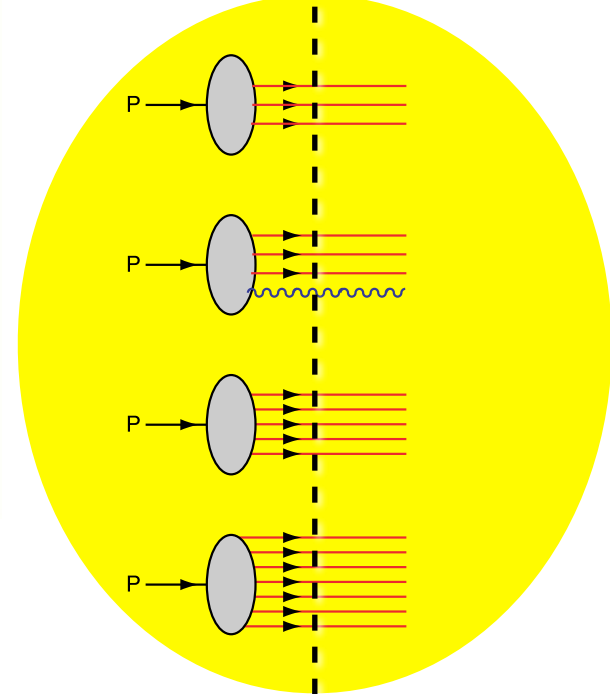
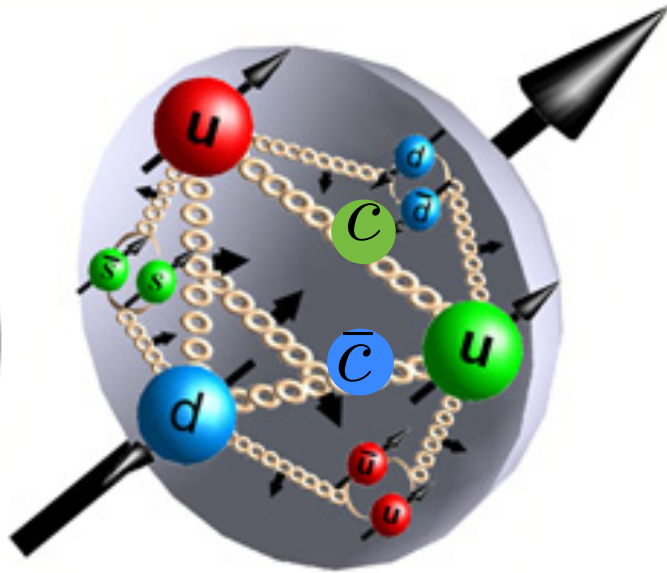
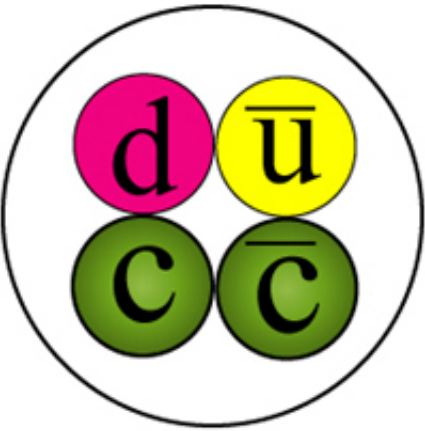


Novel QCD Phenomena in Nuclear Photo - and Electroproduction

Exotic Hadrons

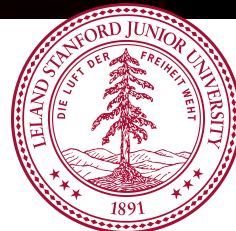


Fixed LF time

$$\tau = t + z/c$$

NUCLEAR PHOTOPRODUCTION WITH GLUEX
APRIL 28-29, 2016

Stan Brodsky



Jefferson Lab
 April 29, 2016

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

sum over states with $n=3, 4, \dots$ constituents

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

are boost invariant; they are independent of the hadron's energy and momentum P^μ .

The light-cone momentum fraction

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

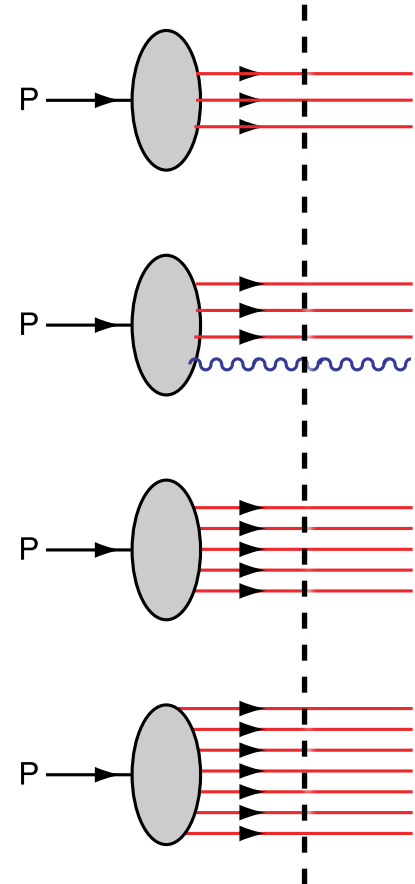
$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_i^\perp = \vec{0}^\perp.$$

Intrinsic heavy quarks
 $s(x), c(x), b(x)$ at high x !

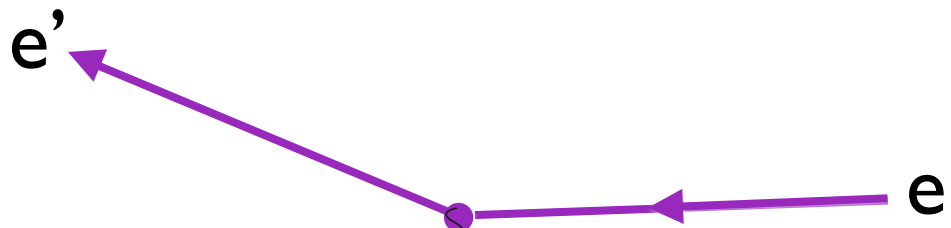
$$\bar{s}(x) \neq s(x)$$

$$\bar{u}(x) \neq \bar{d}(x)$$

Deuteron: Hidden Color



Fixed LF time
 $\tau = t + z/c$



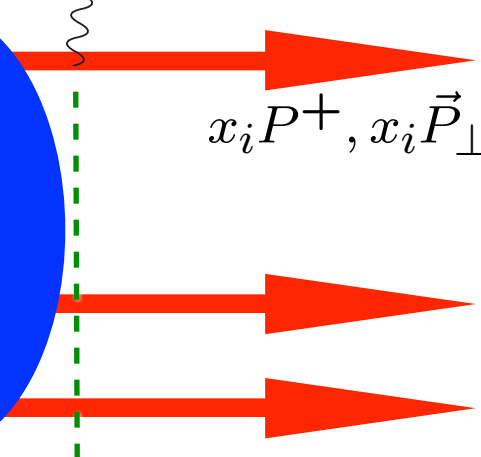
$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

P^+, \vec{P}_\perp



$$\psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

$x_i P^+, x_i \vec{P}_\perp + \vec{k}_{\perp i}$



*Eigenstate of LF Hamiltonian:
Off-shell in Invariant Mass*

***Measurements of hadron LF
wavefunction are at fixed LF time***

Fixed $\tau = t + z/c$

Like a flash photograph

$$x_{bj} = x = \frac{k^+}{P^+}$$

Each element of
flash photograph
illuminated
along the light front
at a fixed

$$\tau = t + z/c$$

Evolve in LF time

$$P^- = i \frac{d}{d\tau}$$

Eigenvalue

$$P^- = \frac{\mathcal{M}^2 + \vec{P}_\perp^2}{P^+}$$

$$H_{LF}^{QCD} |\Psi_h\rangle = \mathcal{M}_h^2 |\Psi_h\rangle$$



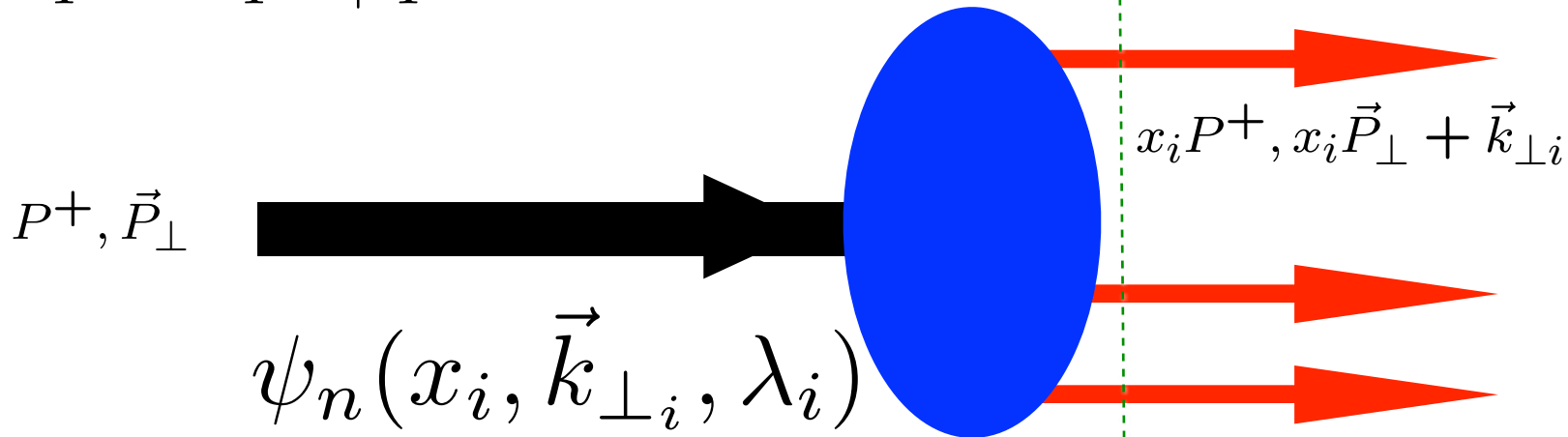
Light-Front Wavefunctions: **rigorous** representation of composite systems in quantum field theory

Eigenstate of LF Hamiltonian: Off-shell in Invariant Mass

$$x = \frac{k^+}{P^+} = \frac{k^0 + k^3}{P^0 + P^3}$$

Fixed $\tau = t + z/c$

Fixed LF time



$$|p, J_z \rangle = \sum_{n=3} \psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; x_i, \vec{k}_{\perp i}, \lambda_i \rangle$$

$$\sum_i^n x_i = 1$$

$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

Invariant under boosts! Independent of P^μ

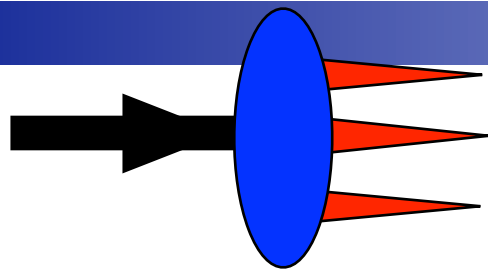
Sum Rules

Causal, Frame-independent. Creation Operators on Simple Vacuum, Current Matrix Elements are Overlaps of LFWFS

