :
2. Fit intensity with different wave sets:
 - $S_0, P_{0,1}, D_{0,1,2}$ $\epsilon=+1$
 - $S_0, P_{0,1}, D_{0,1,2}$ $\epsilon=\pm 1$
3. Invariant mass bin size of $75 \text{ MeV}/c^2$, momentum transfer bin size of $0.6 (\text{GeV}/c)^2$

Plot acceptance uncorrected results

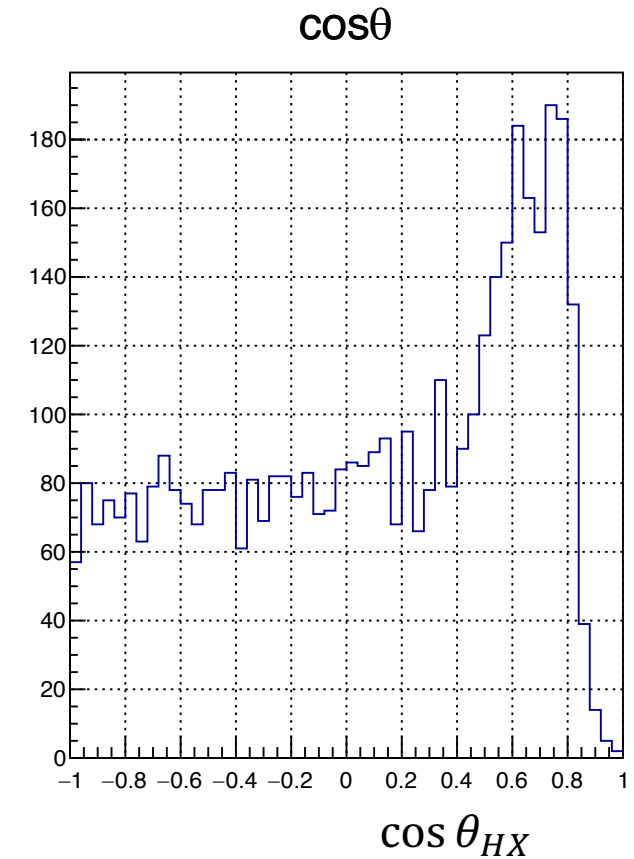
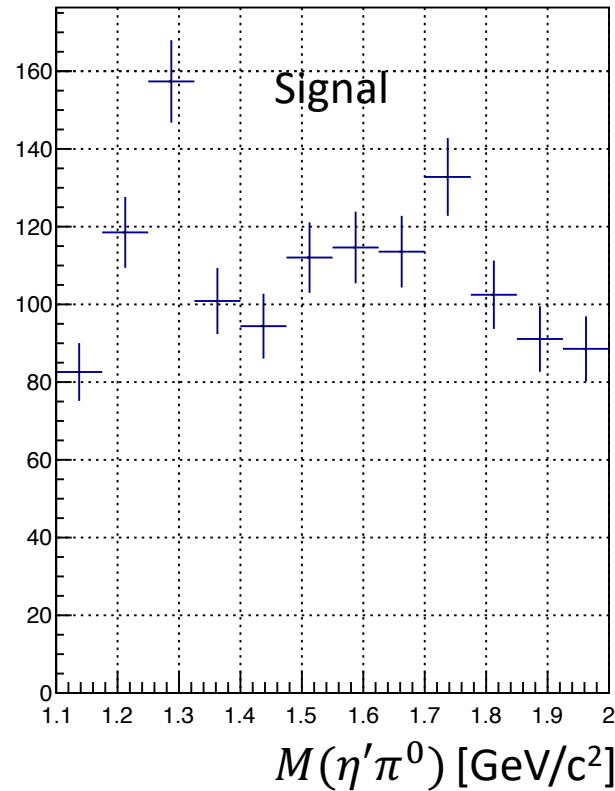
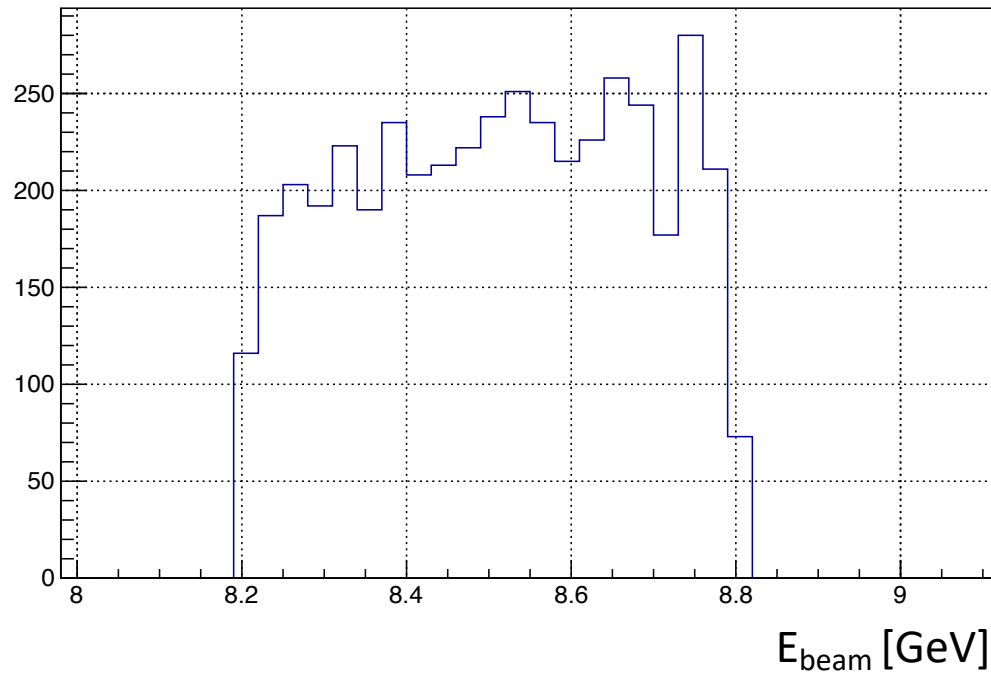
4397 GlueX ($p\eta'\pi^0$) events for 0° polarization

0 Deg.
 $P_\gamma = 0.3519$

Signal-Background separation using Probabilistic Weighing Method

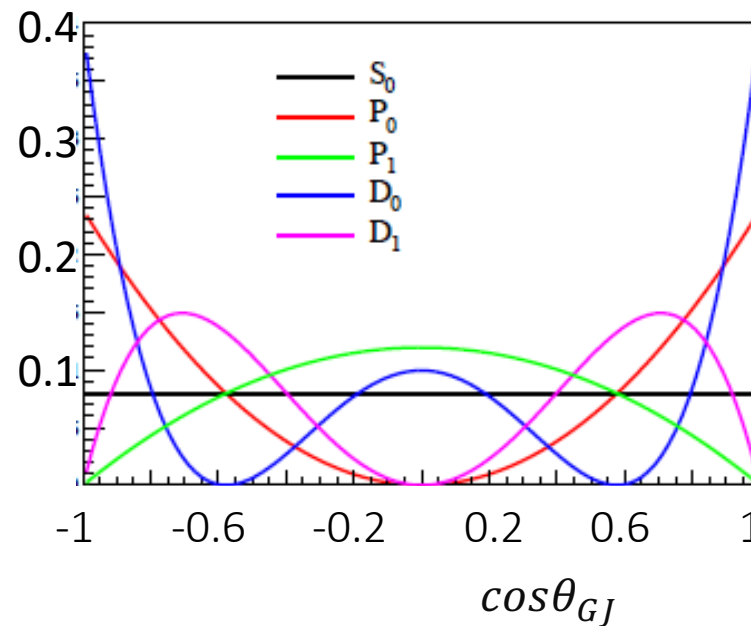
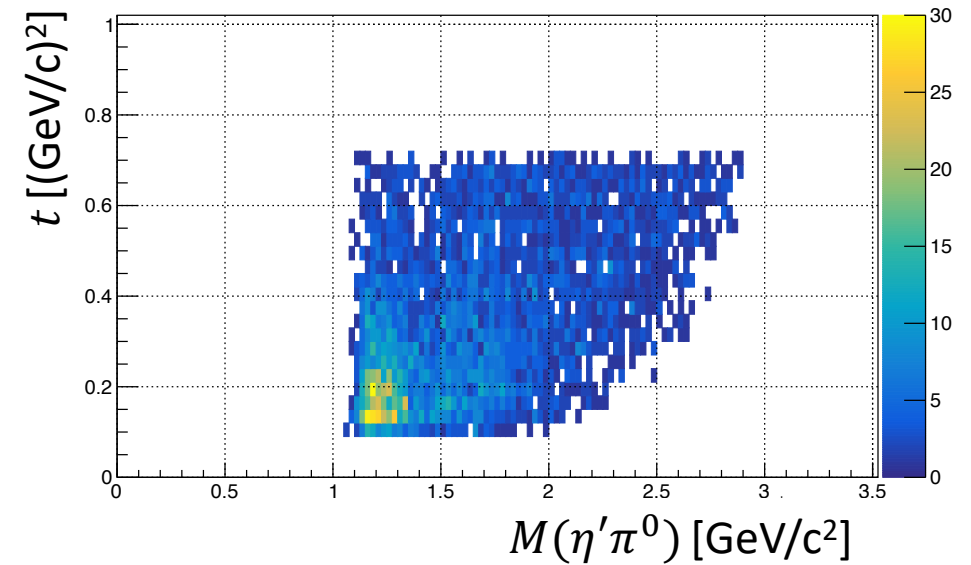
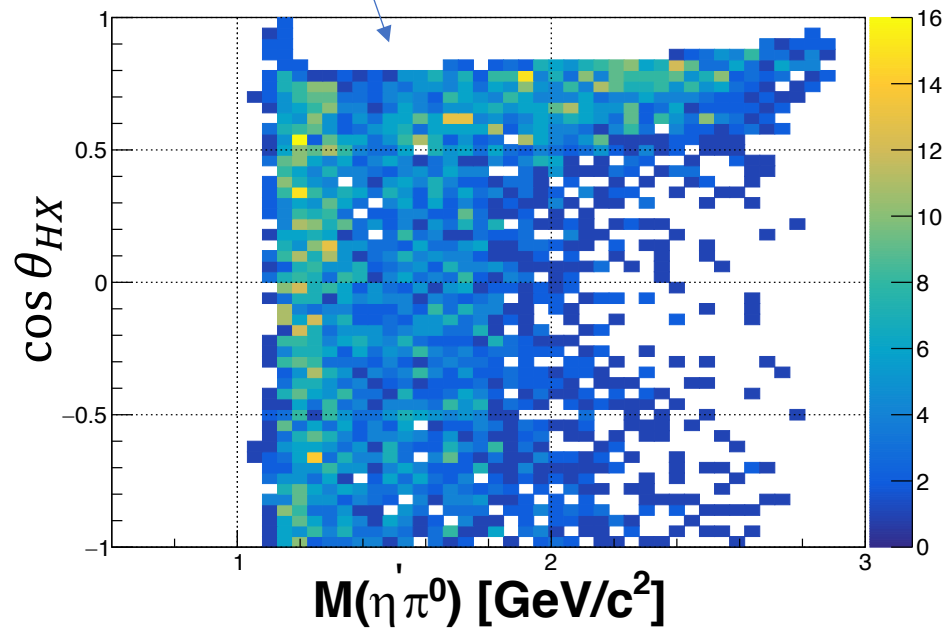
Reaction $\gamma p \rightarrow p\eta'\pi^0$

$\eta' \rightarrow \pi^+\pi^-\eta$, $\eta \rightarrow \gamma\gamma$



4397 GlueX ($p\eta'\pi^0$) events for 0^0 polarization

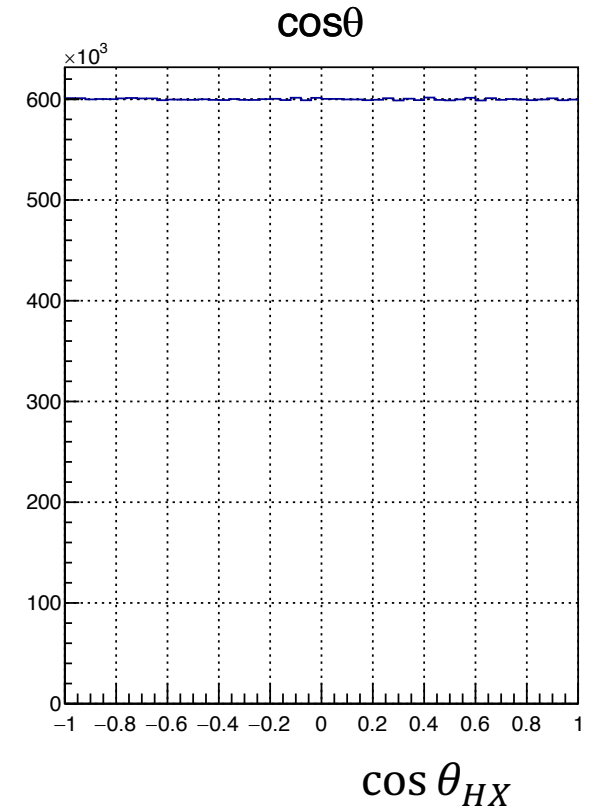
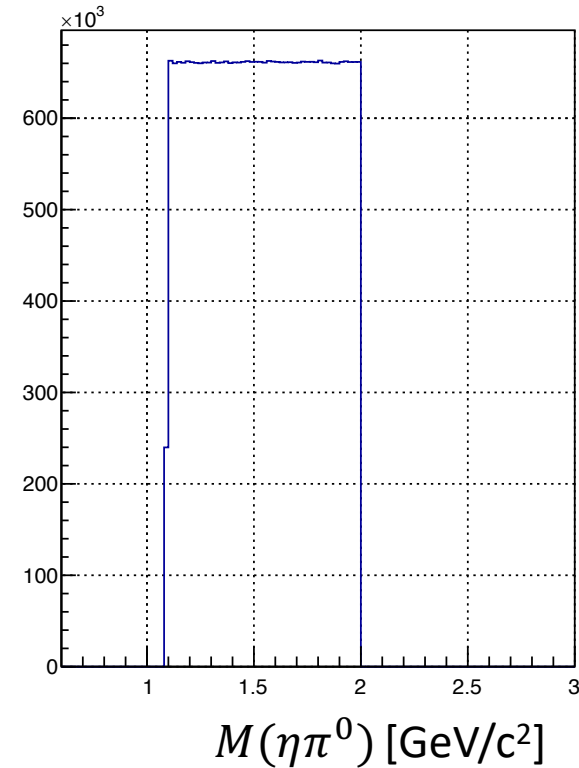
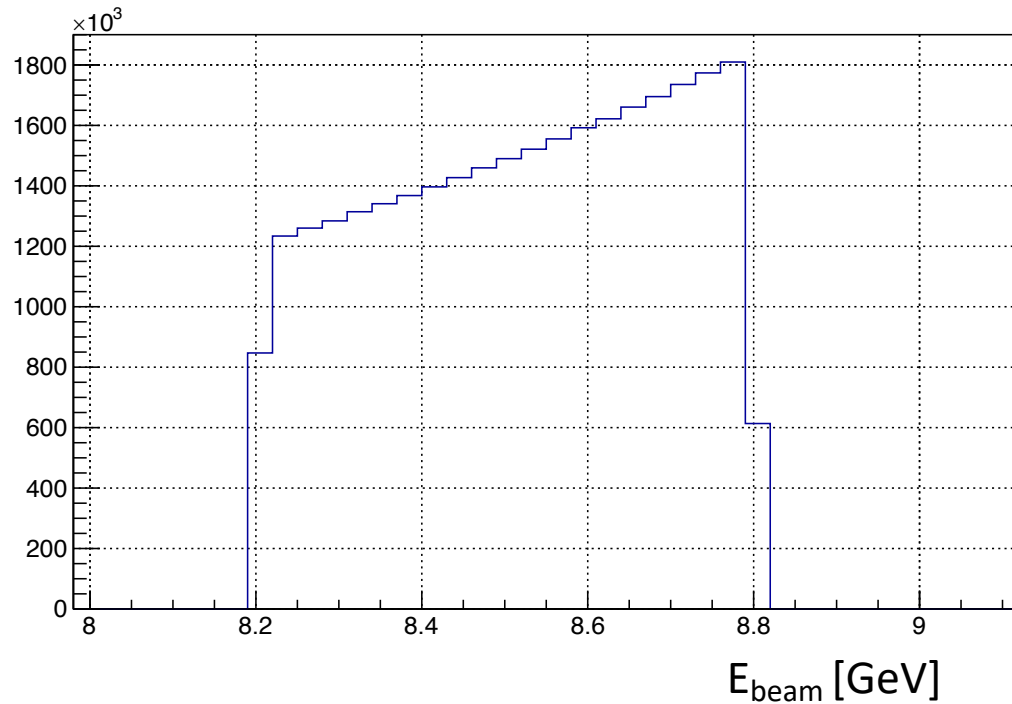
Δ^+ rejection ($0.0 \text{ GeV}/c^2 < M_{\pi^0 p} < 1.4 \text{ GeV}/c^2$)



