

# PWA Challenge

Florida International University 2020

Mariana Khachatryan

# Generated ( $p\eta\pi^0$ ) events with AmpTools

Generated amplitudes are

- S0/a0 (980 MeV)
- P1/ $\pi_1$  (1400 MeV) (**exotic**)
- D1/a2 (1320 MeV)
- G1/a4 (1.995)

J-Spin

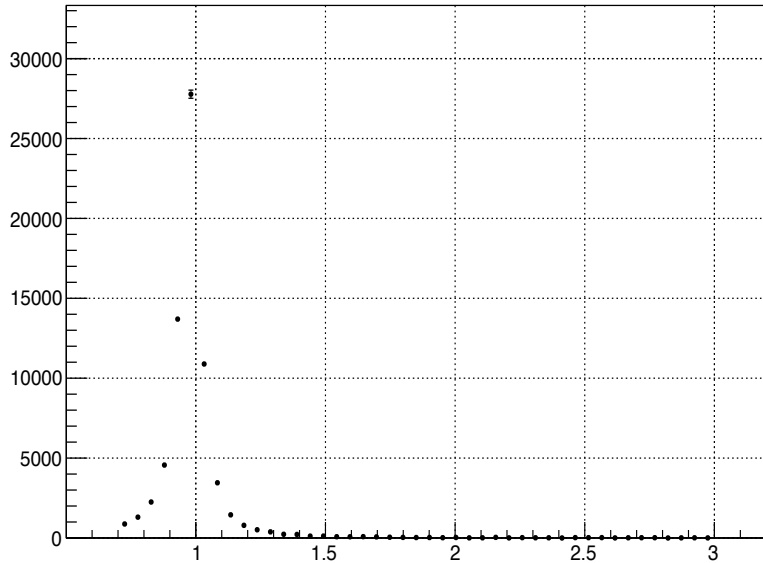
M-absolute value of spin projection along z axis

$\epsilon$ -reflectivity

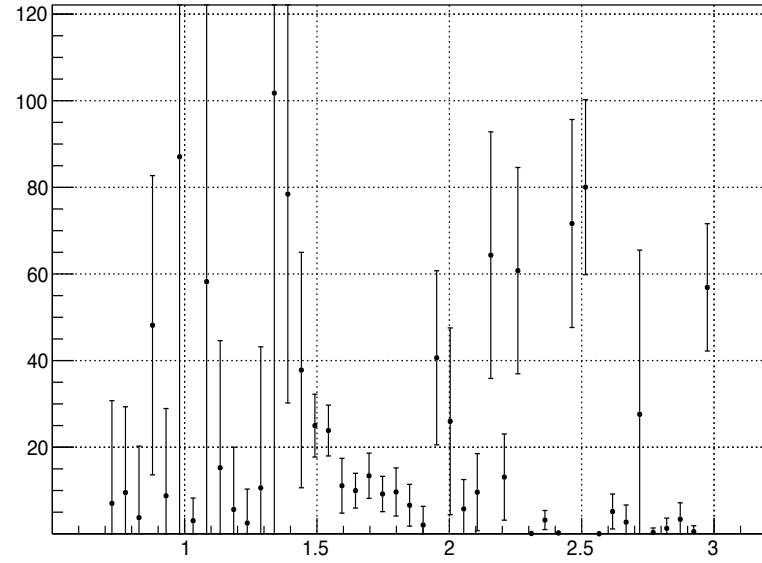
J	M	$\epsilon$	Real	Imaginary	BW Mass	BW Width
0	0	-1	2000	0	0.98	0.075
1	1	+1	60	140	1.354	0.330
2	1	+1	1000	0	1.318	0.111
4	1	+1	0	20	1.995	0.257