Independent of Observer's Motion



- **Measurements are made at fixed τ**
- **Causality is automatic**
- **Structure Functions are squares of LFWFs**
- **Form Factors are overlap of LFWFs**
- **LFWFs are frame-independent: no boosts, no pancakes!**
- **Same structure function measured at an e p collider and the proton rest frame**
- **No dependence on observer's frame**
- **LF Holography: Dual to AdS space**
- **LF Vacuum trivial -- no vacuum condensates!**
- **Profound implications for Cosmological Constant**

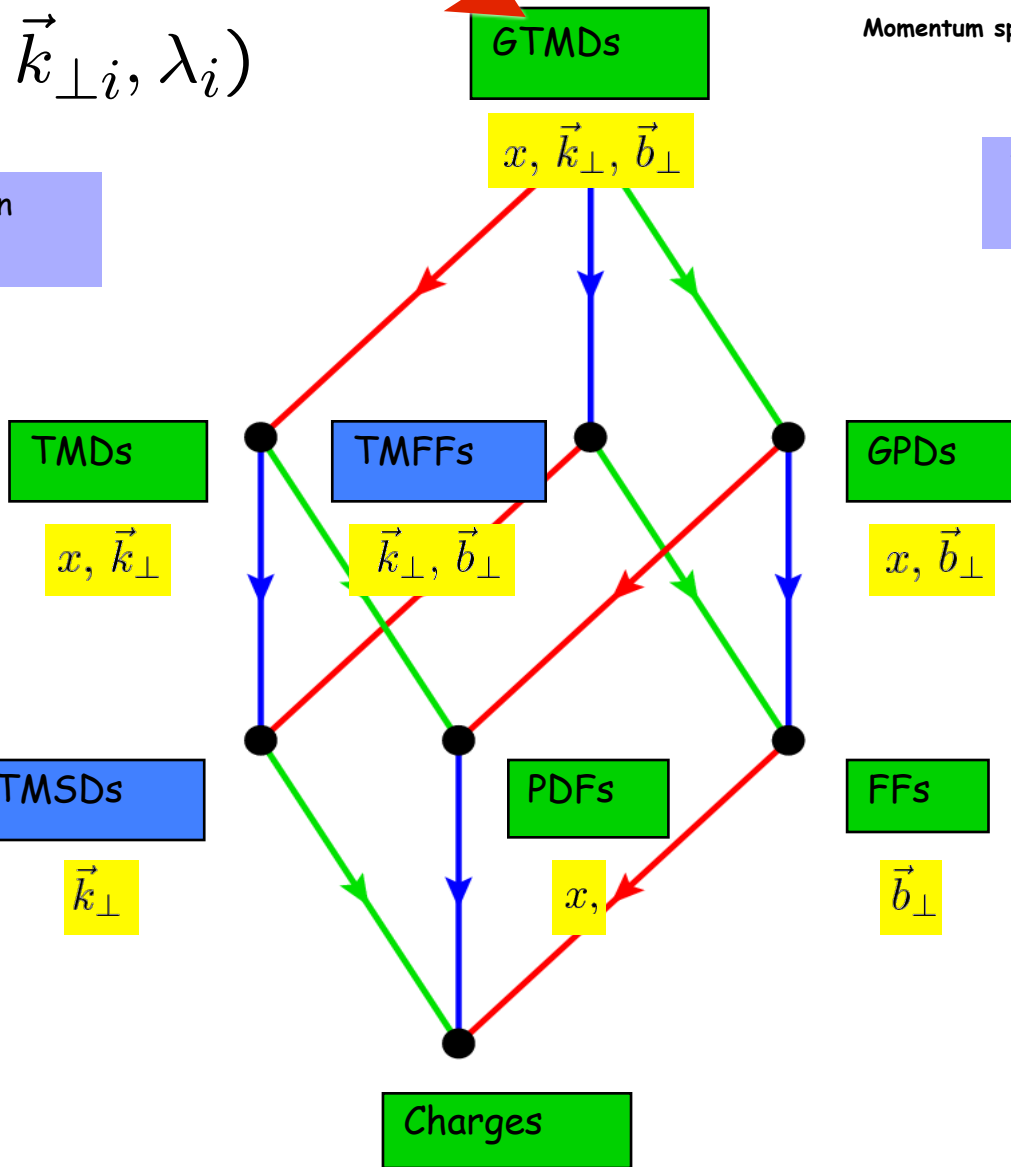


• *Light Front Wavefunctions:*

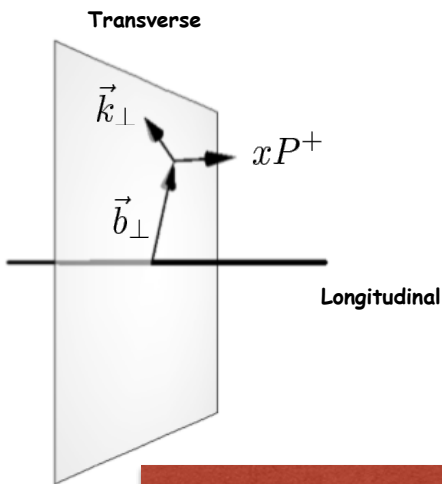
$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

Transverse density in momentum space

Momentum space $\vec{k}_{\perp} \leftrightarrow \vec{z}_{\perp}$ Position space
 $\vec{\Delta}_{\perp} \leftrightarrow \vec{b}_{\perp}$
 Transverse density in position space



*Lorce,
Pasquini*



→ $\int d^2 b_{\perp}$
 → $\int dx$
 → $\int d^2 k_{\perp}$

+ Factorization-Breaking Lensing Corrections: Sivers, T-odd

Some Key QCD Issues in Electroproduction

- **Intrinsic Heavy Quarks at high x ;** $s(x) \neq \bar{s}(x)$
- **Role of Color Confinement in DIS**
- **Hadronization at the Amplitude Level**
- **Leading-Twist Lensing: Sivers Effect**
- **Diffraction DIS**
- **Static versus Dynamic Structure Functions**
- **Origin of Shadowing and Anti-Shadowing**
- **Is Anti-Shadowing Non-Universal: Flavor Specific?**
- **Nuclear Correlations and Effects**

Color Transparency

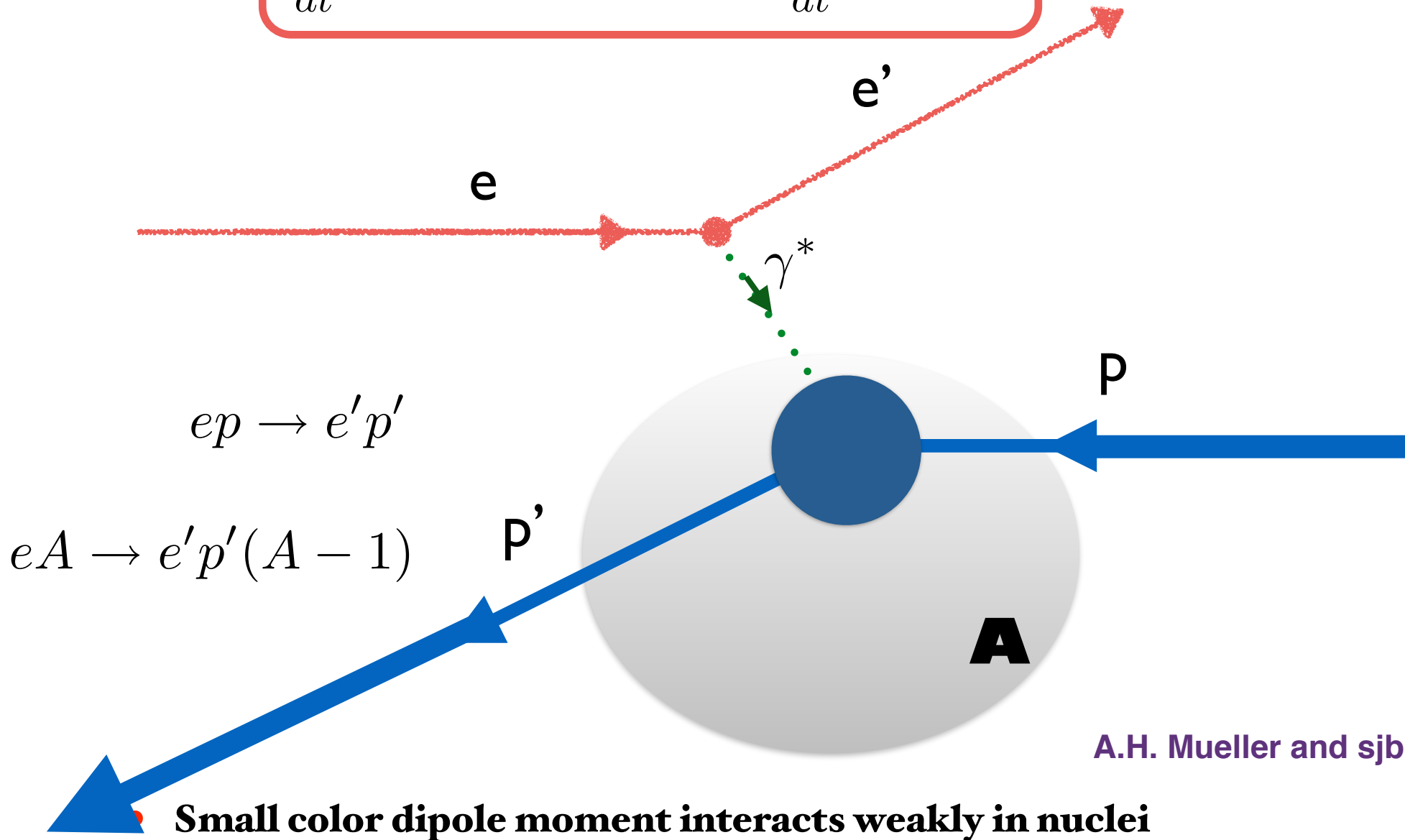
**Bertsch, Gunion, Goldhaber, sjb
Mueller, sjb
Frankfurt, Strikman, Miller**

$$\frac{d\sigma}{dt}(eA \rightarrow ep(A-1)) = Z \frac{d\sigma}{dt}(ep \rightarrow ep) \quad \text{at high momentum transfer}$$