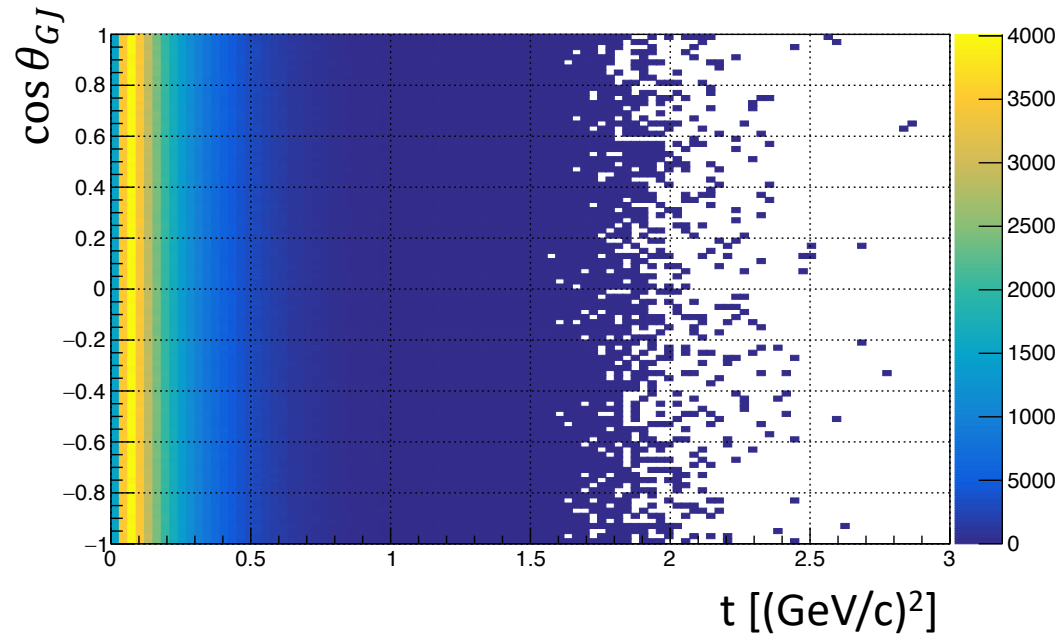
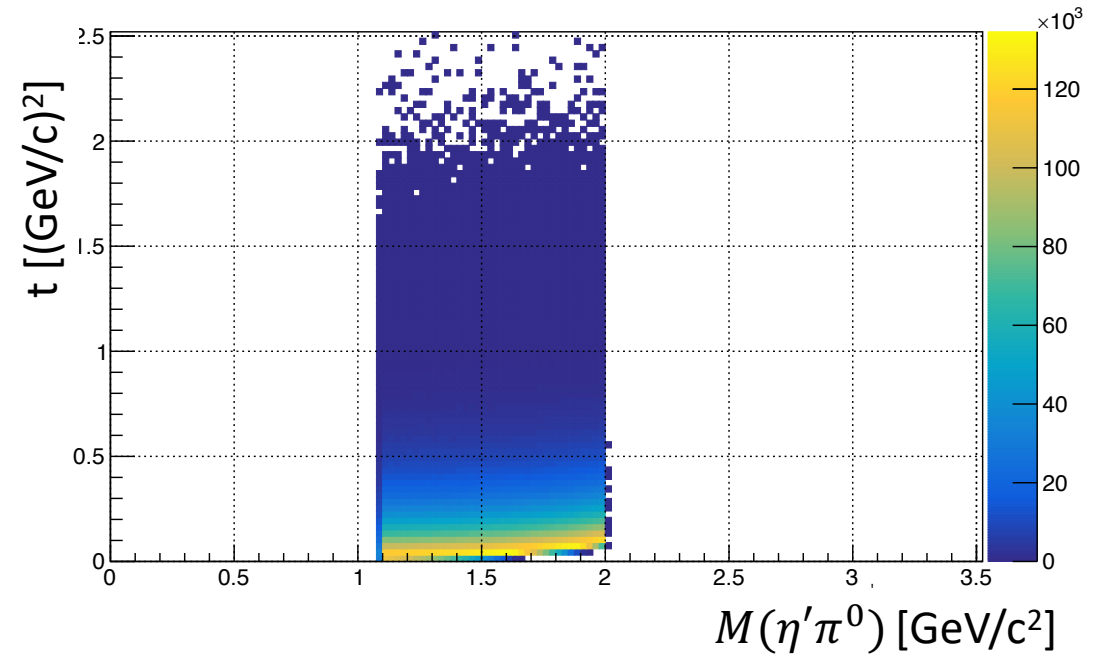
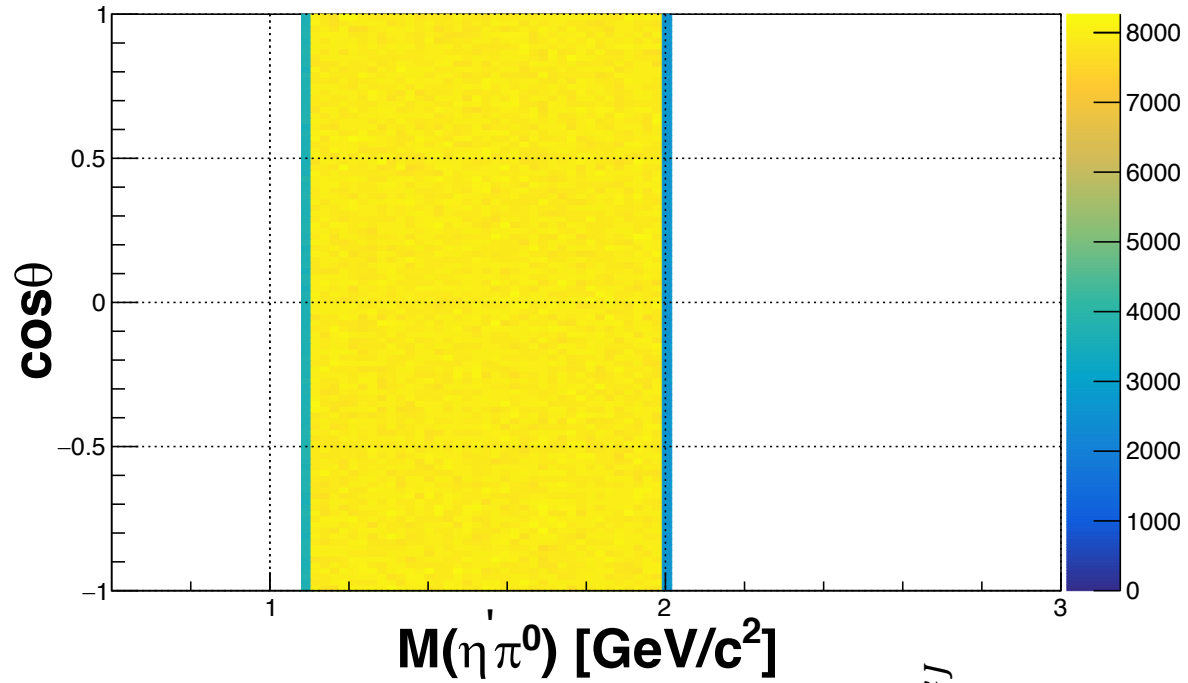
Fit in M and t bins
1.1-2 GeV/c^2 12 bins
0.1-0.7 $(\text{GeV}/c)^2$ 1 bin

Generated $30 \cdot 10^6$ ($p\eta'\pi^0$) **flat** events with AmpTools

- Flat in $\cos \theta_{GJ}$
- Flat in $M(\eta\pi^0)$



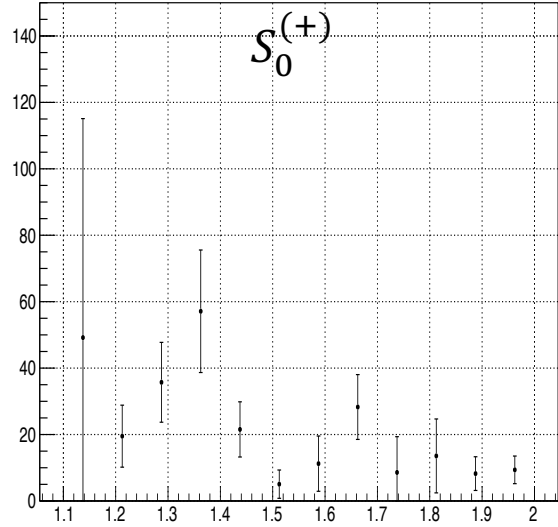
Generated $30 \cdot 10^6$ ($p\eta'\pi^0$) **flat** events with AmpTools



Fit with $S_0, P_{0,1}, D_{0,1,2}$ $\varepsilon=+1$

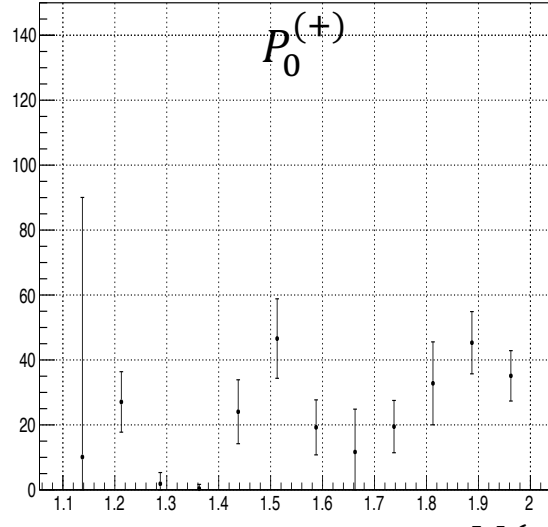
S0pl

$S_0^{(+)}$



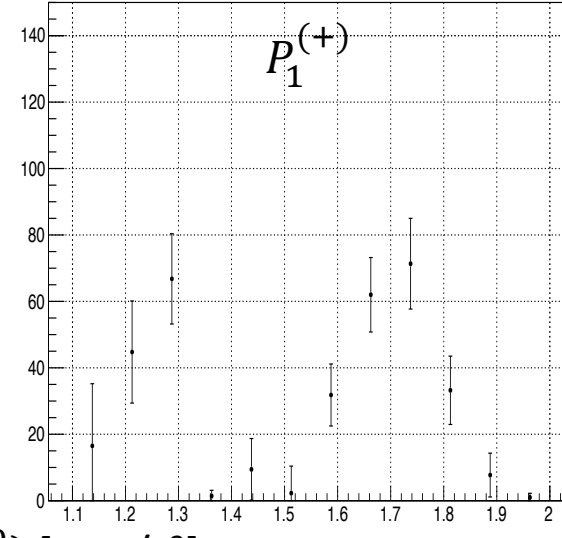
P0pl

$P_0^{(+)}$



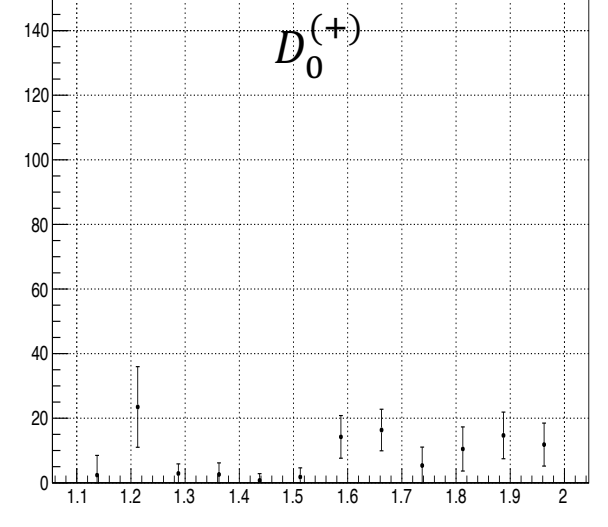
P1pl

$P_1^{(+)}$



D0pl

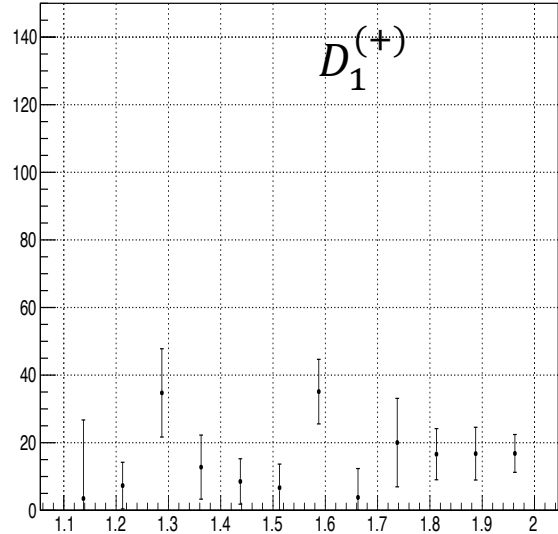
$D_0^{(+)}$



$M(\eta'\pi^0)$ [GeV/c²]