# Uncertainties from AMPTOOLS (MINUIT) for intensities from fitting in different M bins

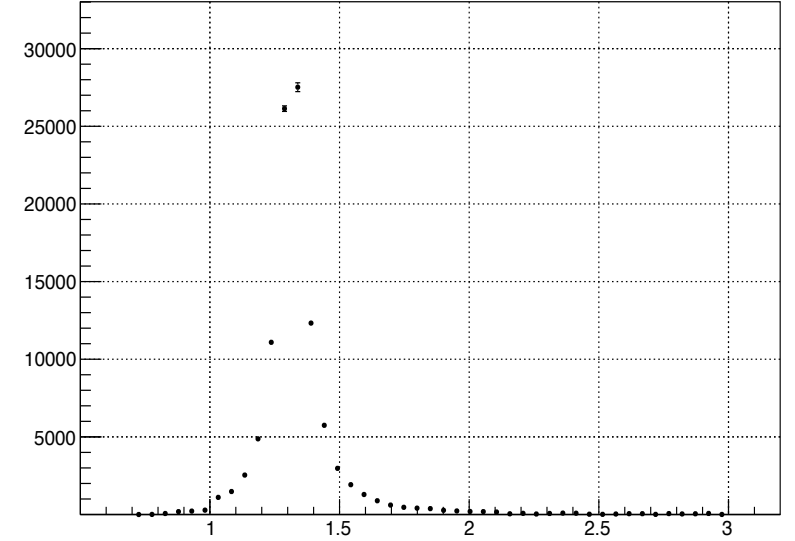
S0mi



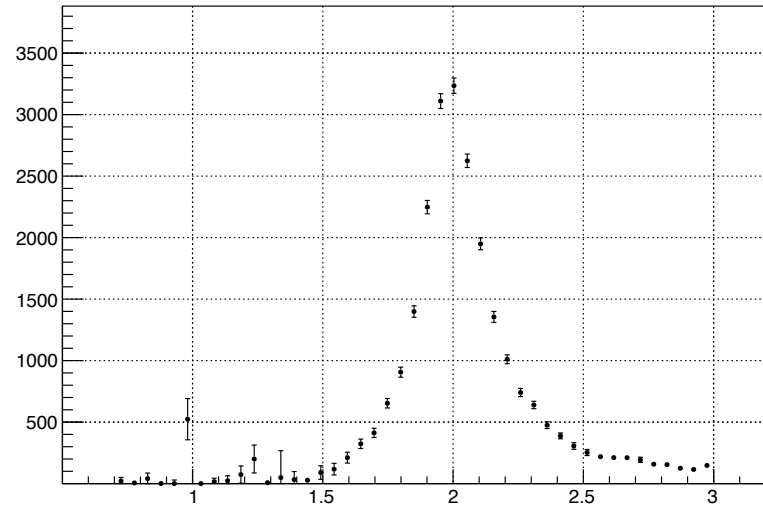
P1pl



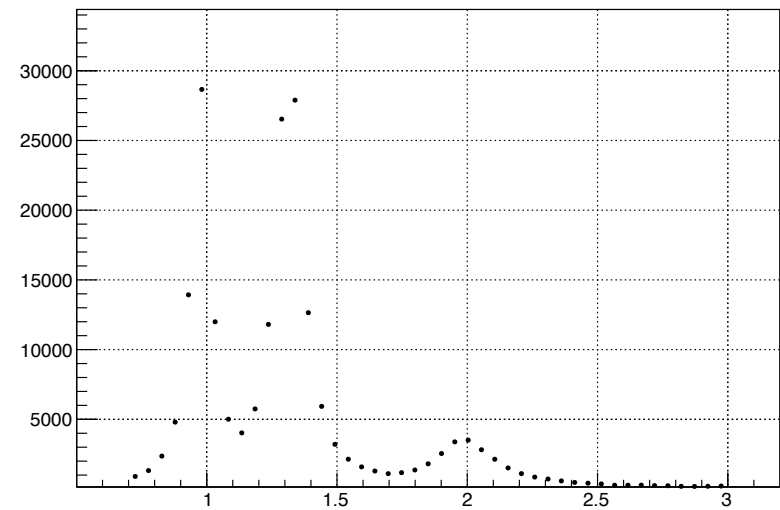
D1pl



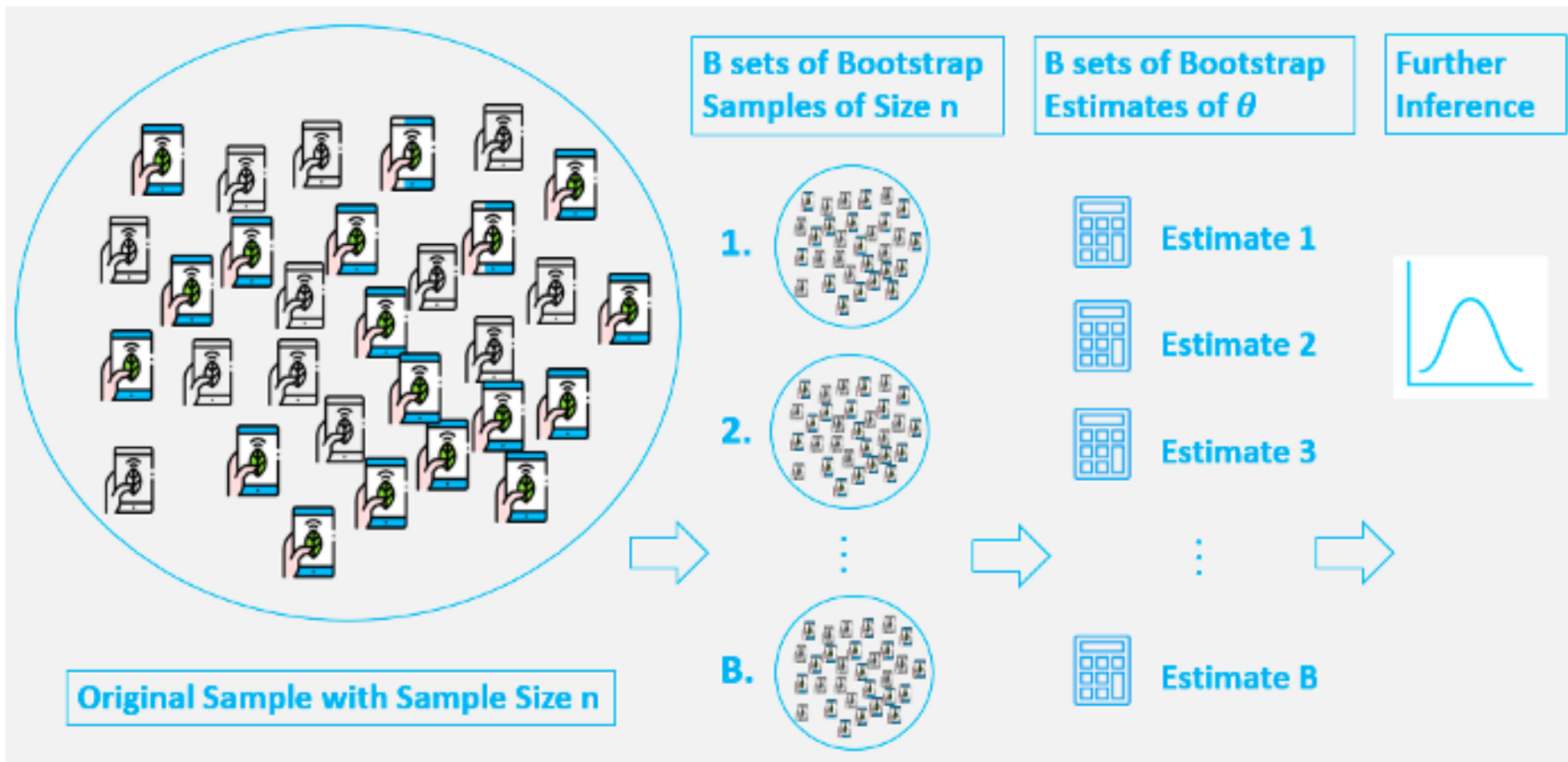
G1pl



All waves