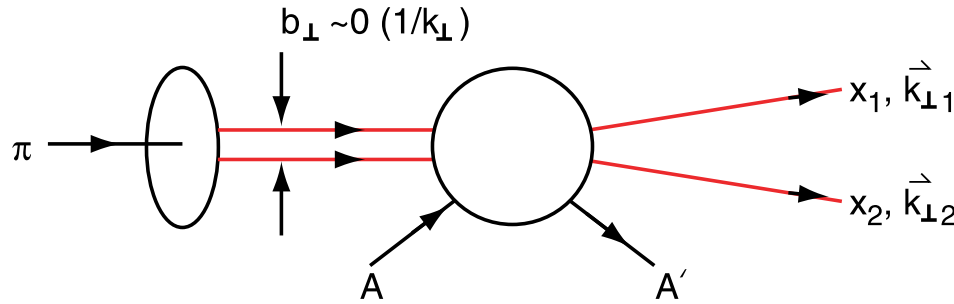
- **Fundamental test of gauge theory in hadron physics**
- **Small color dipole moment interacts weakly in nuclei**
- **Complete coherence at high energies** *See Strikman Talk*
- **Many tests in hard exclusive processes**
- **Clear Demonstration of CT from Diffractive Di-Jets**
- **Explains Baryon Anomaly at RHIC**

Color Transparency

$$\frac{d\sigma}{dt}(eA \rightarrow ep(A-1)) = Z \frac{d\sigma}{dt}(ep \rightarrow ep)$$



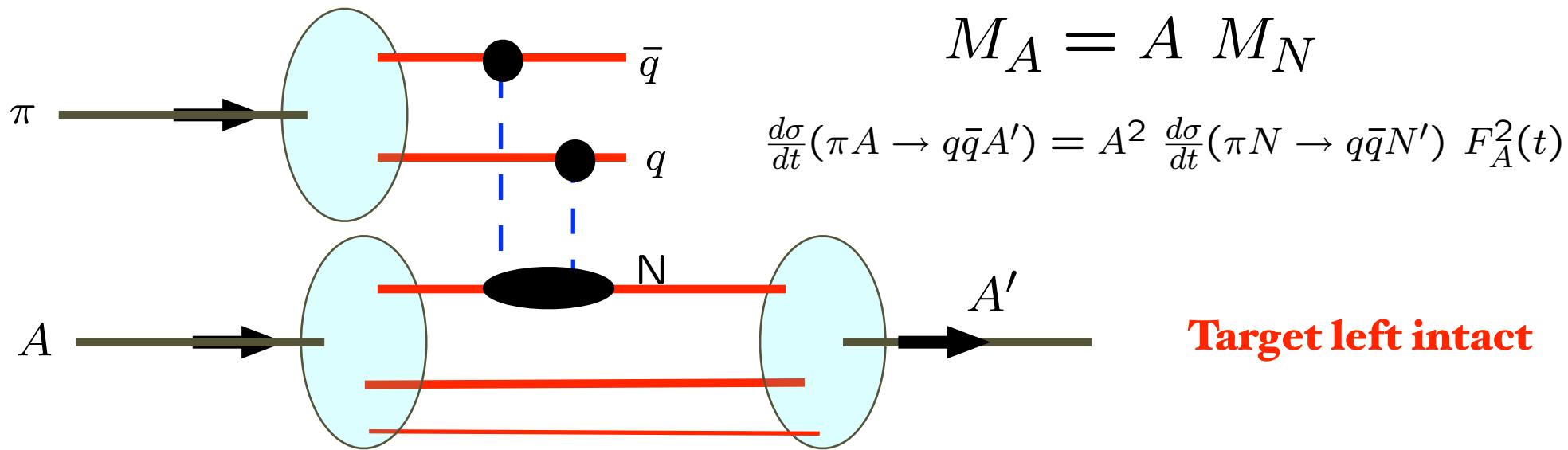
A.H. Mueller and sjb



large k_{\perp} , small b_{\perp}

*Small color-dipole moment pion not absorbed;
interacts with each nucleon coherently*

QCD COLOR Transparency



Diffraction, Rapidity gap

Measure pion LFWF in diffractive dijet production Confirmation of color transparency

A-Dependence results: $\sigma \propto A^\alpha$

<u>k_t range (GeV/c)</u>	<u>α</u>	<u>α (CT)</u>
$1.25 < k_t < 1.5$	$1.64 +0.06 -0.12$	1.25
$1.5 < k_t < 2.0$	1.52 ± 0.12	1.45
$2.0 < k_t < 2.5$	1.55 ± 0.16	1.60

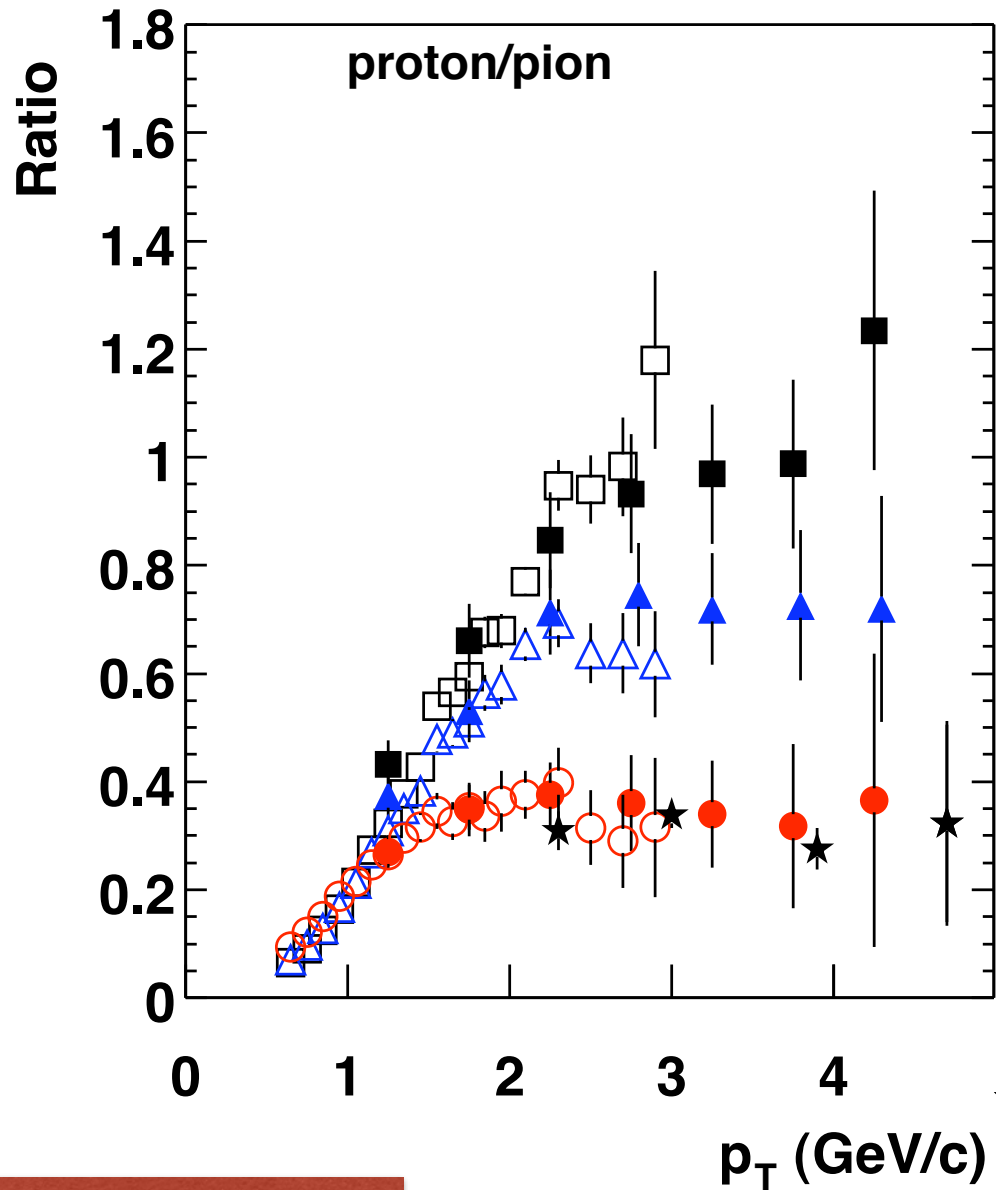
Ashery E791

α (Incoh.) = 0.70 ± 0.1

Conventional Glauber Theory Ruled Out !

Factor of 7

Particle ratio changes with centrality!



← **Central**

- ■ Au+Au 0-10%
- △ ▲ Au+Au 20-30%
- ● Au+Au 60-92%
- ★ p+p, $\sqrt{s} = 53$ GeV, ISR
- e⁺e⁻, gluon jets, DELPHI
- e⁺e⁻, quark jets, DELPHI

← **Peripheral**

*Protons less absorbed
in nuclear collisions than pions
because of dominant
color-transparent higher twist process*

Arleo, Hwang, Sickles, sjb

**Tannenbaum:
Baryon Anomaly**

Evidence for Direct, Higher-Twist, Color Transparent Subprocesses at RHIC

- **Anomalous power behavior at fixed x_T**
- **Protons more likely to come from direct subprocess than pions**
- **Protons less absorbed than pions in “central” nuclear collisions because of color transparency**
- **Predicts increasing proton to pion ratio in “central” collisions**
- **Exclusive-inclusive connection at $x_T = 1$**

EIC: Resolves complex physics signals at hadron and ion colliders

Hidden Color in QCD

Gluon or Quark Exchange within nucleus

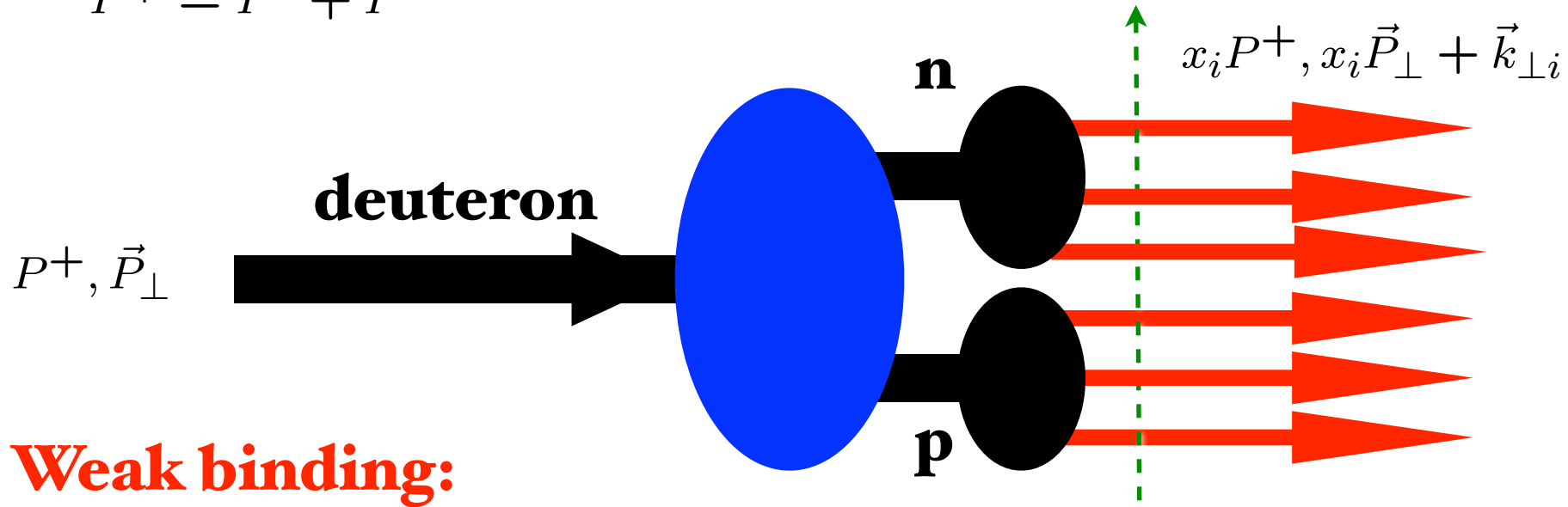
Lepage, Ji, sjb

- Deuteron six-quark wavefunction:
- 5 color-singlet combinations of six color-triplets --
- Only one of the five states is $|\ln p\rangle$
- Components evolve towards equality at short distances
- Hidden color states dominate deuteron form factor and photodisintegration at high momentum transfer
- Dominates $x > 1$ domain of deep inelastic scattering on nuclei: quark carries momentum of more than one nucleus!