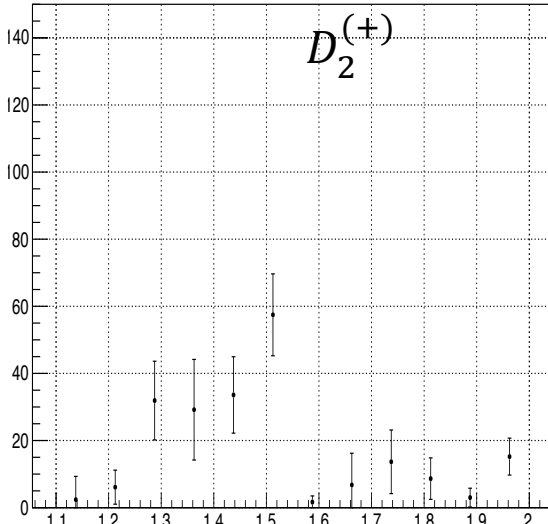
D1pl

$D_1^{(+)}$



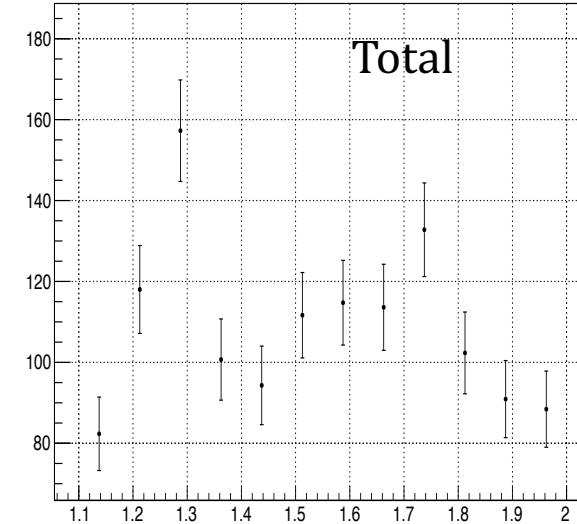
D2pl

$D_2^{(+)}$



All waves

Total

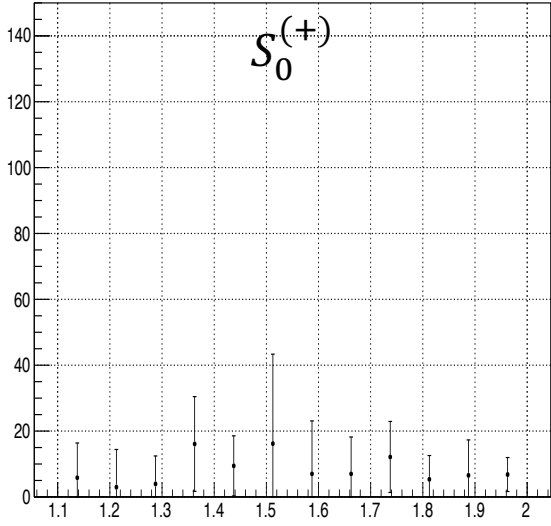


$M(\eta'\pi^0)$ [GeV/c²]

Fit with $S_0, P_{0,1}, D_{0,1,2}$ $\epsilon=\pm 1$

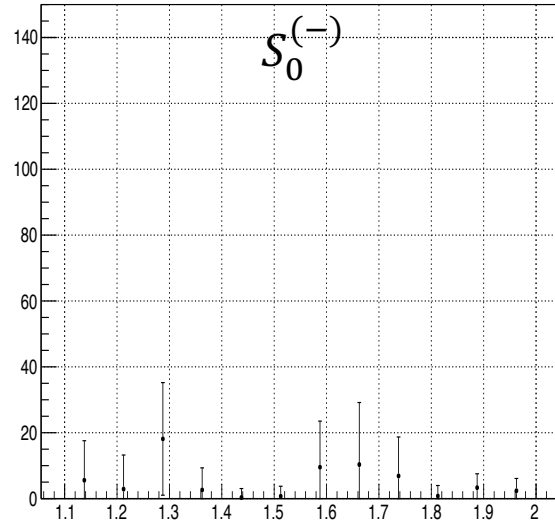
S0pl

$S_0^{(+)}$



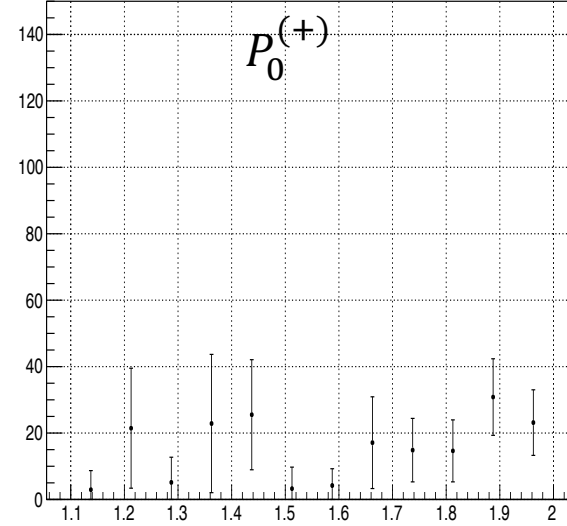
S0mi

$S_0^{(-)}$



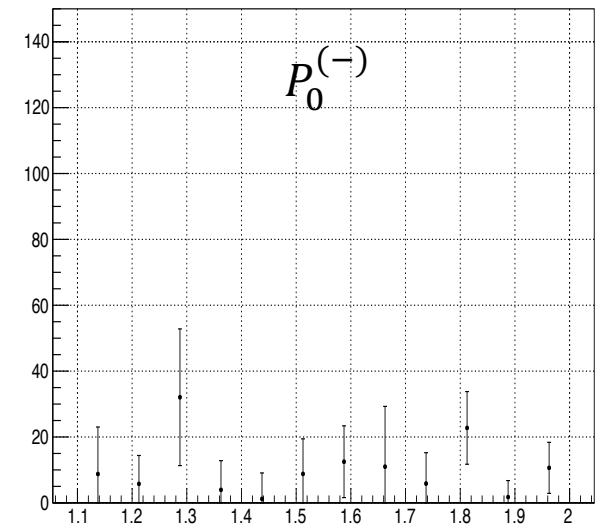
P0pl

$P_0^{(+)}$



P0mi

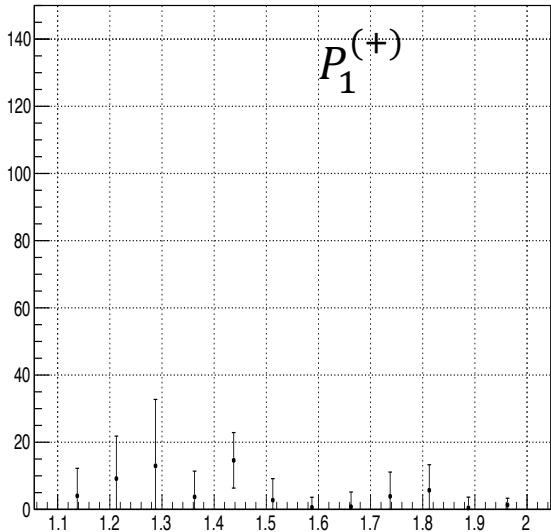
$P_0^{(-)}$



$M(\eta'\pi^0)$ [GeV/c²]

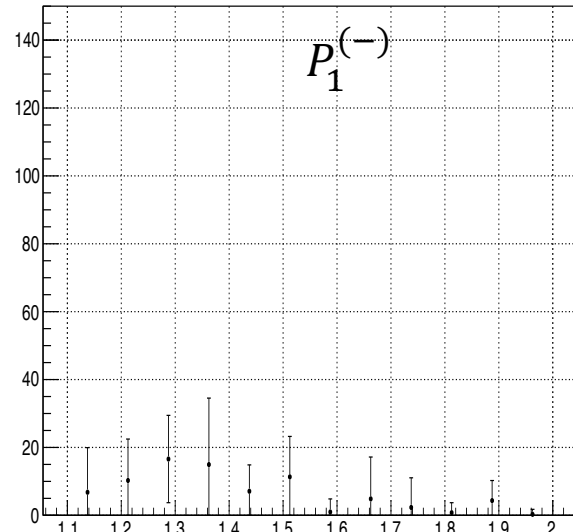
P1pl

$P_1^{(+)}$



P1mi

$P_1^{(-)}$

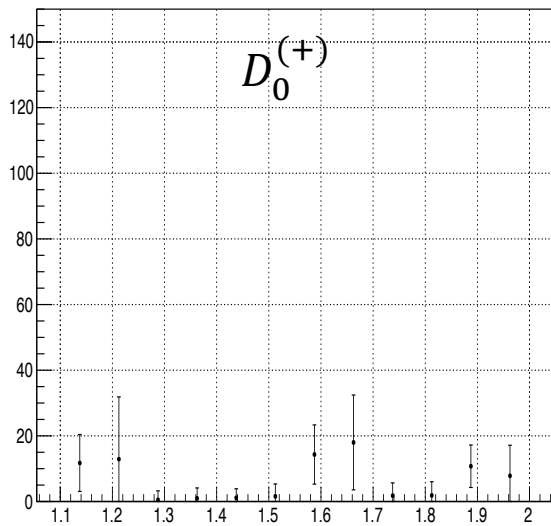


$M(\eta'\pi^0)$ [GeV/c²]

Fit with $S_0, P_0, D_{0,1,2}$ $\epsilon=\pm 1$

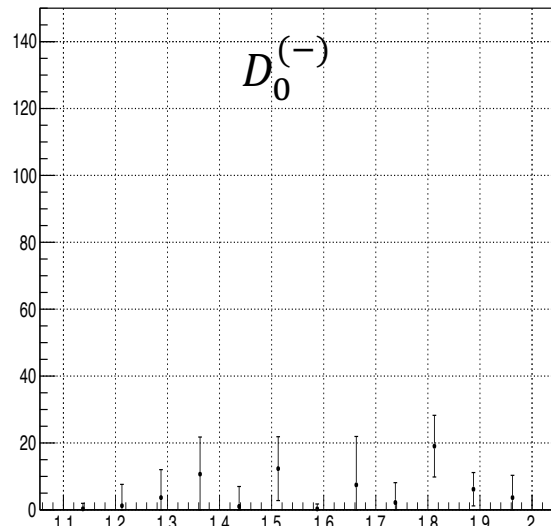
D0pl

$D_0^{(+)}$



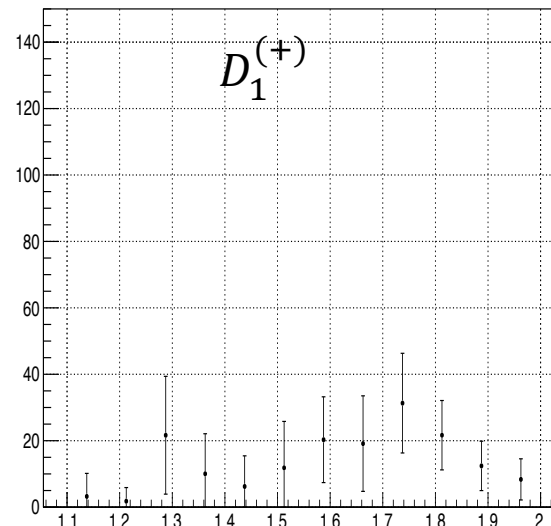
D0mi

$D_0^{(-)}$



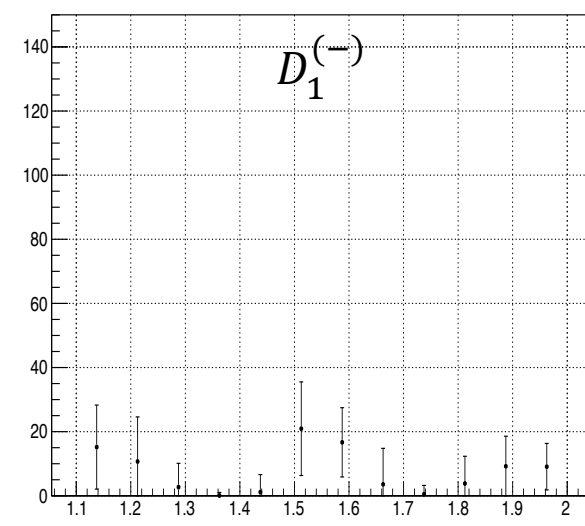
D1pl

$D_1^{(+)}$



D1mi

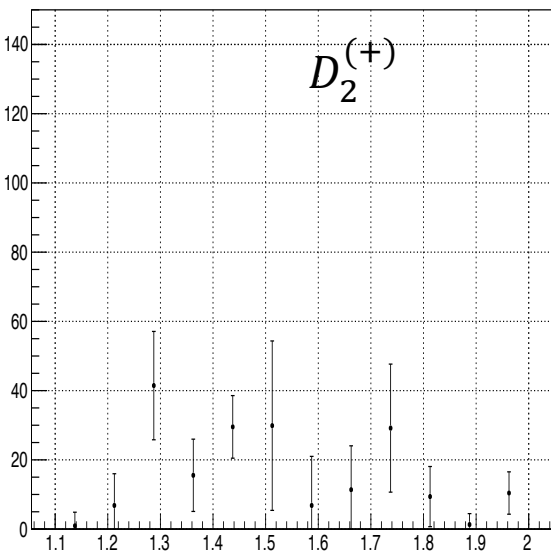
$D_1^{(-)}$



$M(\eta'\pi^0)$ [GeV/c²]

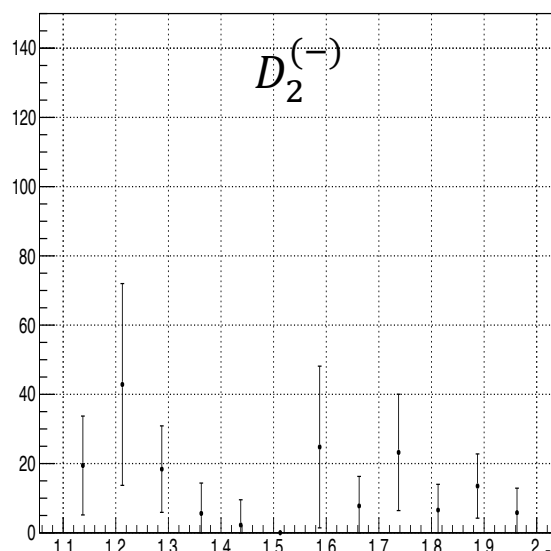
D2pl

$D_2^{(+)}$



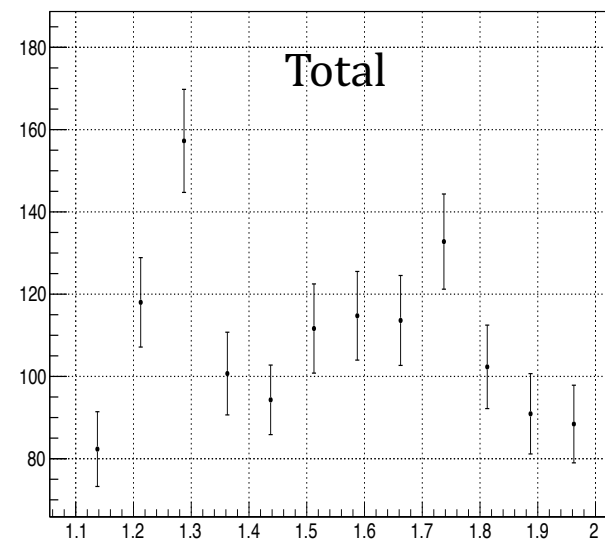
D2mi

$D_2^{(-)}$



All waves

Total



$M(\eta'\pi^0)$ [GeV/c²]