# Bootstrapping



1. A sample from population with sample size  $n$ .

2. Draw a Bootstrap Sample from the original sample data with replacement with size  $n$

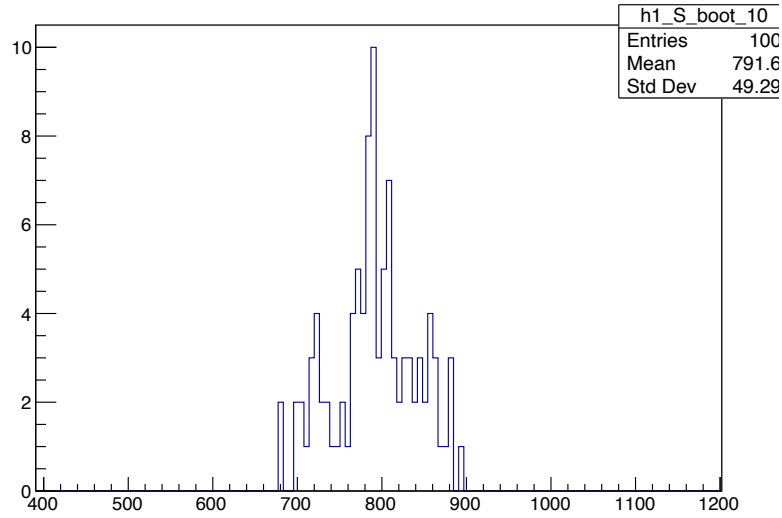
3. Evaluate  $\vartheta$  for each Bootstrap Sample, and there will be totally  $B$  estimates of  $\vartheta$ .