$$\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++}\Delta^{-}) \simeq \frac{d\sigma}{dt}(\gamma d \rightarrow pn) \text{ at high } Q^2$$

$$P^+ = P^0 + P^z$$

Fixed $\tau = t + z/c$



$$\psi_d(x_i, \vec{k}_{\perp i}) = \psi_d^{body} \times \psi_n \times \psi_p$$

$$\sum_i^n x_i = 1$$

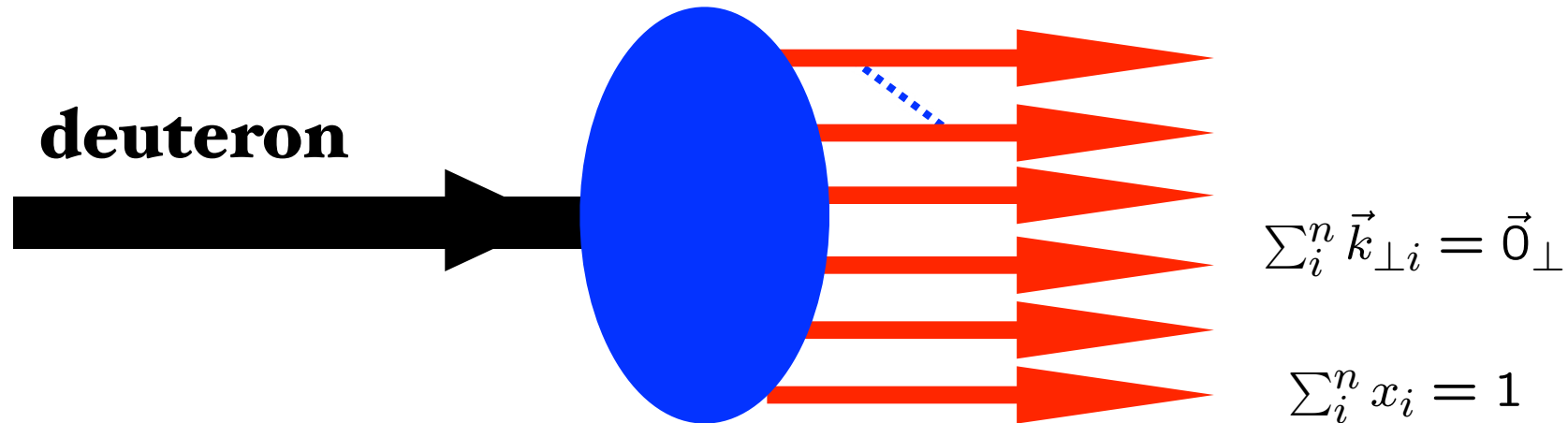
$$\sum_i^n \vec{k}_{\perp i} = \vec{0}_\perp$$

Nuclear Physics:
Two color-singlet combinations of three 3_c

pQCD Evolution of 5 color-singlet Fock states

Lepage, Ji, sjb

$$\Psi_n^d(x_i, \vec{k}_{\perp i}, \lambda_i)$$



$$\Phi_n(x_i, Q) = \int^{k_{\perp i}^2 < Q^2} \prod' d^2 k_{\perp j} \psi_n(x_i, \vec{k}_{\perp j})$$

5 X 5 Matrix Evolution Equation for deuteron
distribution amplitude

Hidden Color of Deuteron

Deuteron six-quark state has five color-singlet configurations, only one of which is n-p.

Asymptotic Solution has Expansion

$$\psi_{[6]\{33\}} = \left(\frac{1}{9}\right)^{1/2} \psi_{NN} + \left(\frac{4}{45}\right)^{1/2} \psi_{\Delta\Delta} + \left(\frac{4}{5}\right)^{1/2} \psi_{CC}$$

ERBL Evolution: Transition to Delta-Delta

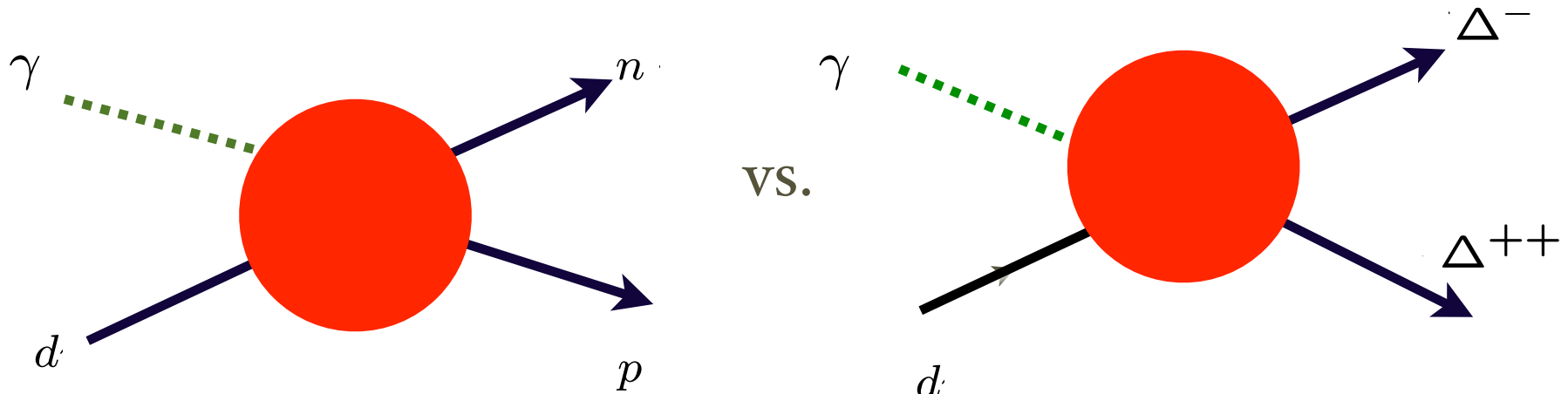
Lepage, Ji, sjb

Test of Hidden Color in Deuteron Photodisintegration

$$R = \frac{\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++} \Delta^{--})}{\frac{d\sigma}{dt}(\gamma d \rightarrow pn)}$$

Ratio predicted to approach 2:5

Ratio should grow with transverse momentum as the hidden color component of the deuteron grows in strength.



Possible contribution from pion charge exchange at small t .