1. Fitting entire GlueX phase 1 data (except fall 2018) for four γ polarization plane angles relative to horizontal (0, 45, 90, 135 $^\circ$) + amorphous data using loop statement in AmpTools
2. Fit intensity with different wave sets:
 - $S_0, P_{0,1}, D_{0,1,2}$ $\epsilon=+1$
 - $S_0, P_{0,1}, D_{0,1,2}$ $\epsilon=\pm 1$
 - $S_0, P_{0,\pm 1}, D_{0,\pm 1,\pm 2}$ $\epsilon=\pm 1$
3. Invariant mass bin size of 75 MeV/c 2 , momentum transfer bin size of 0.6 (GeV/c) 2

Plot acceptance uncorrected results

18482 GlueX ($p\eta'\pi^0$) events for 4 γ polarization plane angles relative to horizontal (0, 45, 90, 135°) + amorphous data

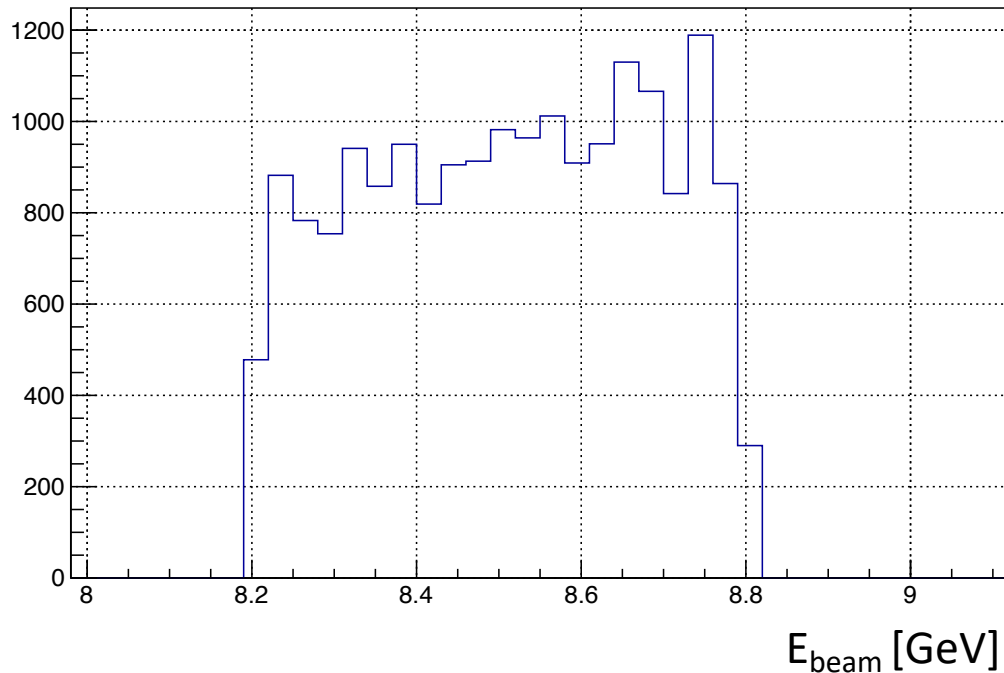
0 Deg. $P_\gamma = 0.3519$

45 Deg. $P_\gamma = 0.3374$

90 Deg. $P_\gamma = 0.3303$

135 Deg. $P_\gamma = 0.3375$

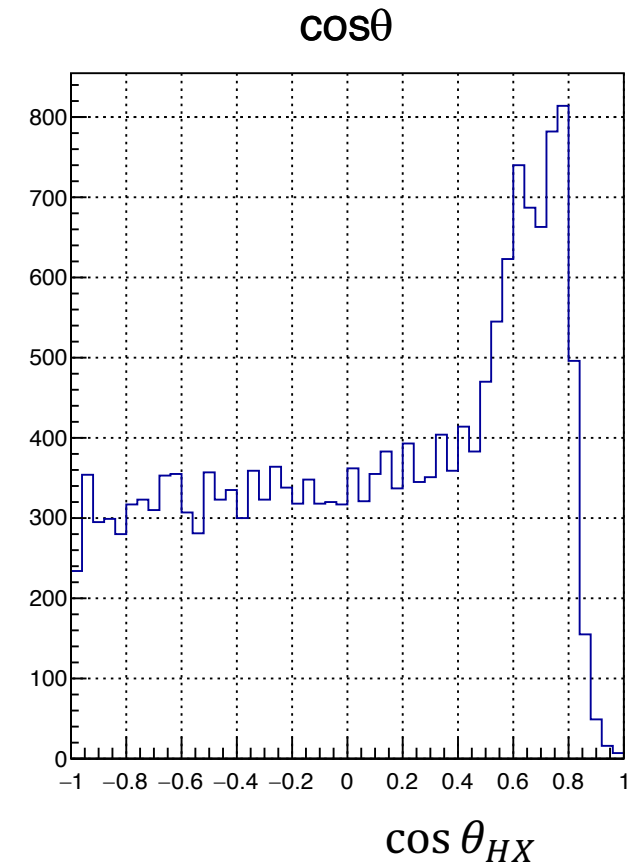
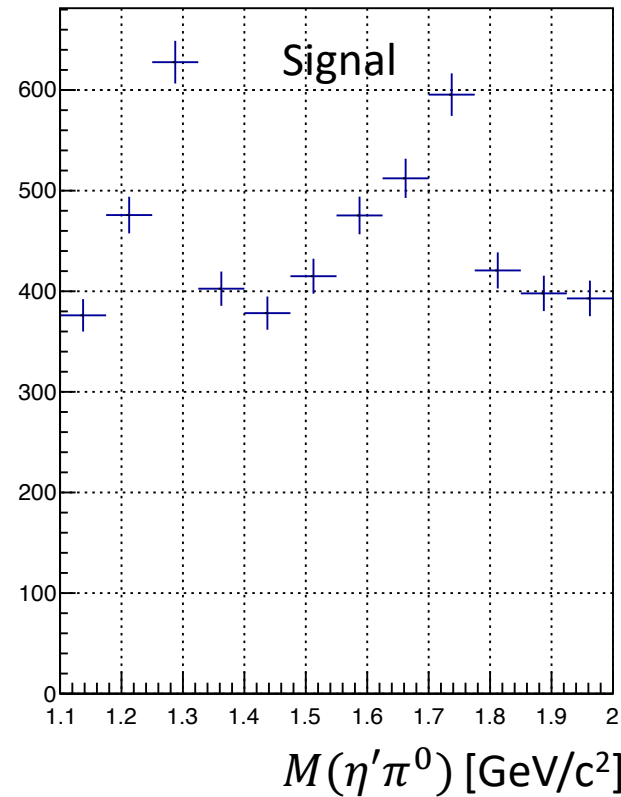
Amorphous $P_\gamma = 0.00001$



Signal-Background separation using Probabilistic Weighing Method

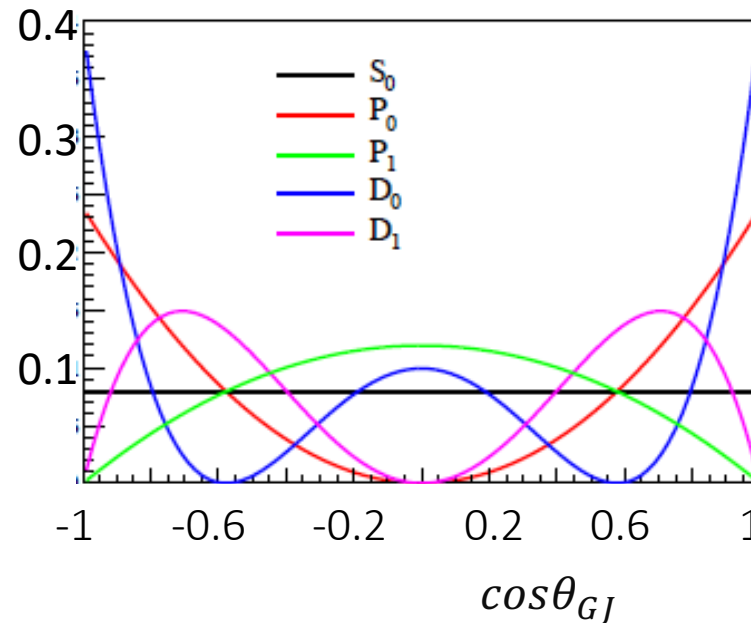
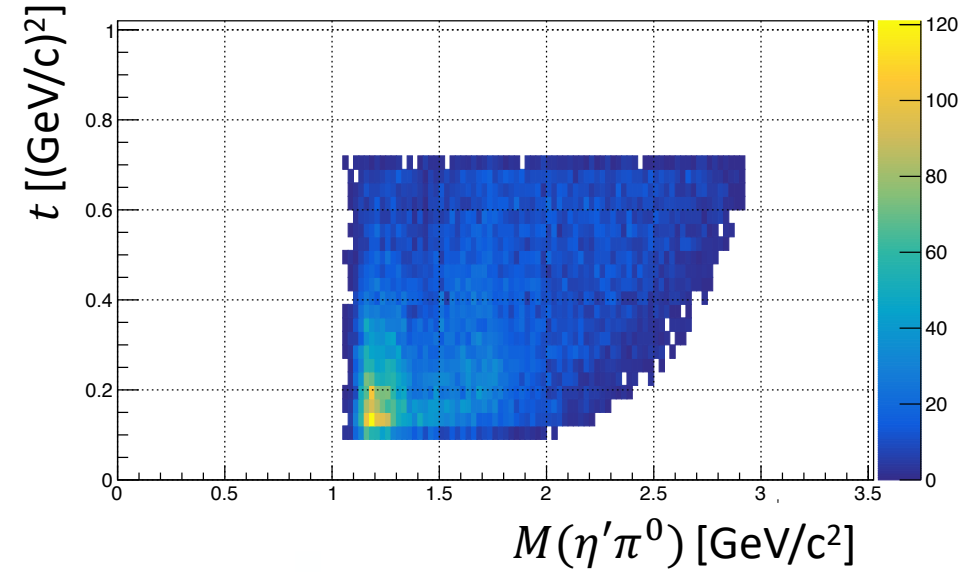
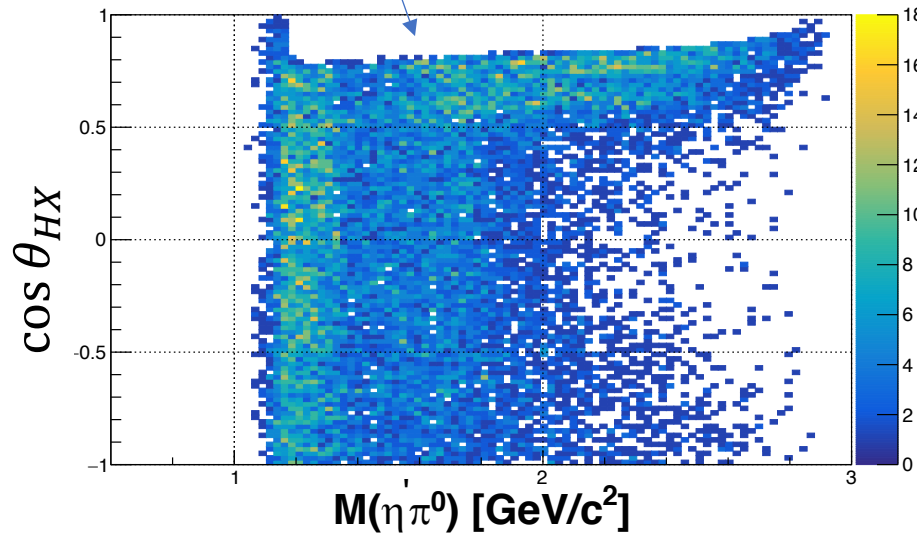
Reaction $\gamma p \rightarrow p\eta'\pi^0$

$\eta' \rightarrow \pi^+\pi^-\eta$, $\eta \rightarrow \gamma\gamma$



18482 GlueX ($p\eta'\pi^0$) events for 4 γ polarization plane angles relative to horizontal (0, 45, 90, 135°) + amorphous data

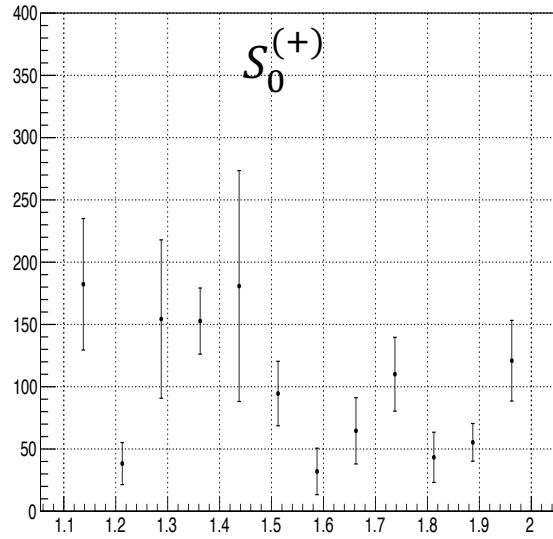
Δ^+ rejection ($0.0 \text{ GeV}/c^2 < M_{\pi^0 p} < 1.4 \text{ GeV}/c^2$)



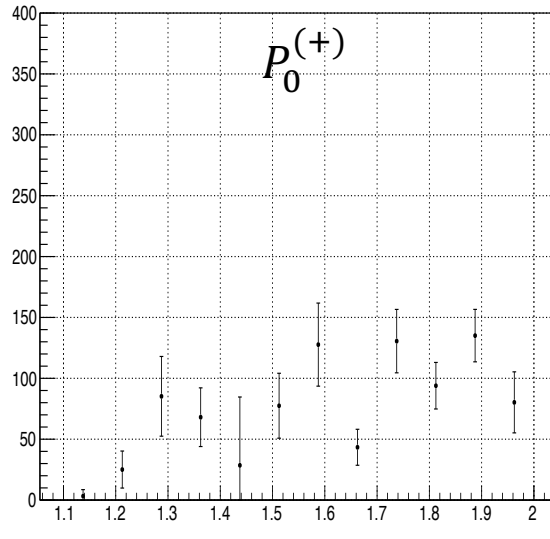
Fit in M and t bins
 $1.1\text{-}2 \text{ GeV}/c^2$ 12 bins
 $0.1\text{-}0.7 (\text{GeV}/c)^2$ 1 bin