4. Construct a sampling distribution with these  $B$  Bootstrap statistics and use it to make further statistical inference, such as:

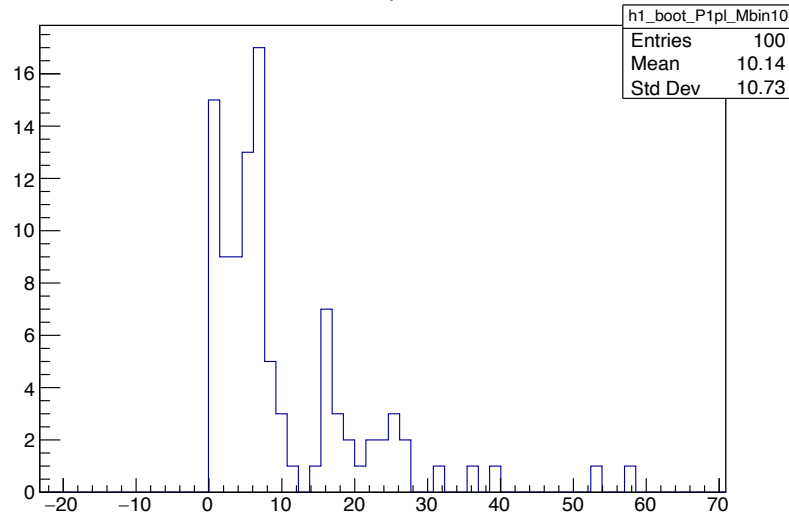
- Estimating the standard error of statistic for  $\vartheta$ .

# Intensity distributions from fitting 100 bootstrapping samples in M=1.2 GeV/c bin

S0 wave



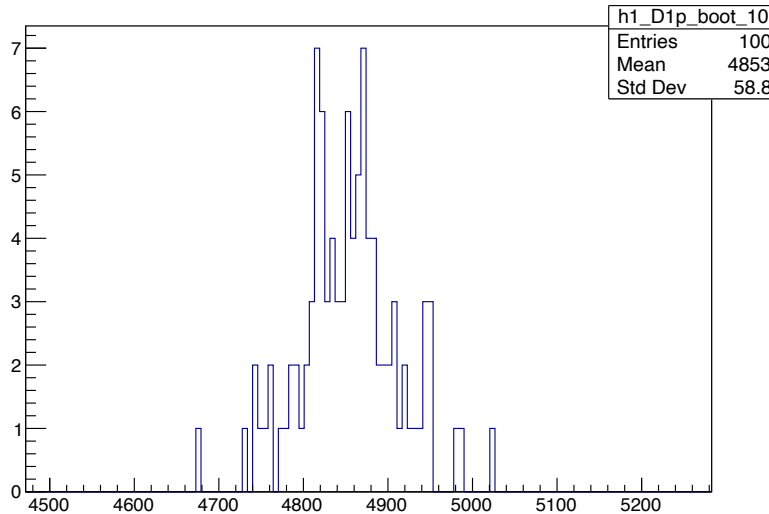
P1pl



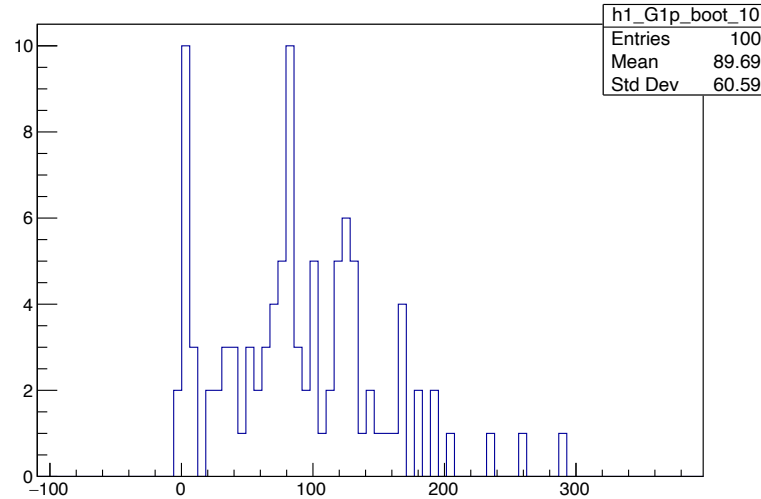
$$\sigma = \sqrt{\frac{\sum_i^B (I_i - I_{mean})^2}{B}}$$