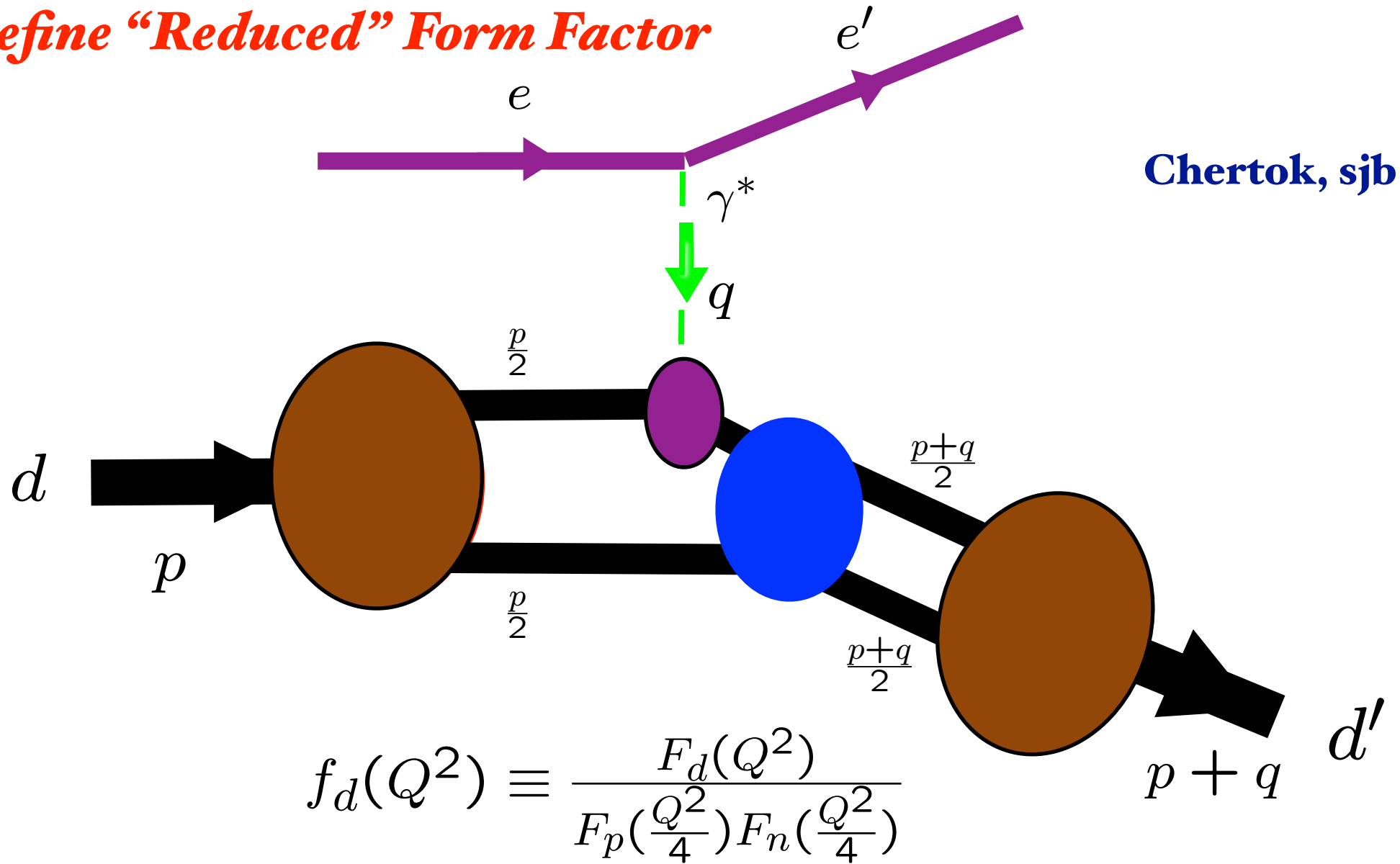
Hidden Color in QCD

Study the Deuteron as a QCD Object

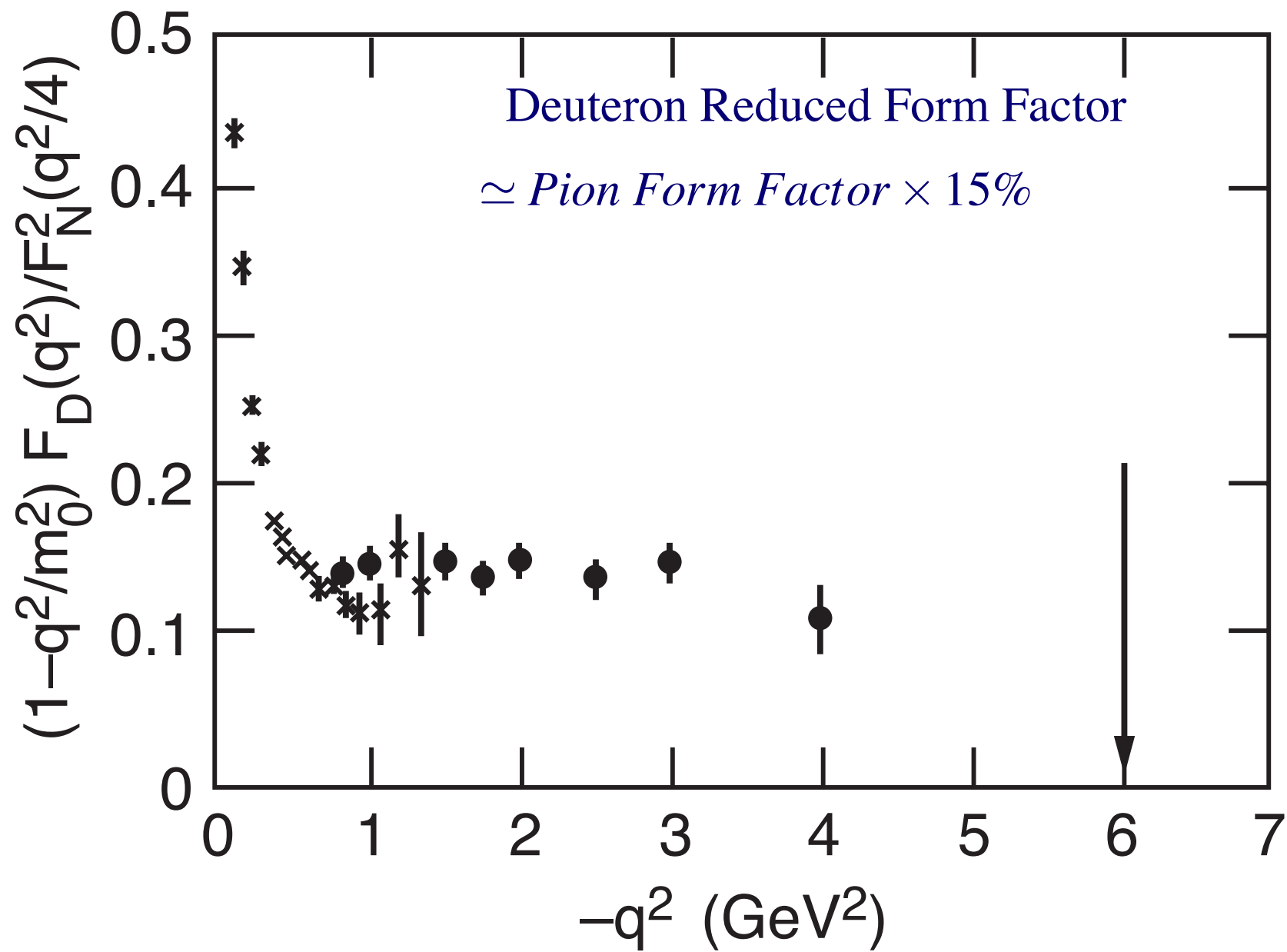
- **Deuteron six-quark wavefunction**
- **5 color-singlet combinations of 6 color-triplets -- only one state is $|n p\rangle$**
- **Components evolve towards equality at short distances**
- **Hidden color states dominate deuteron form factor and photodisintegration at high momentum transfer**
- **Predict**

$$\frac{d\sigma}{dt}(\gamma d \rightarrow \Delta^{++}\Delta^{-}) \simeq \frac{d\sigma}{dt}(\gamma d \rightarrow pn) \text{ at high } Q^2$$

Define "Reduced" Form Factor



Elastic electron-deuteron scattering



QCD Prediction for Deuteron Form Factor

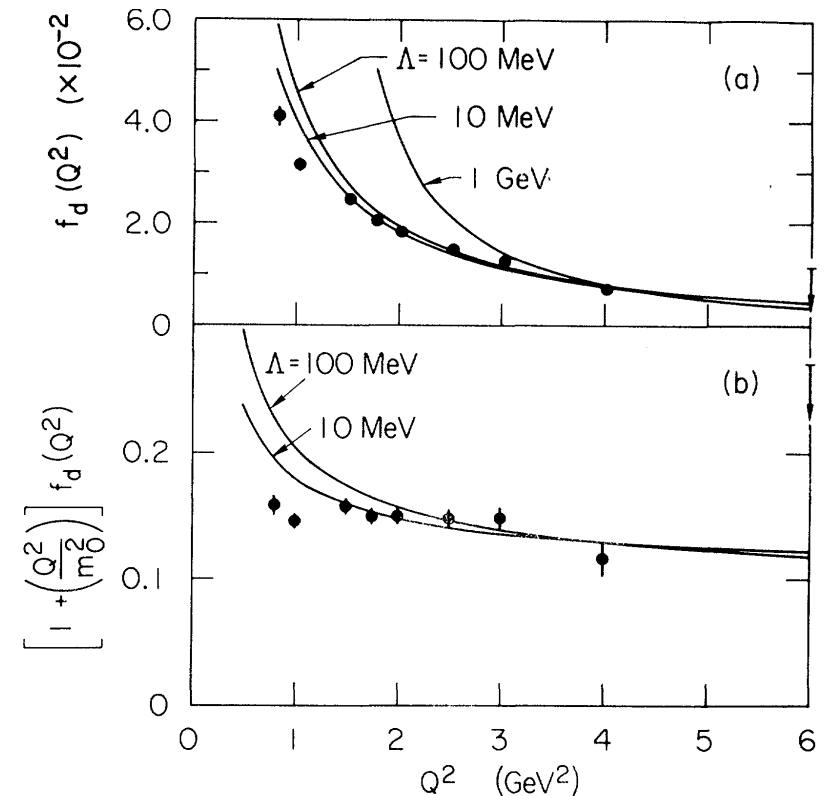
Lepage, Ji, sjb

$$F_d(Q^2) = \left[\frac{\alpha_s(Q^2)}{Q^2} \right]^5 \sum_{m,n} d_{mn} \left(\ln \frac{Q^2}{\Lambda^2} \right)^{-\gamma_n^d - \gamma_m^d} \left[1 + \mathcal{O} \left(\alpha_s(Q^2), \frac{m}{Q} \right) \right]$$

Define “Reduced” Form Factor

$$f_d(Q^2) \equiv \frac{F_d(Q^2)}{F_N^2(Q^2/4)} \cdot$$

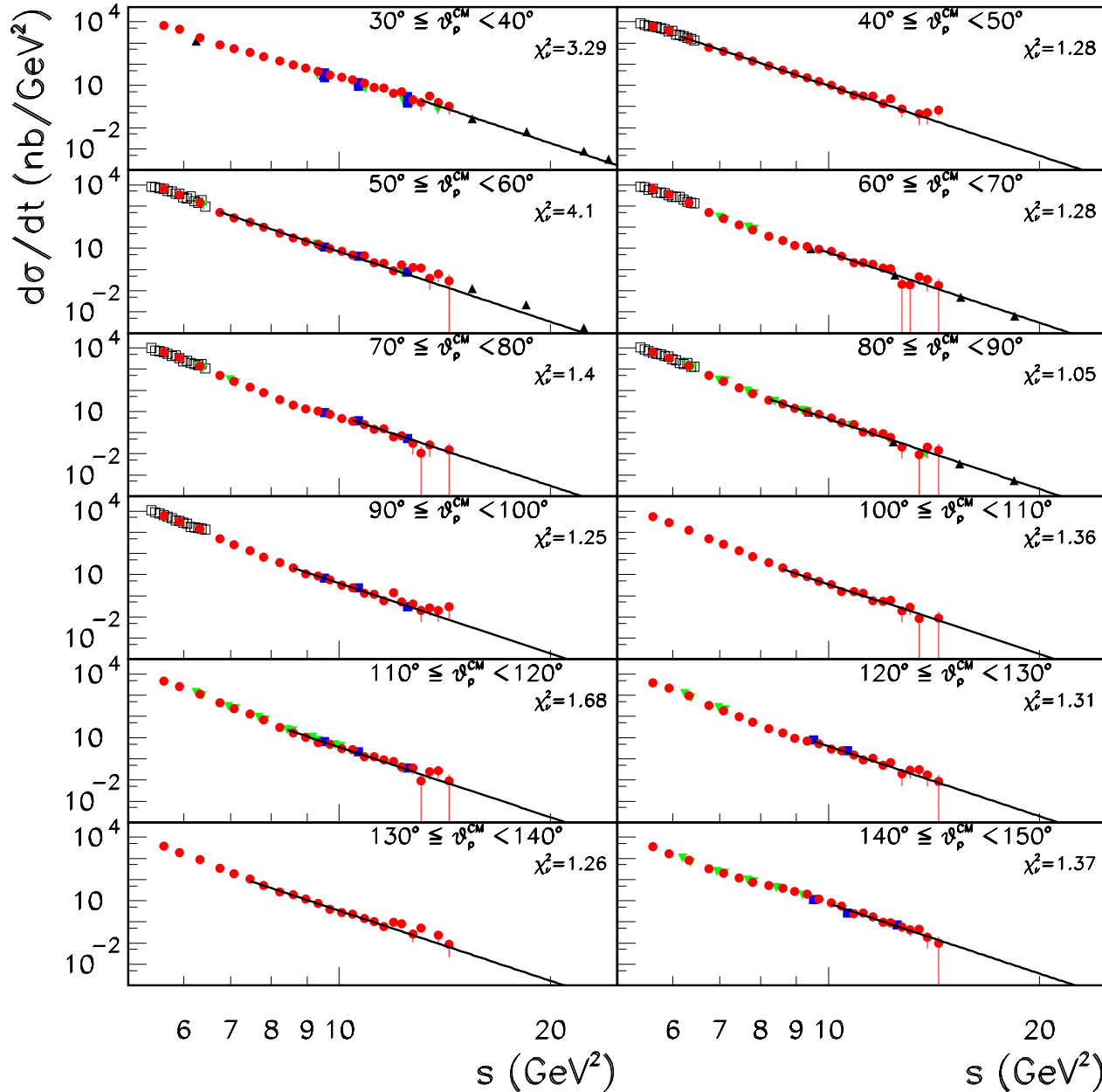
$$f_d(Q^2) \sim \frac{\alpha_s(Q^2)}{Q^2} \left(\ln \frac{Q^2}{\Lambda^2} \right)^{-(2/5) C_F/\beta}$$