Fit with $S_0, P_0, D_0, P_1, D_1, D_2$ $\epsilon=+1$

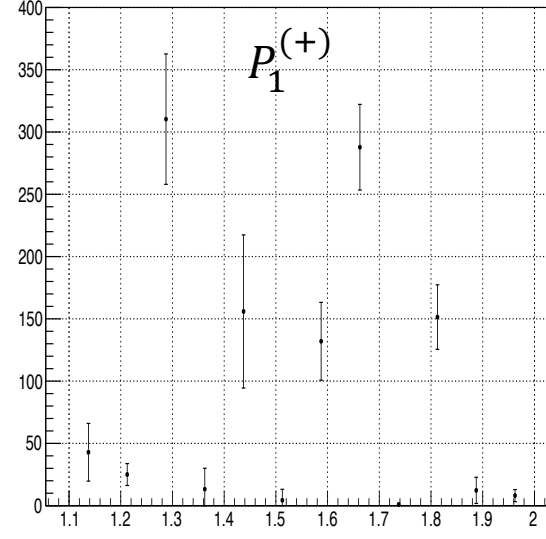
S0pl



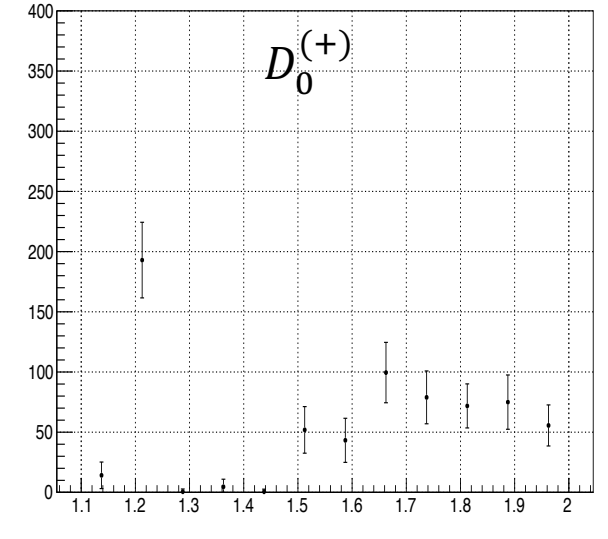
P0pl



P1pl

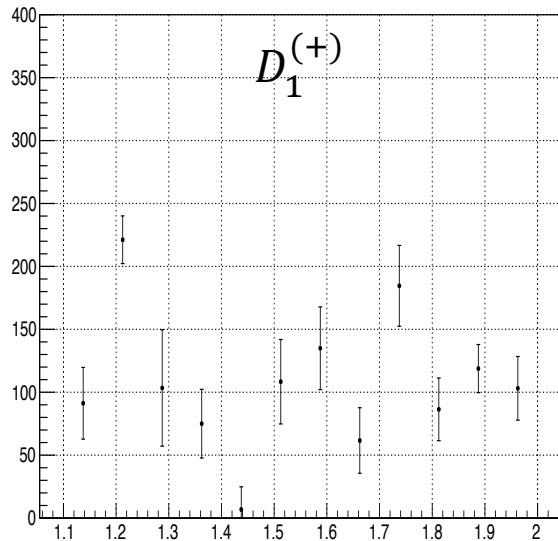


D0pl

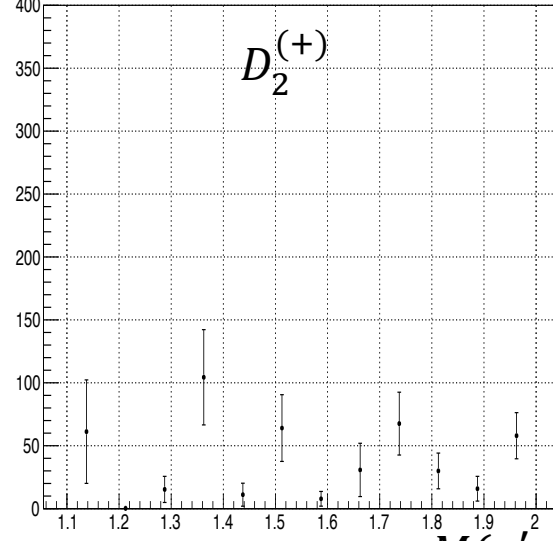


$M(\eta'\pi^0) [\text{GeV}/c^2]$

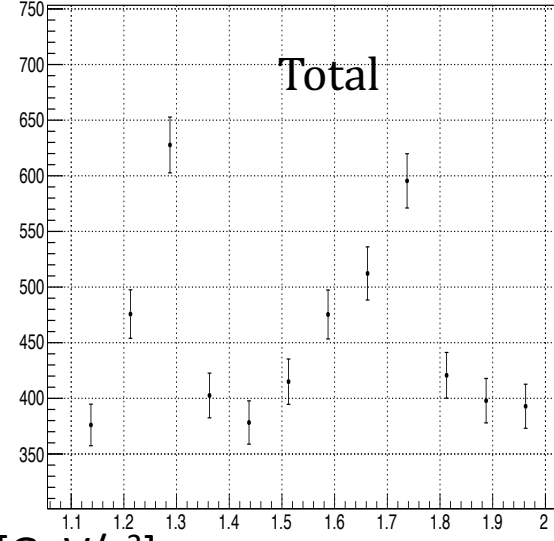
D1pl



D2pl



All waves

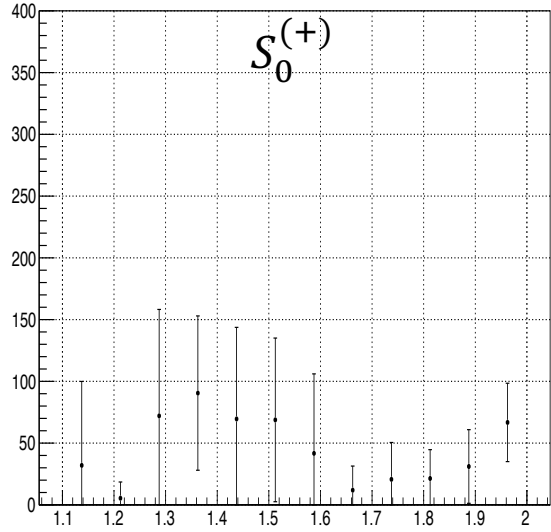


$M(\eta'\pi^0) [\text{GeV}/c^2]$

Fit with $S_0, P_{0,1}, D_{0,1,2}$ $\epsilon=\pm 1$

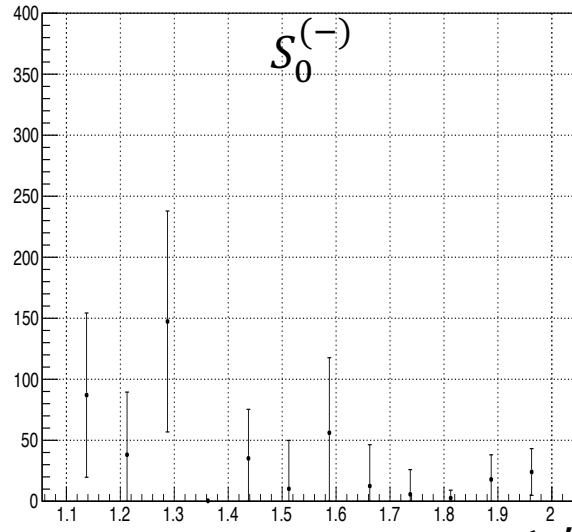
S0pl

$S_0^{(+)}$



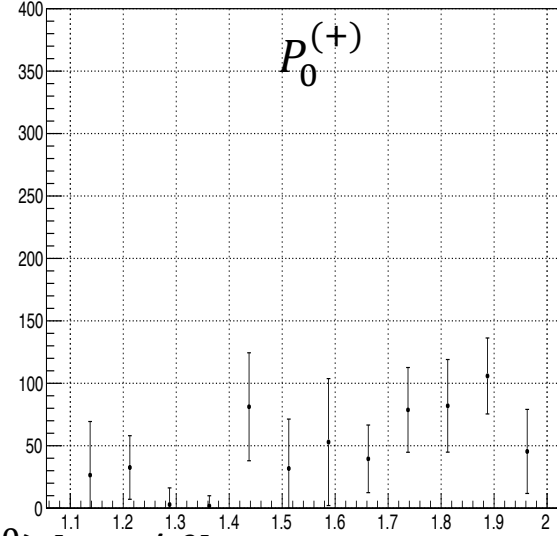
S0mi

$S_0^{(-)}$



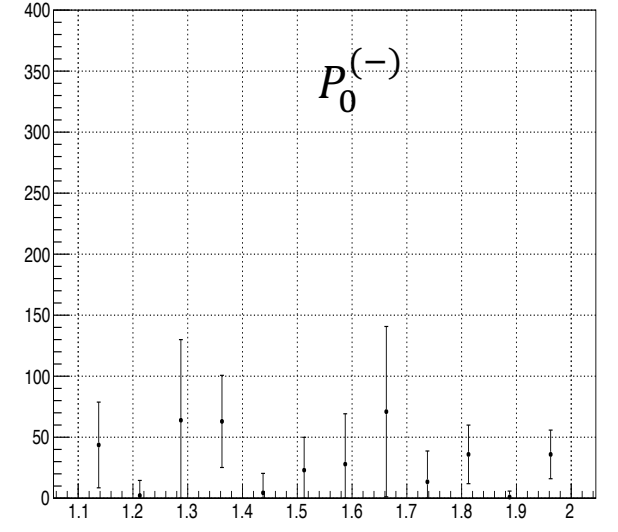
P0pl

$P_0^{(+)}$



P0mi

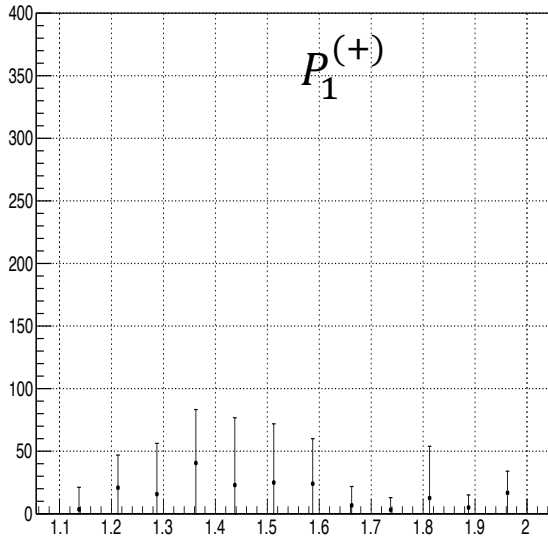
$P_0^{(-)}$



$M(\eta'\pi^0)$ [GeV/c²]

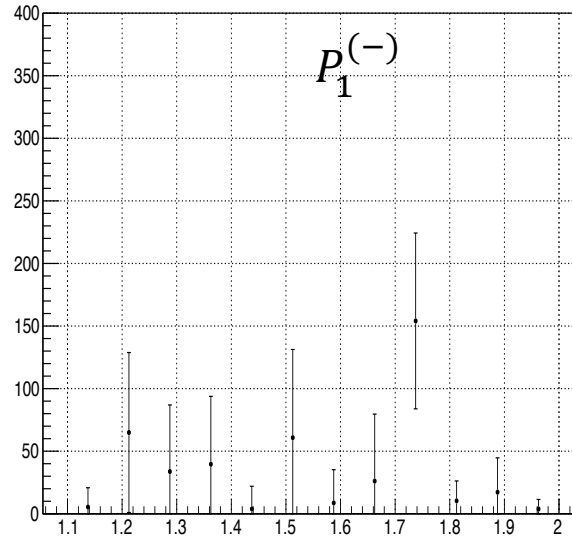
P1pl

$P_1^{(+)}$



P1mi

$P_1^{(-)}$

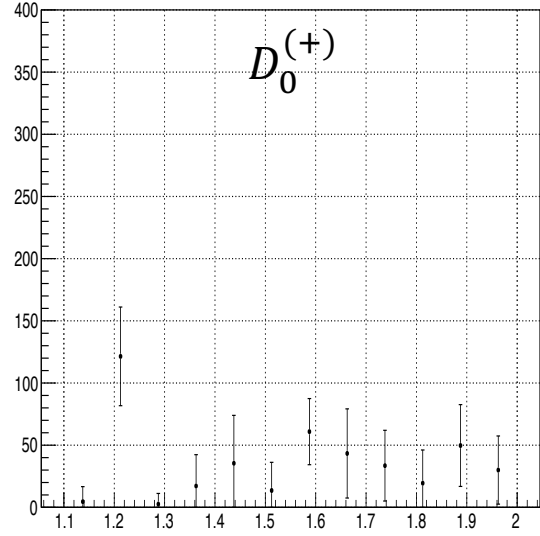


$M(\eta'\pi^0)$ [GeV/c²]

Fit with $S_0, P_0, D_{0,1,2}$ $\varepsilon=\pm 1$

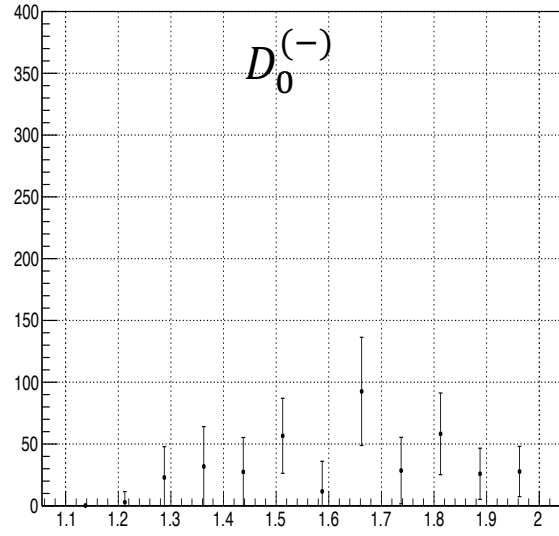
D0pl

$D_0^{(+)}$



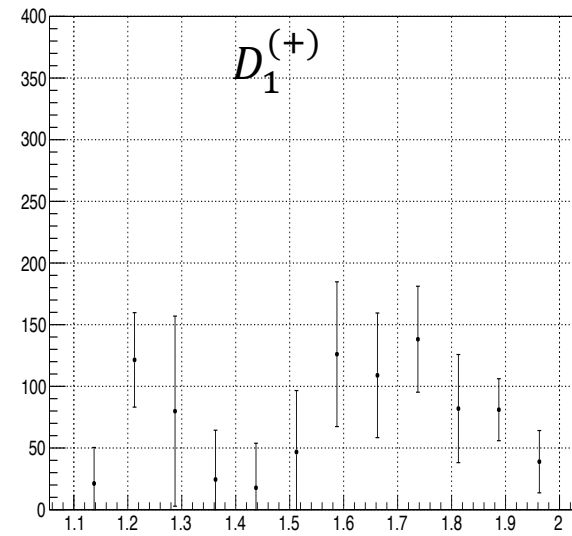
D0mi

$D_0^{(-)}$



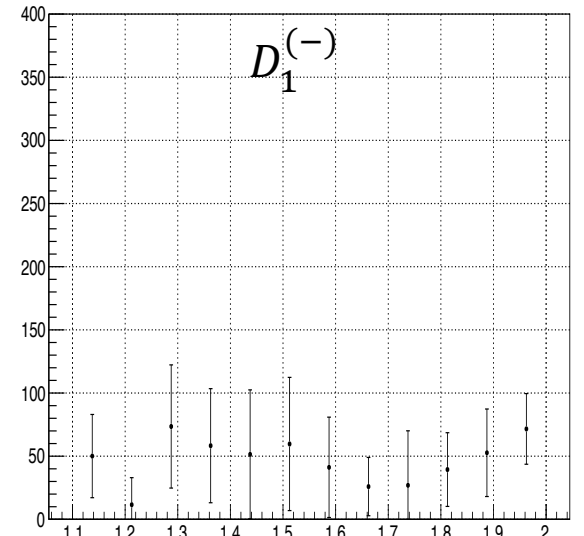
D1pl

$D_1^{(+)}$



D1mi

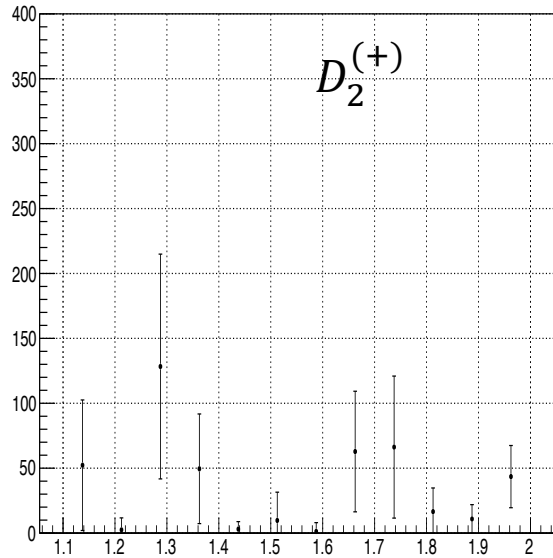
$D_1^{(-)}$



$M(\eta'\pi^0)$ [GeV/c²]