B- number of Bootstraps (100 in this case )

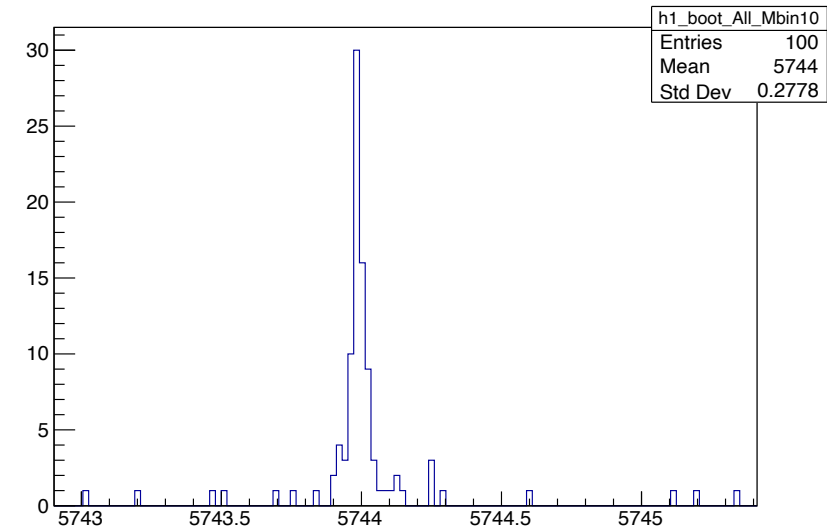
D1+ wave



G1+ wave

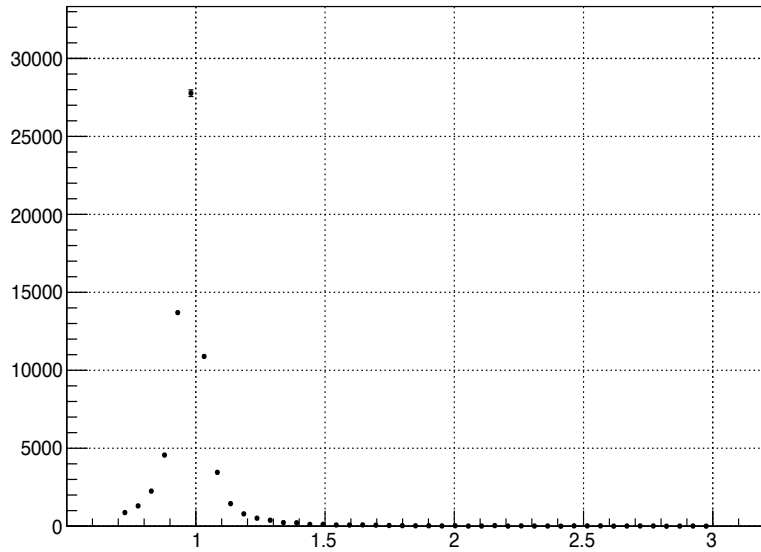


All waves

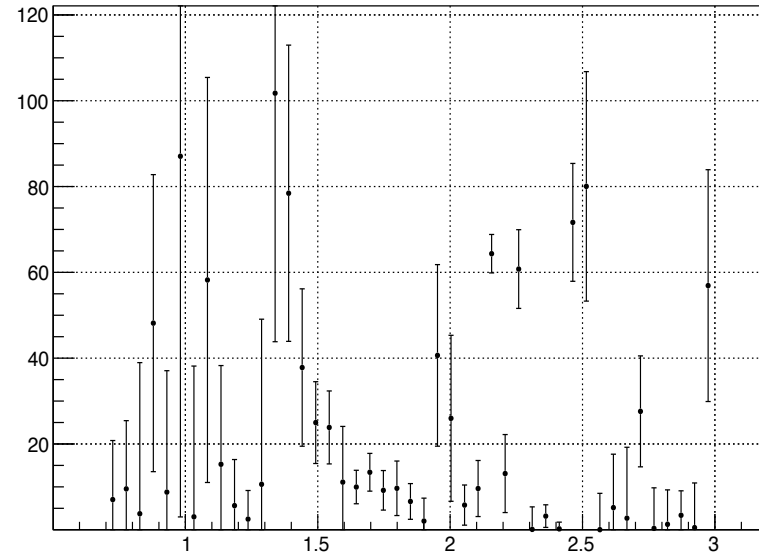


# Uncertainties from Bootstrapping for intensities from fitting in different