(a) Comparison of the asymptotic QCD prediction $f_d(Q^2) \propto (1/Q^2) [\ln(Q^2/\Lambda^2)]^{-1-(2/5)C_F/\beta}$ with final data of Ref. 10 for the reduced deuteron form factor, where $F_N(Q^2) = [1 + Q^2/(0.71 \text{ GeV}^2)]^{-2}$. The normalization is fixed at the $Q^2 = 4 \text{ GeV}^2$ data point. (b) Comparison of the prediction $[1 + (Q^2/m_0^2)] f_d(Q^2) \propto [\ln(Q^2/\Lambda^2)]^{-1-(2/5)C_F/\beta}$ with the above data. The value $m_0^2 = 0.28 \text{ GeV}^2$ is used

Same large momentum transfer behavior as pion form factor

Deuteron Photodisintegration



PQCD and AdS/CFT:

$$s^{n_{tot}-2} \frac{d\sigma}{dt} (A + B \rightarrow C + D) = F_{A+B \rightarrow C+D}(\theta_{CM})$$

$$s^{11} \frac{d\sigma}{dt} (\gamma d \rightarrow np) = F(\theta_{CM})$$

$$n_{tot} - 2 = (1 + 6 + 3 + 3) - 2 = 11$$

Reflects conformal invariance

Properties of Hard Exclusive Reactions

- **Dimensional Counting Rules at fixed CM angle**
- **Hadron Helicity Conservation**
- **Color Transparency**
- **Hidden color**
- **$s \gg -t \gg \Lambda_{\text{QCD}}$: Reggeons have negative-integer intercepts at large $-t$**
- **$J=0$ Fixed pole in DVCS**
- **Quark interchange — no gluon exchange evident**
- **Renormalization group invariance**
- **No renormalization scale ambiguity**
- **Exclusive inclusive connection with spectator counting rules**
- **Diffractive reactions from pomeron, Reggeon, odderon**

$$|p, S_z\rangle = \sum_{n=3} \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) |n; \vec{k}_{\perp i}, \lambda_i\rangle$$

sum over states with $n=3, 4, \dots$ constituents

The Light Front Fock State Wavefunctions

$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

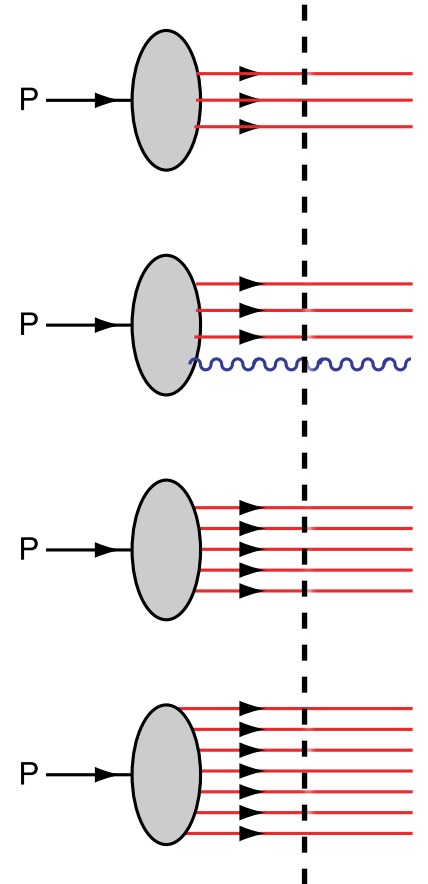
are boost invariant; they are independent of the hadron's energy and momentum P^μ .

The light-cone momentum fraction

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^z}{P^0 + P^z}$$

are boost invariant.

$$\sum_i^n k_i^+ = P^+, \quad \sum_i^n x_i = 1, \quad \sum_i^n \vec{k}_i^\perp = \vec{0}^\perp.$$



Fixed LF time

Hidden Color

Intrinsic heavy quarks
 $s(x), c(x), b(x)$ at high x !

$\bar{s}(x) \neq s(x)$
 $\bar{u}(x) \neq \bar{d}(x)$

Mueller: gluon Fock states BFKL

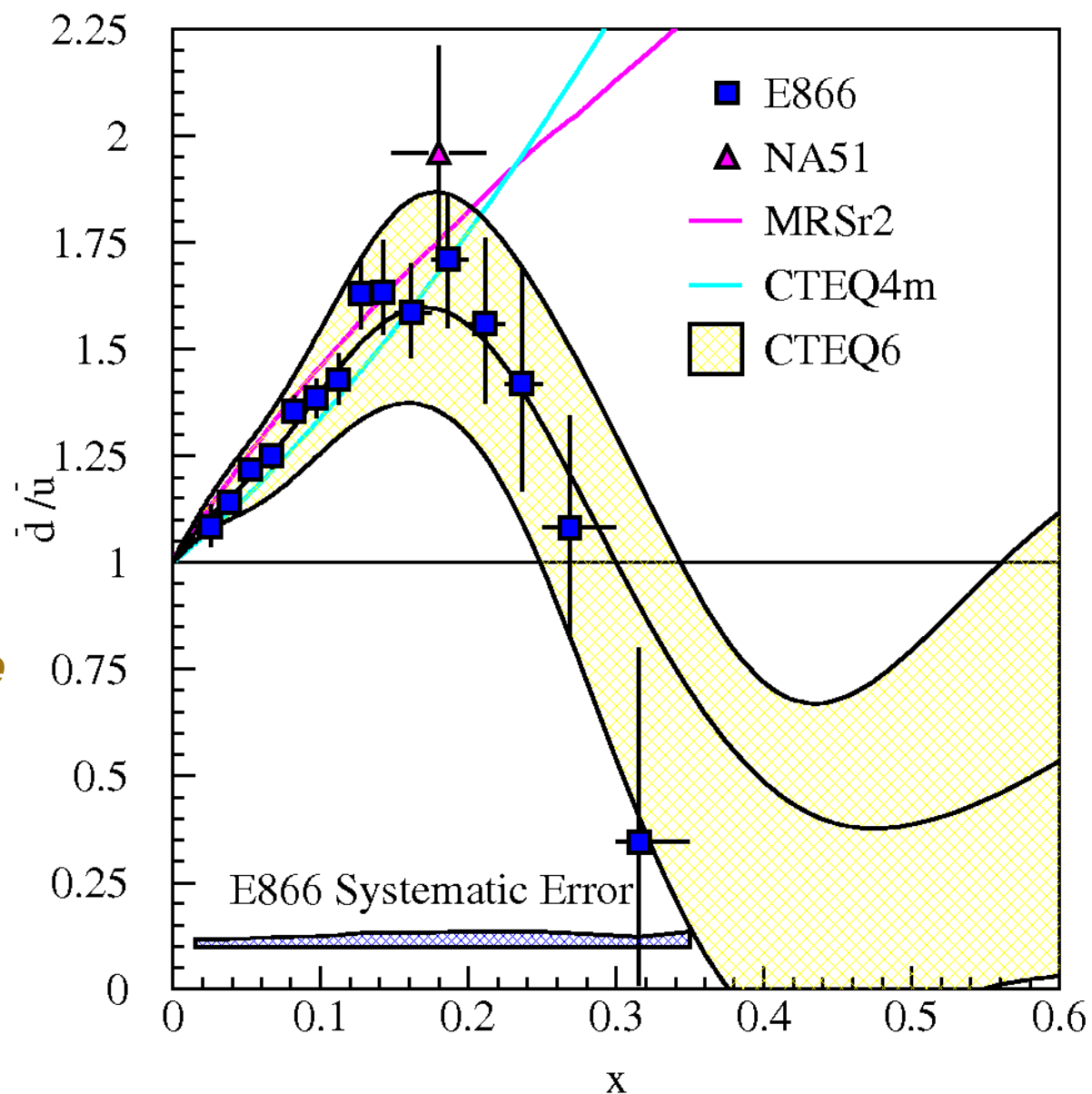
■ E866/NuSea (Drell-Yan)

$$\bar{d}(x) \neq \bar{u}(x)$$

Interactions of quarks at same rapidity in 5-quark Fock state

Intrinsic sea quarks

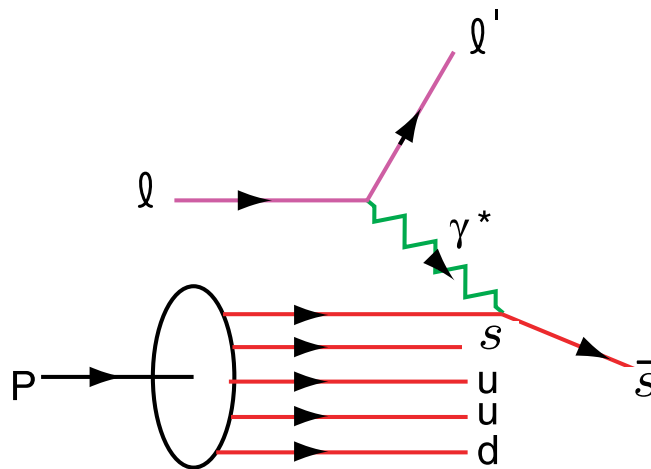
$\bar{d}(x)/\bar{u}(x)$ for $0.015 \leq x \leq 0.35$



Measure strangeness distribution in Semi-Inclusive DIS at JLab

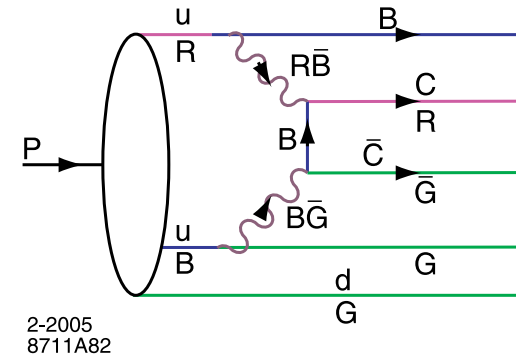
$$\text{Is } s(x) = \bar{s}(x)?$$

- **Non-symmetric strange and antistrange sea?**
- **Non-perturbative physics; e.g** $|uuds\bar{s}\rangle \simeq |\Lambda(uds)K^+(\bar{s}u)\rangle$
- **Important for interpreting NuTeV anomaly** **B. Q. Ma, sjb**