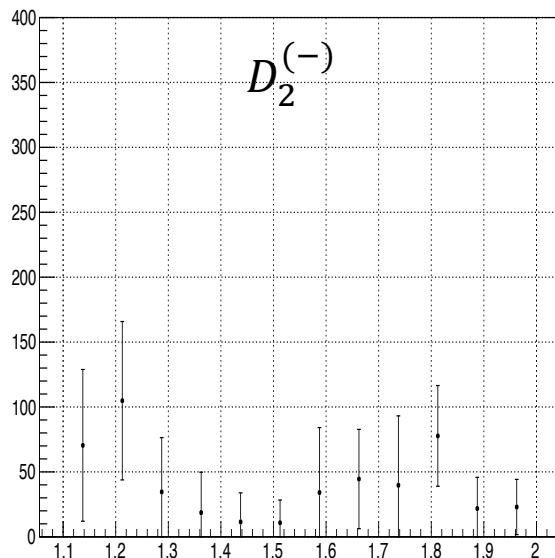
D2pl

$D_2^{(+)}$



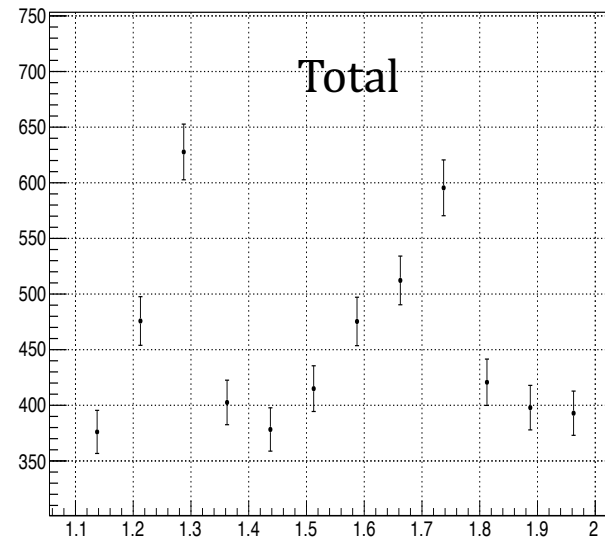
D2mi

$D_2^{(-)}$



All waves

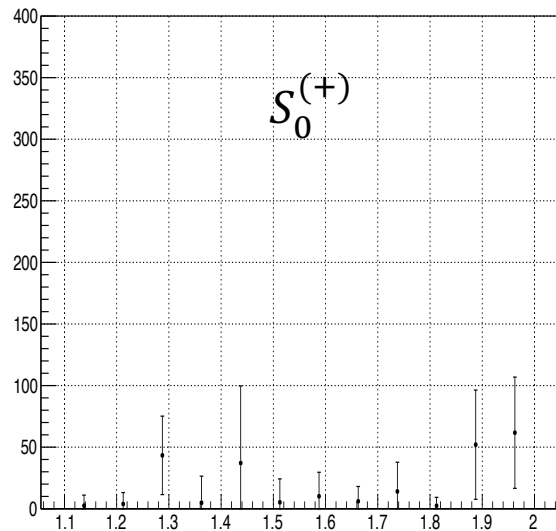
Total



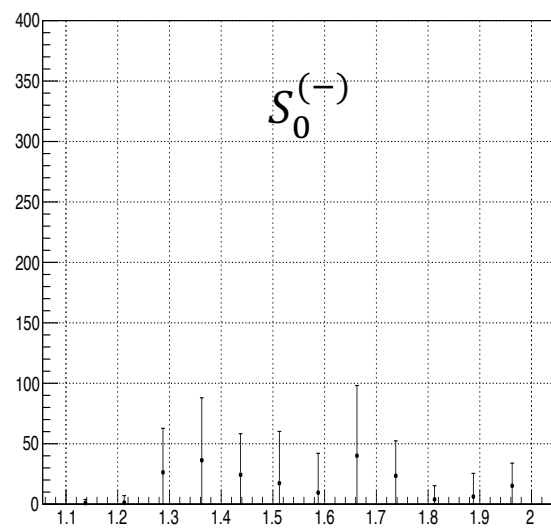
$M(\eta'\pi^0)$ [GeV/c²]

Fit with $S_0, P_{0,\pm 1}, D_{0,\pm 1,\pm 2}$ $\varepsilon = \pm 1$

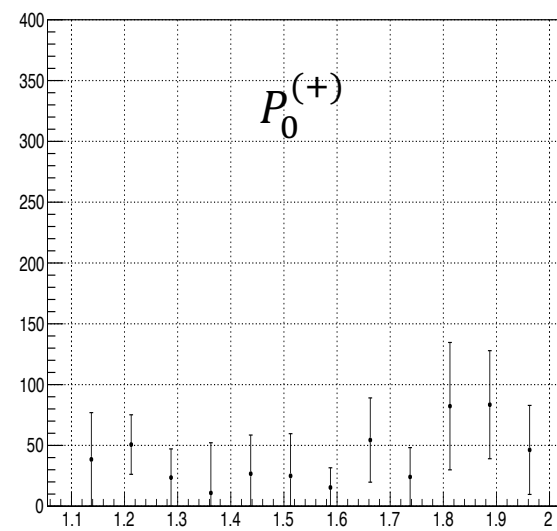
S0pl



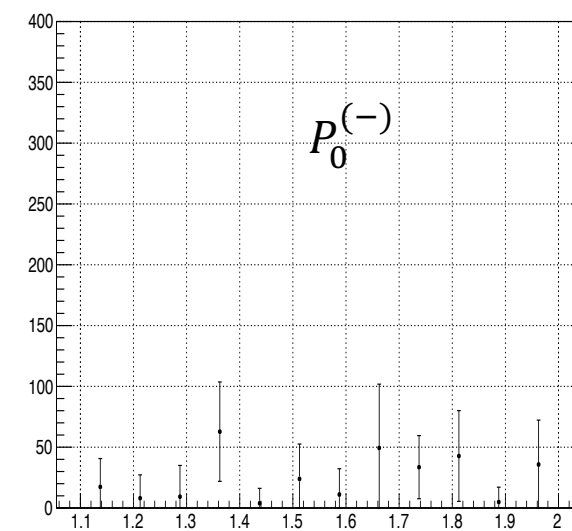
S0mi



P0pl

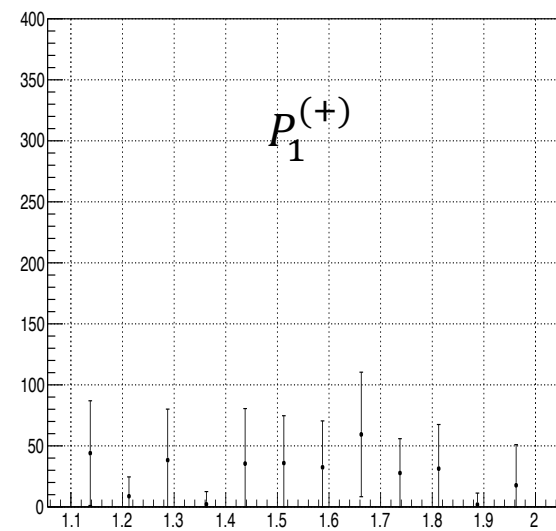


P0mi

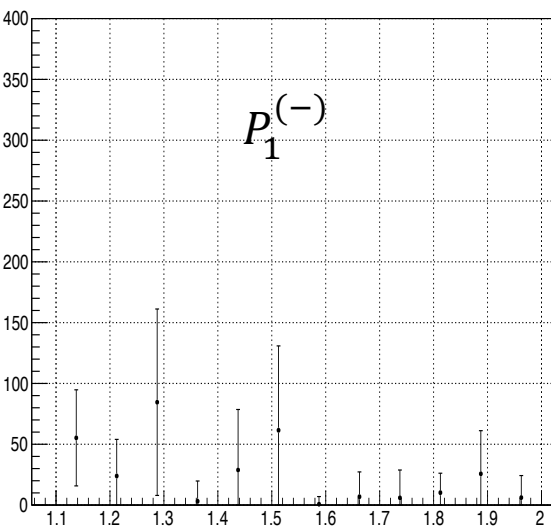


$M(\eta'\pi^0)$ [GeV/c²]

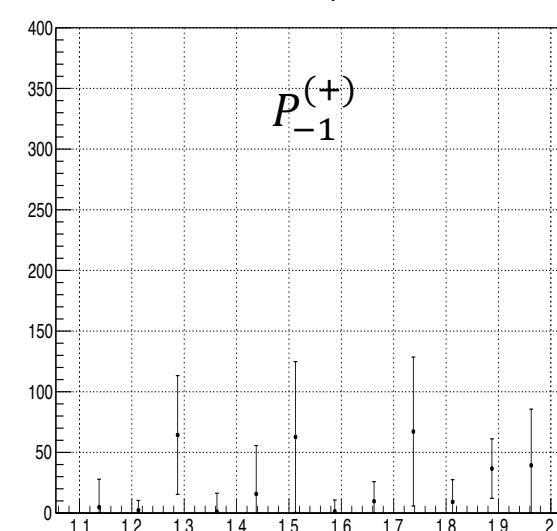
P1pl



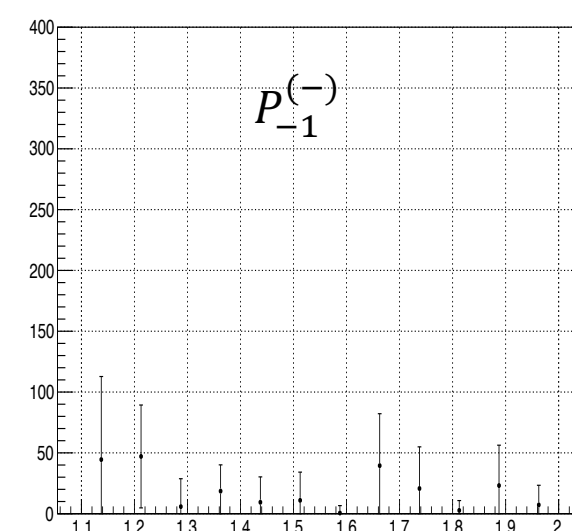
P1mi



Pmi1pl



Pmi1mi

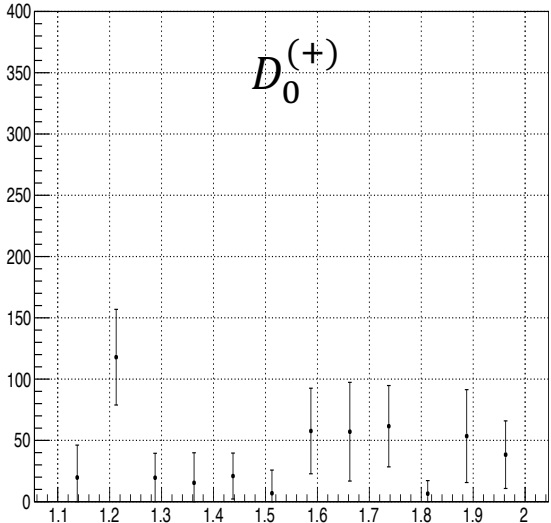


$M(\eta'\pi^0)$ [GeV/c²]

Fit with $S_0, P_{0,\pm 1}, D_{0,\pm 1,\pm 2} \ \varepsilon=\pm 1$

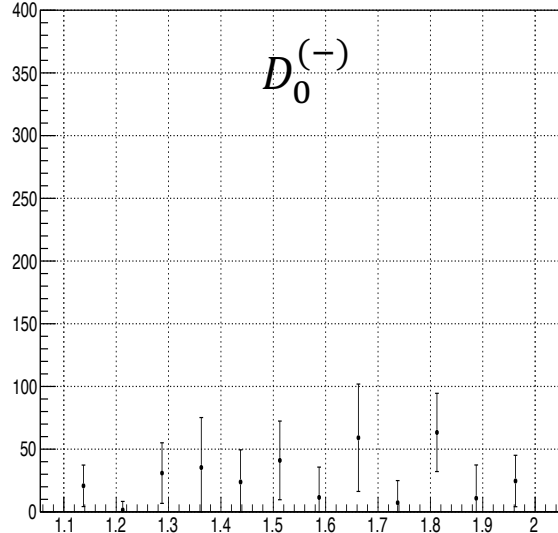
D0pl

$D_0^{(+)}$



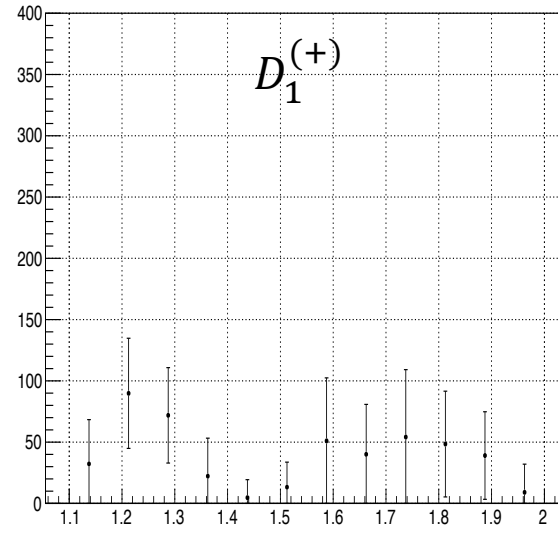
D0mi

$D_0^{(-)}$



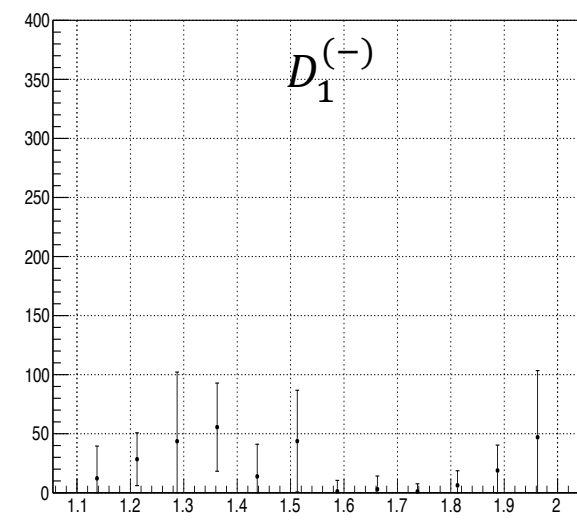
D1pl

$D_1^{(+)}$



D1mi

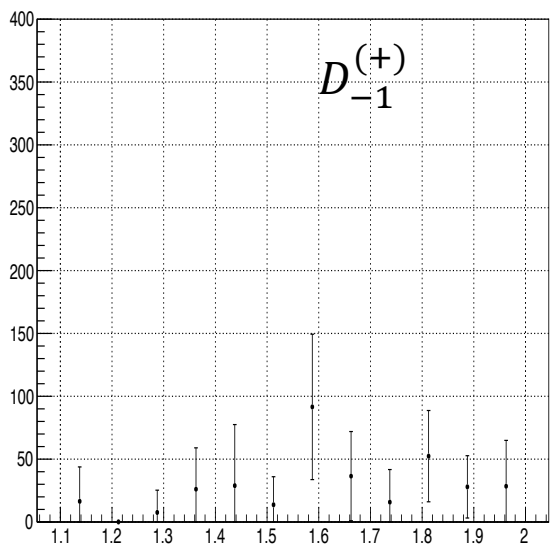
$D_1^{(-)}$



$M(\eta'\pi^0)$ [GeV/c²]