M bins

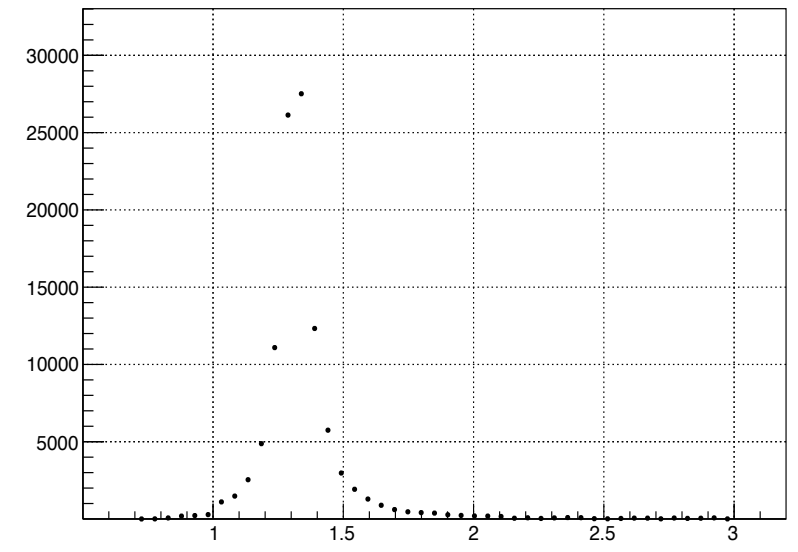
S0mi



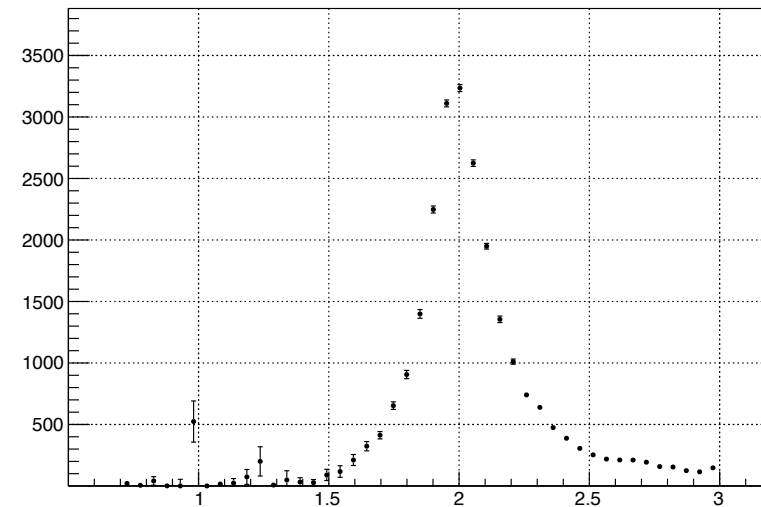
P1pl



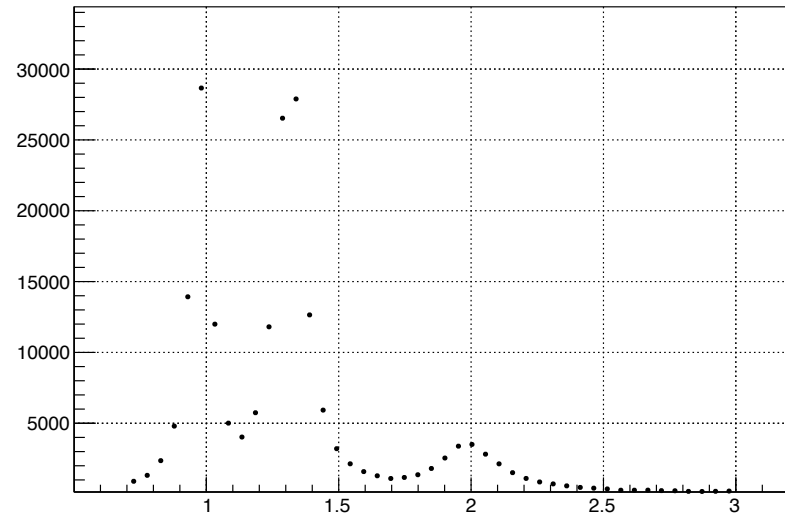
D1pl



G1pl



All waves



$$\sigma = \sqrt{\frac{\sum_i^B (I_i - I_{mean})^2}{B}}$$

- number of Bootstraps (100 in this case )