Tag struck quark flavor in semi-inclusive DIS $ep \rightarrow e' K^+ X$

Intrinsic Heavy-Quark Fock States

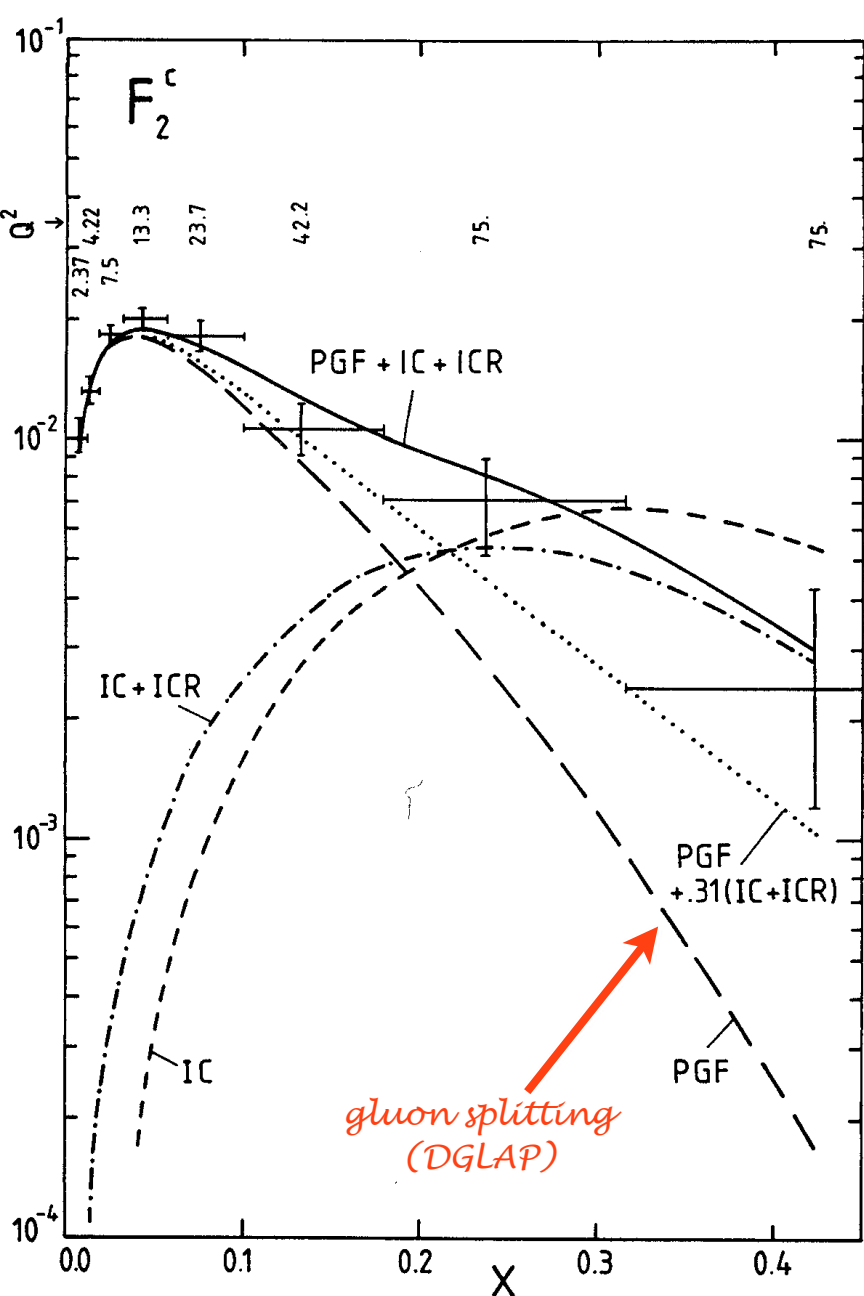


- Rigorous prediction of QCD, OPE
- Color-Octet Color-Octet Fock State!
- Probability $P_{Q\bar{Q}} \propto \frac{1}{M_Q^2}$ $P_{Q\bar{Q}Q\bar{Q}} \sim \alpha_s^2 P_{Q\bar{Q}}$ $P_{c\bar{c}/p} \simeq 1\%$
- Large Effect at high x
- Greatly increases kinematics of colliders such as Higgs production at high x_F (Kopeliovich, Schmidt, Soffer, Goldhaber, sjb)
- Severely underestimated in conventional parameterizations of heavy quark distributions (Pumplin, Tung)
- Many empirical tests (Gardener, Karliner, ..)

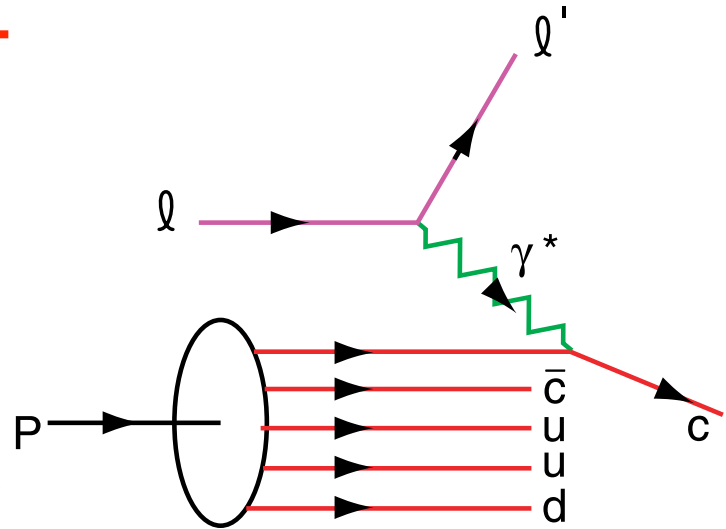
Measurement of Charm Structure Function

J. J. Aubert et al. [European Muon Collaboration], "Production Of Charmed Particles In 250-GeV Mu+ - Iron Interactions," Nucl. Phys. B 213, 31 (1983).

First Evidence for Intrinsic Charm Hoyer, Peterson, Sakai, sjb



factor of 30!

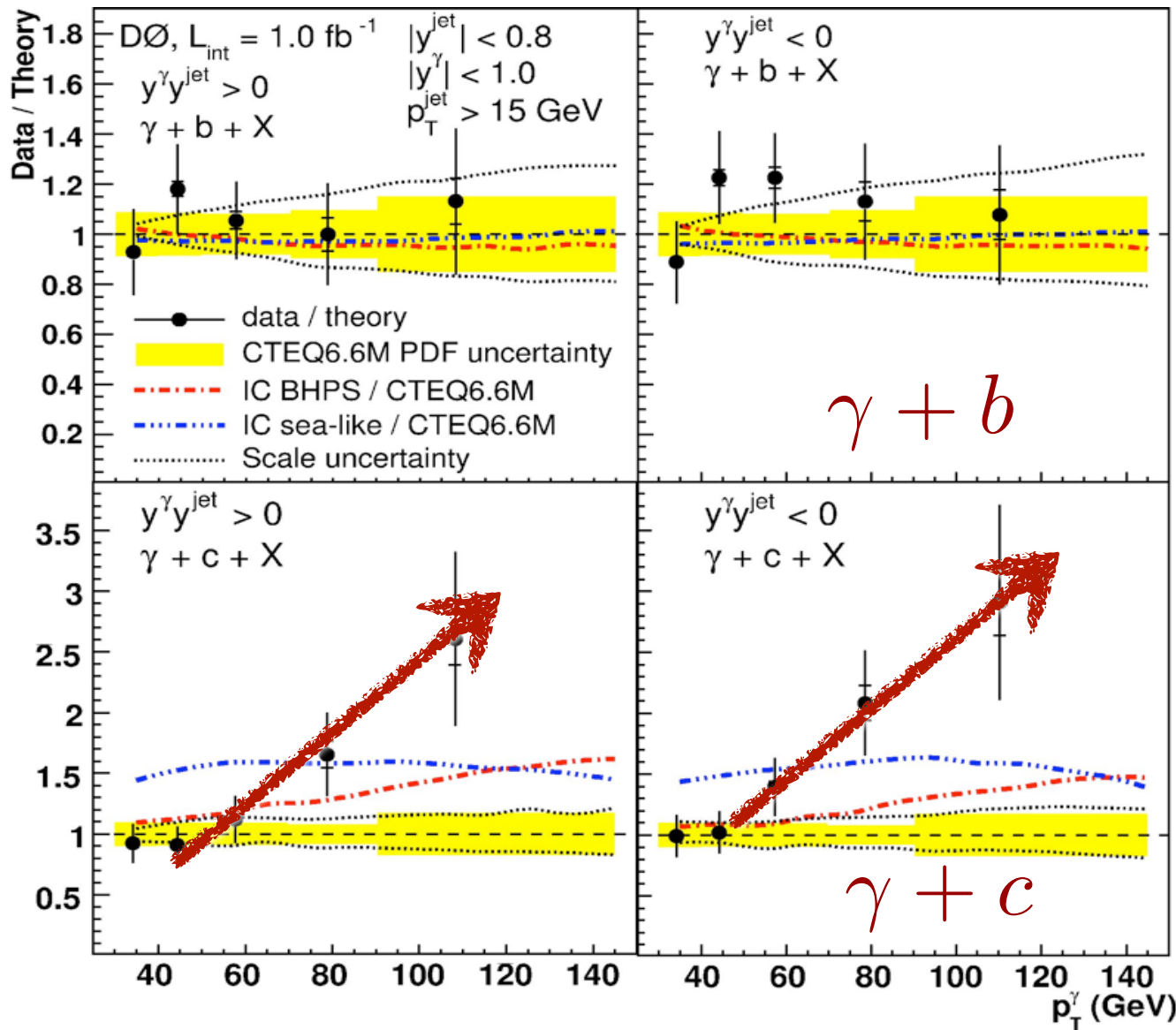


DGLAP / Photon-Gluon Fusion: factor of 30 too small

Two Components (separate evolution):

$$c(x, Q^2) = c(x, Q^2)_{\text{extrinsic}} + c(x, Q^2)_{\text{intrinsic}}$$

Measurement of $\gamma + b + X$ and $\gamma + c + X$ Production Cross Sections
in $p\bar{p}$ Collisions at $\sqrt{s} = 1.96$ TeV



$$\frac{\Delta\sigma(\bar{p}p \rightarrow \gamma c X)}{\Delta\sigma(\bar{p}p \rightarrow \gamma b X)}$$

Ratio
insensitive to
gluon PDF,
scales

Signal for
significant IC
at $x > 0.1$

Need COMPASS
Measurement
of $c(x, Q^2)$!

Do heavy quarks exist in the proton at high x ?

Conventional wisdom: impossible!