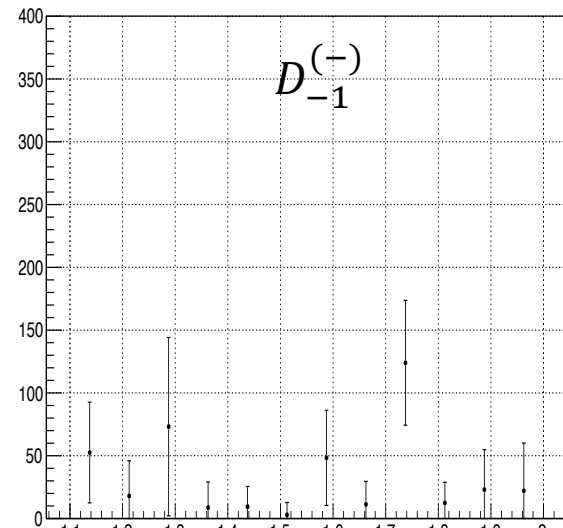
Dmi1pl

$D_{-1}^{(+)}$



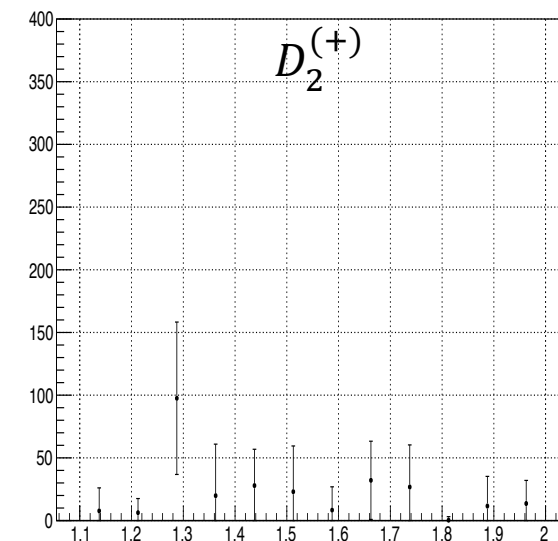
Dmi1mi

$D_{-1}^{(-)}$



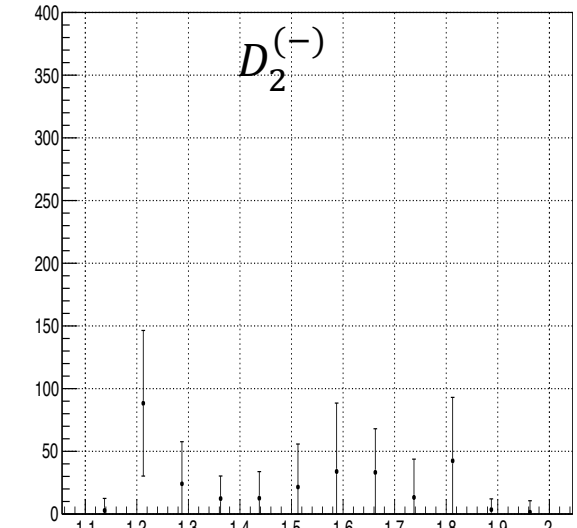
D2pl

$D_2^{(+)}$



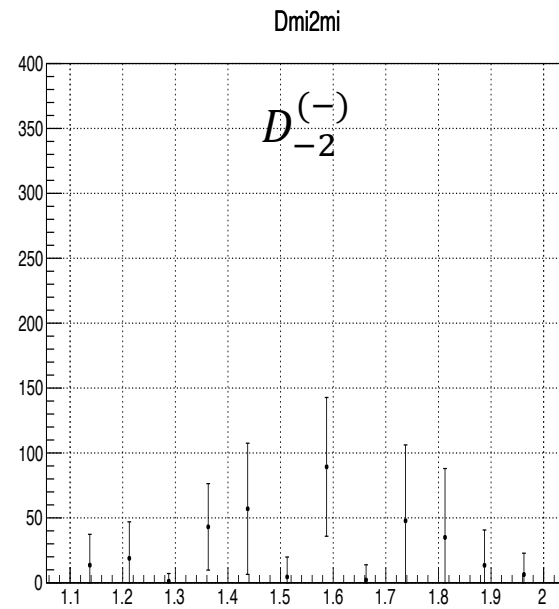
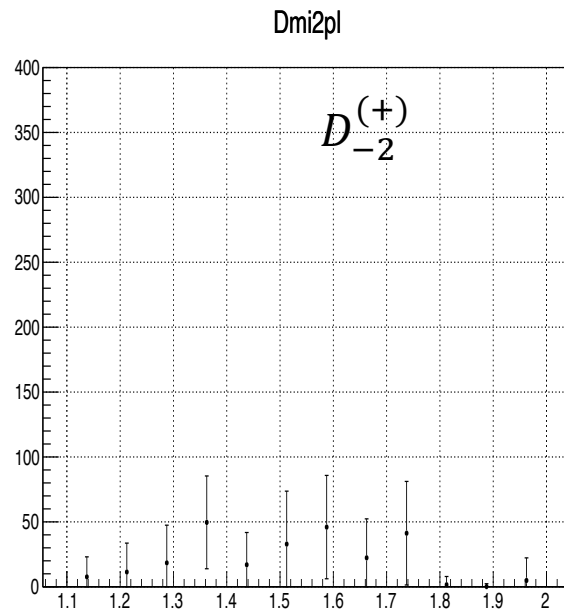
D2mi

$D_2^{(-)}$

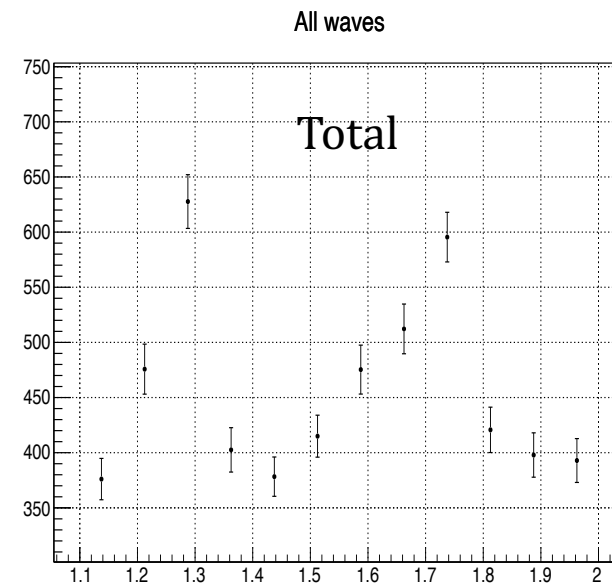


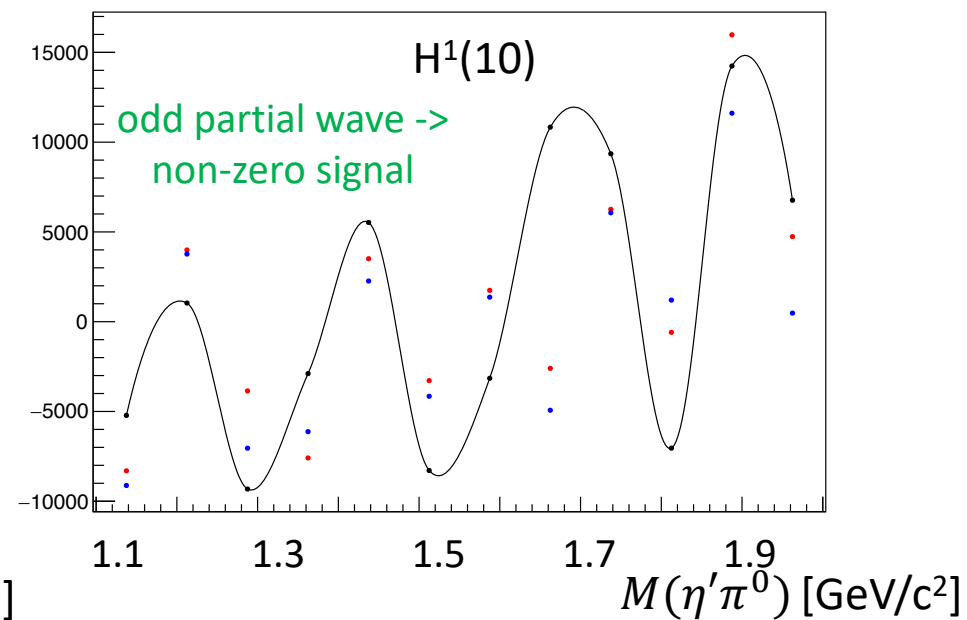
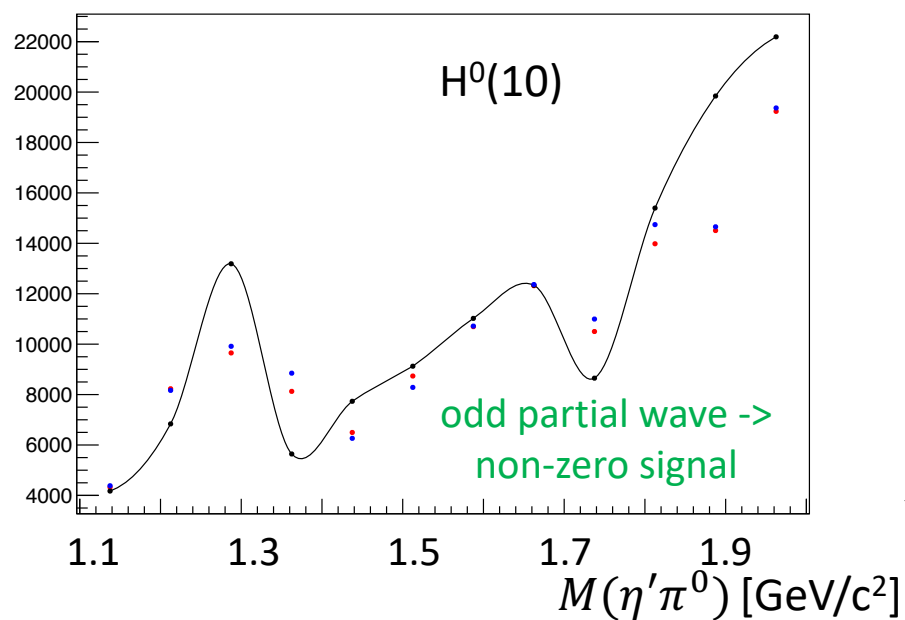
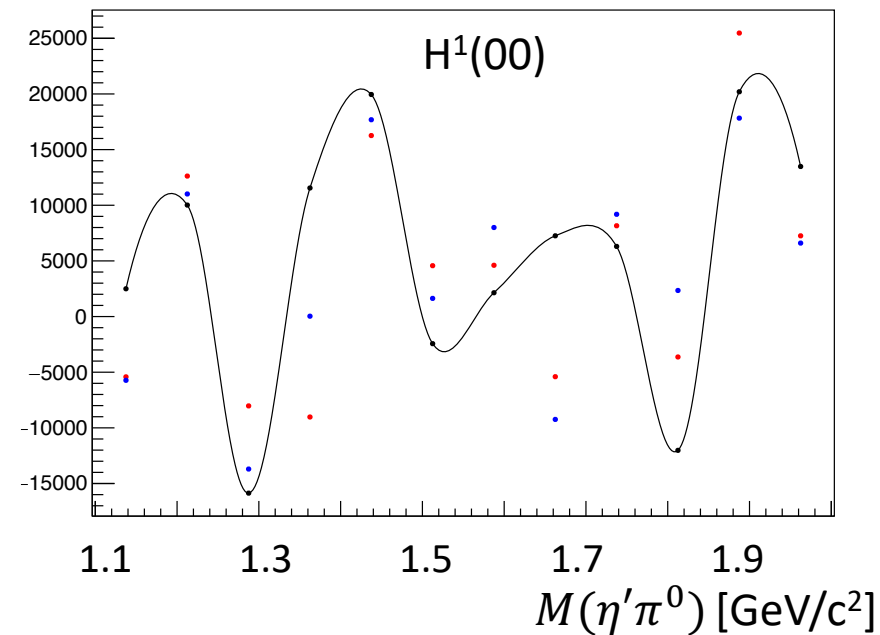
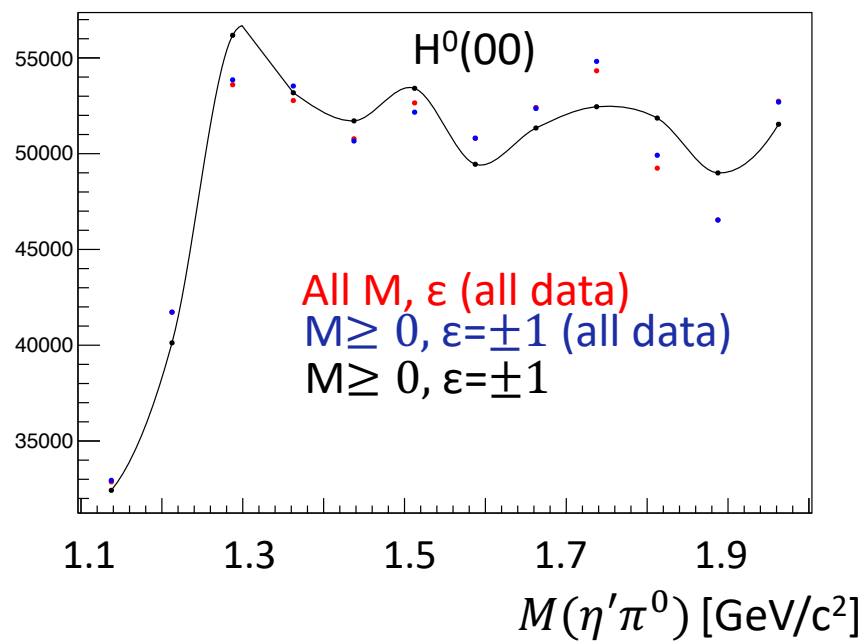
$M(\eta'\pi^0)$ [GeV/c²]

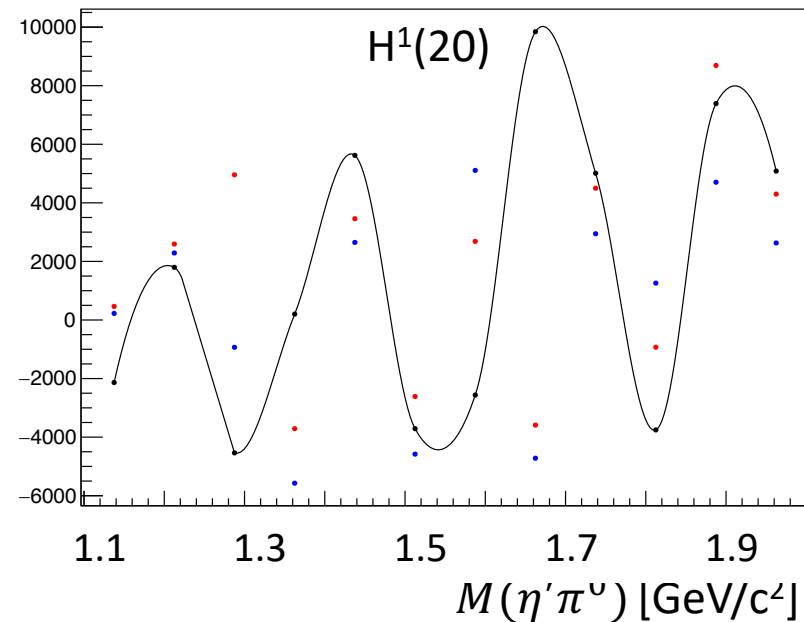
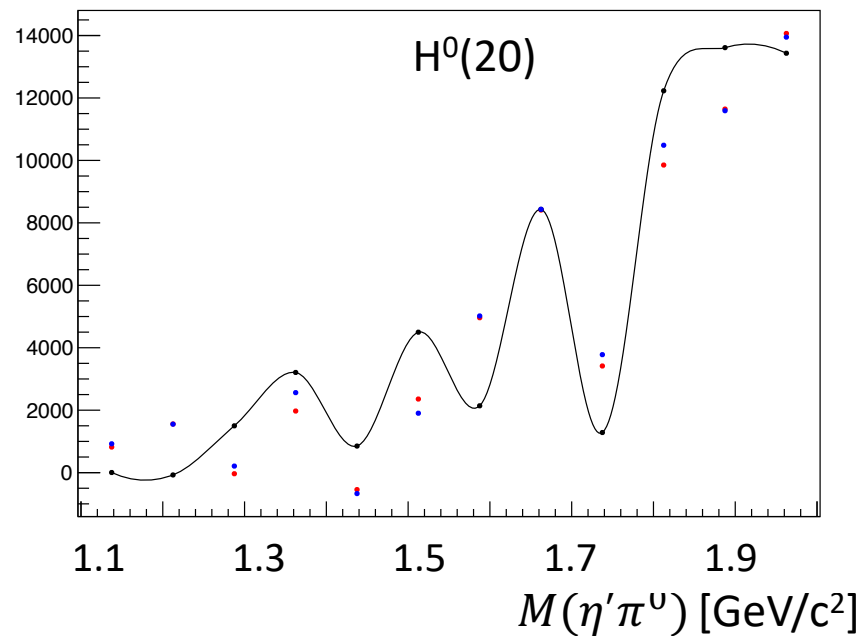
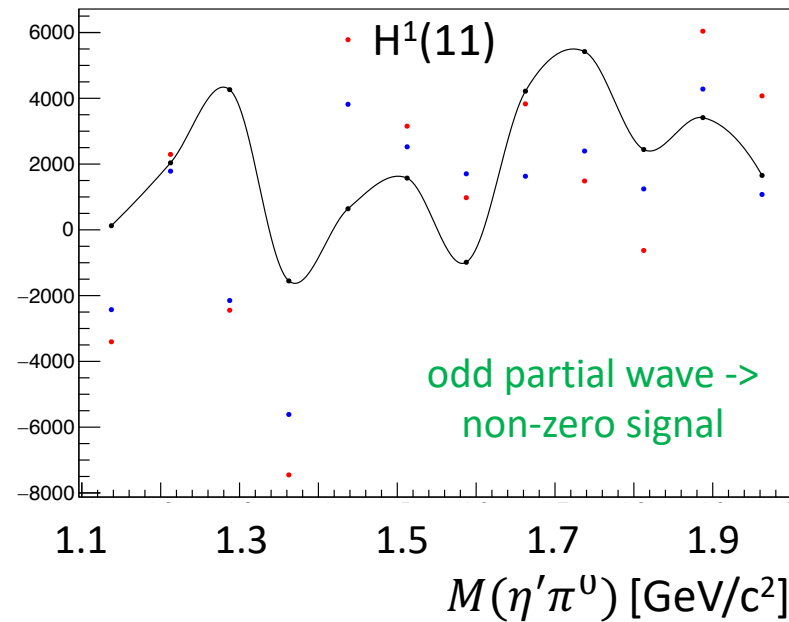
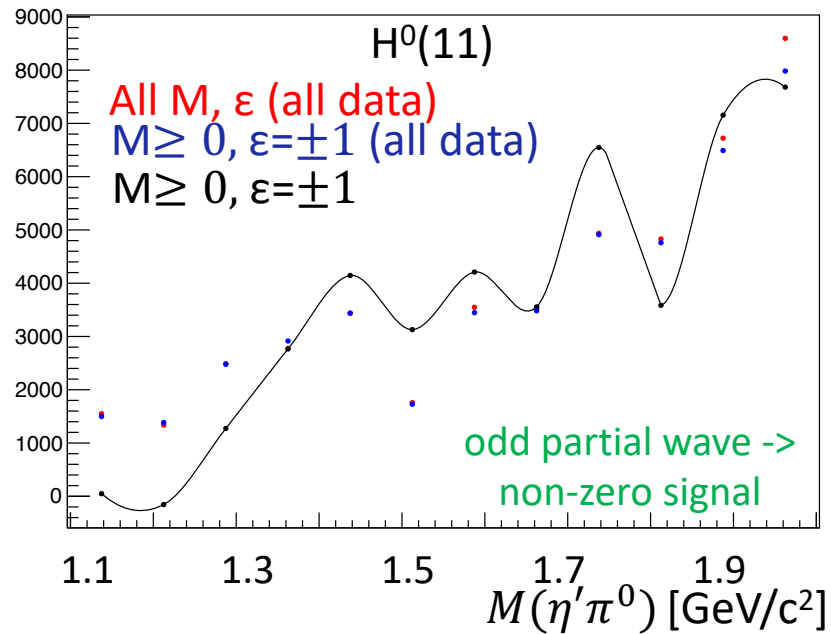
Fit with $S_0, P_{0,\pm 1}, D_{0,\pm 1,\pm 2} \ \varepsilon=\pm 1$

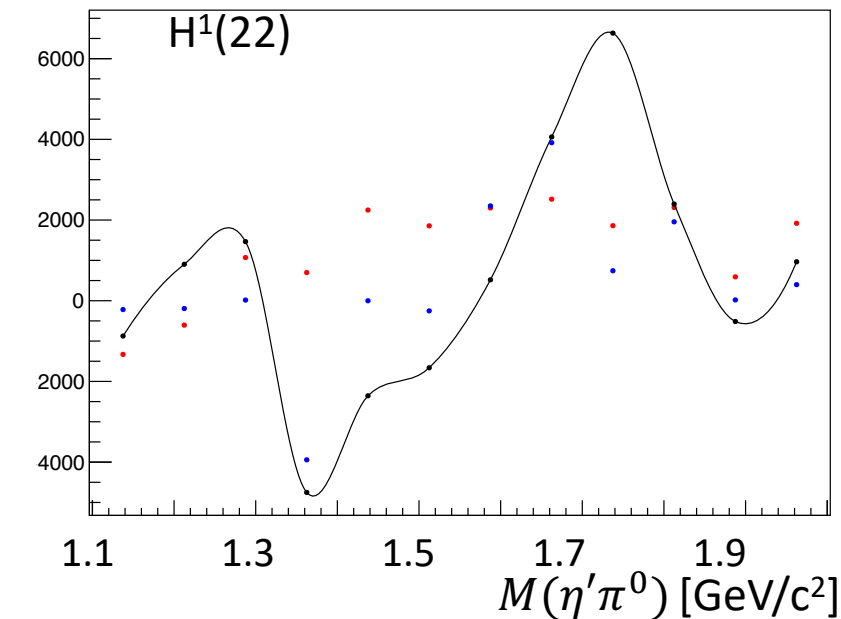
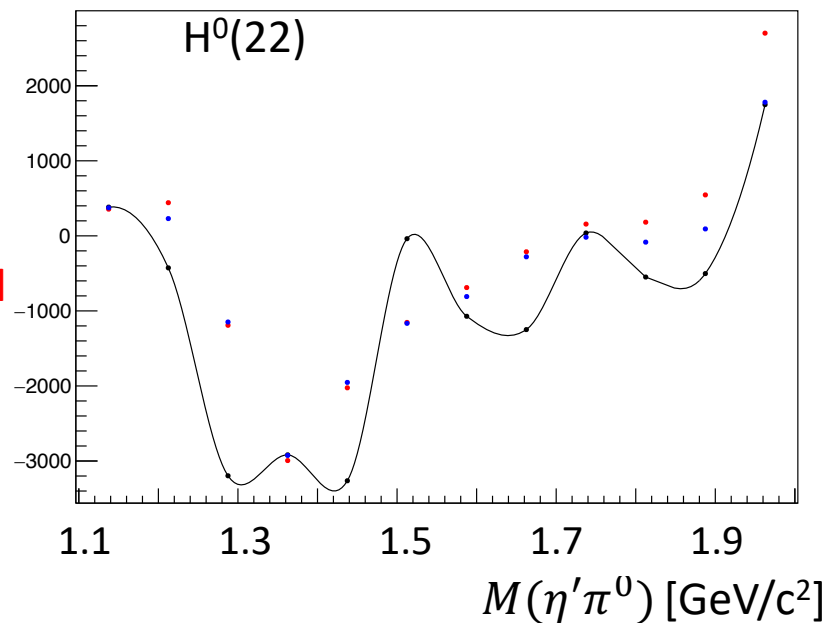
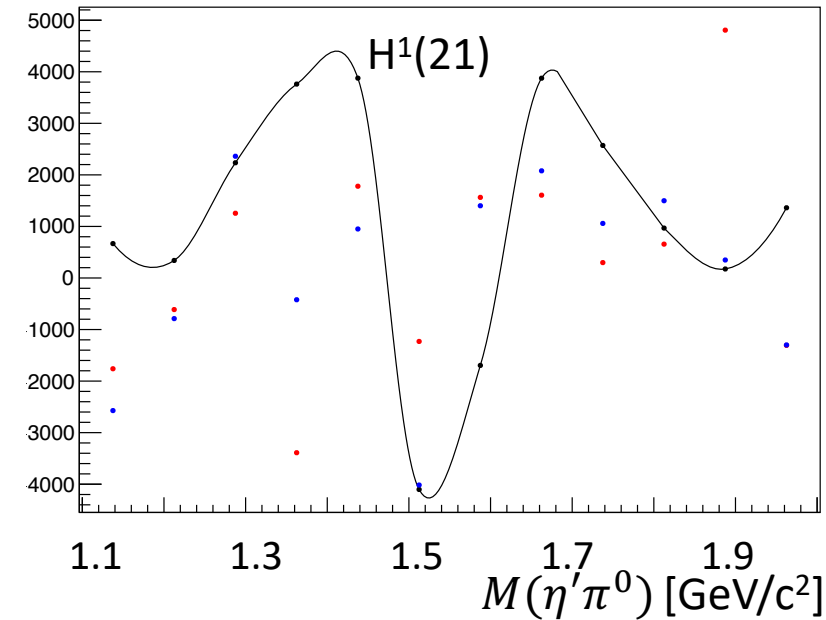
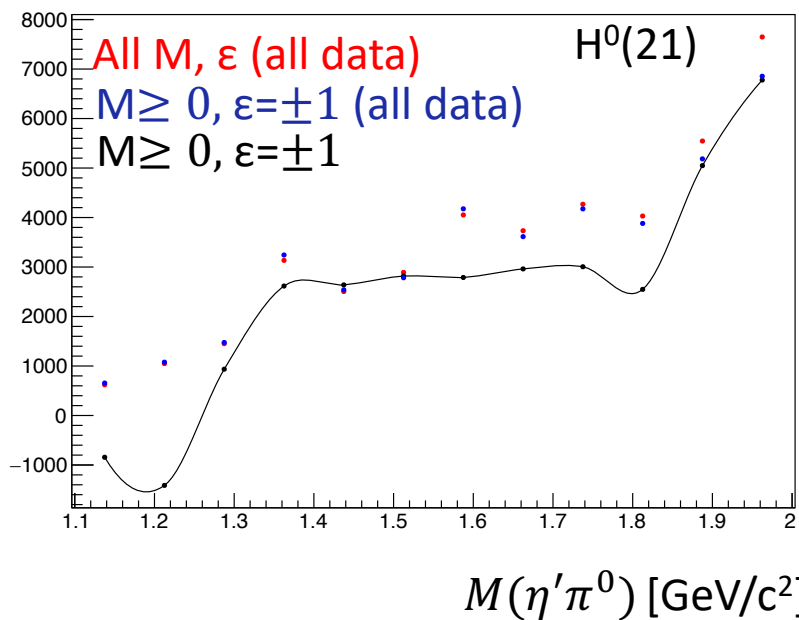


$M(\eta'\pi^0) [\text{GeV}/c^2]$



$0 < t < 0.3 \text{ (GeV/c)}^2$ 

$0 < t < 0.3 \text{ (GeV/c)}^2$ 

$0 < t < 0.3 \text{ (GeV/c)}^2$ 

Moments from fit
results with **all M, ϵ (all
data)**
agree with moments
from fit with **$M \geq$
 $0, \epsilon = \pm 1$ (all data)**

Summary

- Have used new loop statement to fit data for different polarization angles together
- Can improve fitting using more than 100 fits with randomized initial parameters, to choose good starting parameters
- Improve Q-factor signal-background separation
- Use different generated and accepted MC data files when fitting data corresponding to different polarizations
- Change the bin size?
- Compare the obtained moments to the ones obtained by weighting each event by corresponding intensity as defined in Mathiew et al.

$$H^0(LM) = \frac{P_\gamma}{2} \int_{\circ} I(\Omega, \Phi) d_{M0}^L(\theta) \cos M\phi,$$

$$H^1(LM) = \int_{\circ} I(\Omega, \Phi) d_{M0}^L(\theta) \cos M\phi \cos 2\Phi,$$

$$\text{Im } H^2(LM) = - \int_{\circ} I(\Omega, \Phi) d_{M0}^L(\theta) \sin M\phi \sin 2\Phi,$$

$$\text{with } \int_{\circ} = (1/\pi P_\gamma) \int_0^\pi \sin \theta d\theta \int_0^{2\pi} d\phi \int_0^{2\pi} d\Phi$$