***Standard Assumption: Heavy quarks are generated
via DGLAP evolution
from gluon splitting***

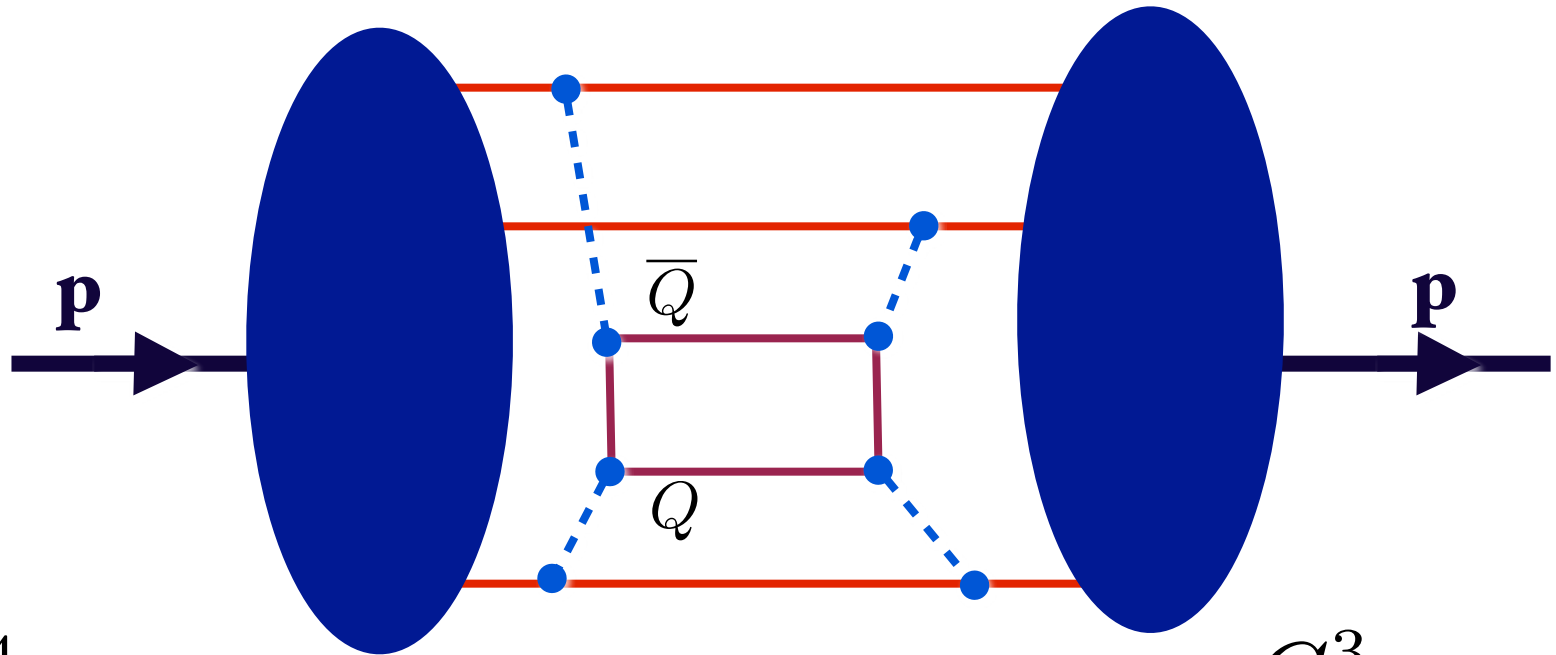
$$s(x, \mu_F^2) = c(x, \mu_F^2) = b(x, \mu_F^2) \equiv 0$$

at starting scale μ_F^2

Conventional wisdom is wrong even in QED!

Proton Self Energy from g g to gg scattering
QCD predicts Intrinsic Heavy Quarks!

$$x_Q \propto (m_Q^2 + k_{\perp}^2)^{1/2}$$



$$\frac{F_{\mu\nu}^4}{M_{\ell}^2}$$

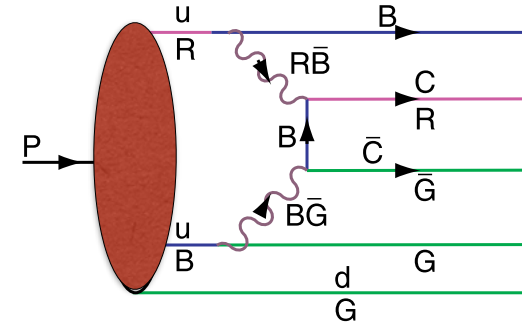
Probability (QED) $\propto \frac{1}{M_{\ell}^4}$

$$\frac{G_{\mu\nu}^3}{M_Q^2}$$

Probability (QCD) $\propto \frac{1}{M_Q^2}$

Collins, Ellis, Gunion, Mueller, sjb
M. Polyakov, et al.

Intrinsic Heavy-Quark Fock



- **Rigorous prediction of QCD, OPE**

- **Color-Octet Color-Octet Fock State**

- **Probability** $P_{Q\bar{Q}} \propto \frac{1}{M_Q^2}$ $P_{Q\bar{Q}Q\bar{Q}} \sim \alpha_s^2 P_{Q\bar{Q}}$ $P_{c\bar{c}/p} \simeq 1\%$

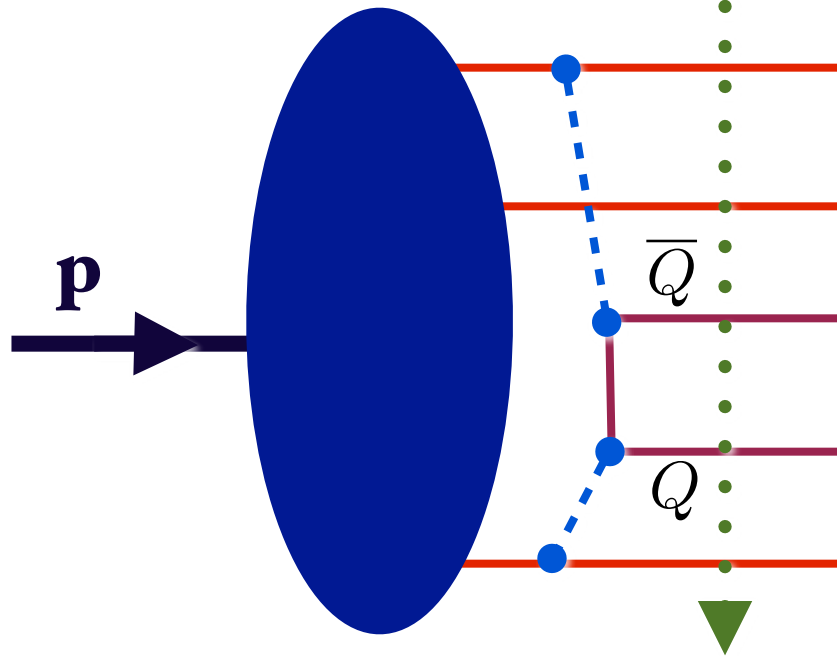
- **Large Effect at high x**

- **Greatly increases kinematics of colliders such as Higgs production (Kopeliovich, Schmidt, Soffer, sjb)**

- **Underestimated in conventional parameterizations of heavy quark distributions (Pumplin, Tung)**

Fixed LF time

*Proton 5-quark Fock State:
Intrinsic Heavy Quarks*



*QCD predicts
Intrinsic Heavy
Quarks at high x*

**Minimal off-
shellness**

$$x_Q \propto (m_Q^2 + k_{\perp}^2)^{1/2}$$

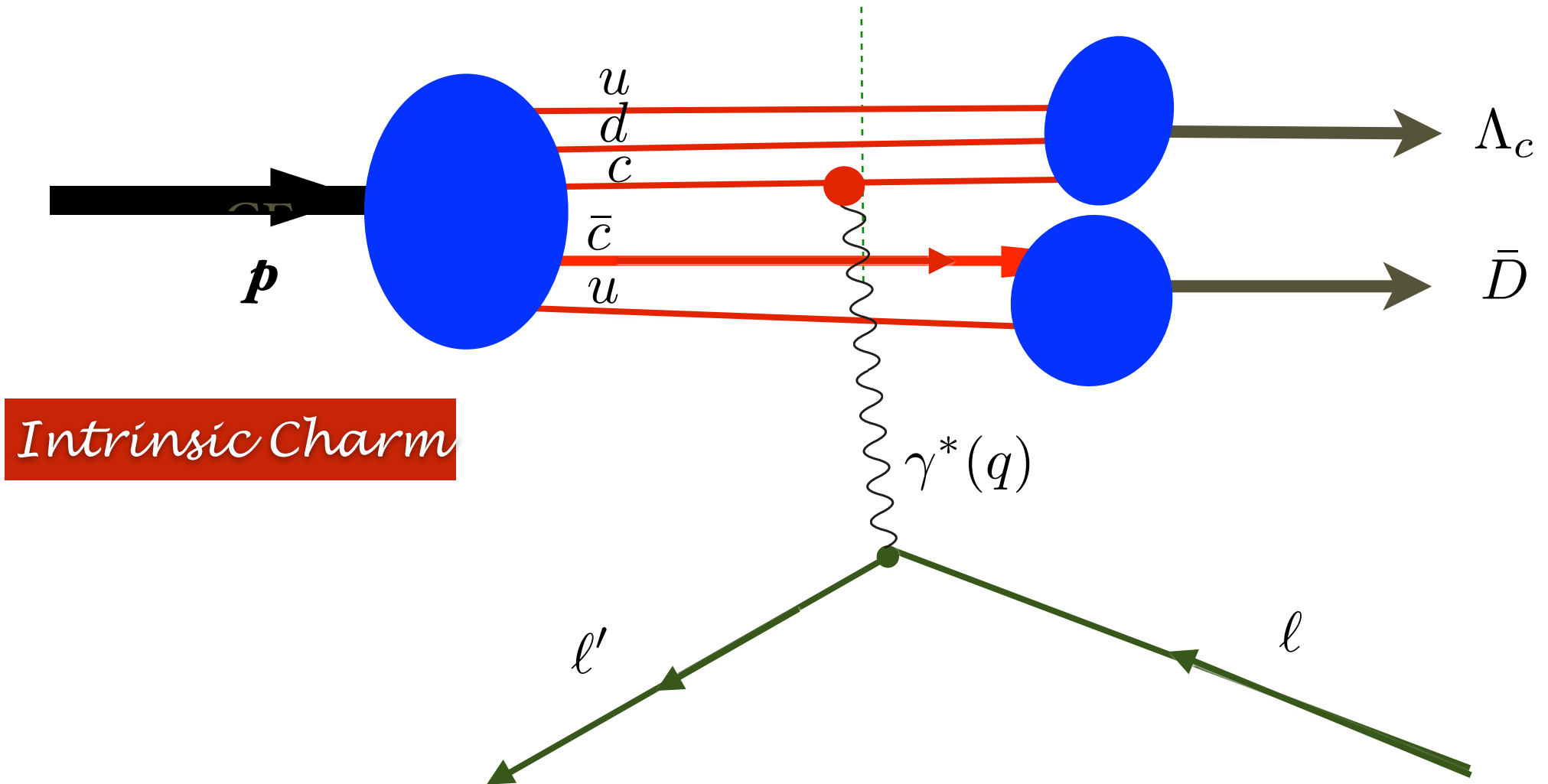
$$\text{Probability (QED)} \propto \frac{1}{M_{\ell}^4}$$

$$\text{Probability (QCD)} \propto \frac{1}{M_Q^2}$$

**Collins, Ellis, Gunion, Mueller, sjb
M. Polyakov**

Light-Front Wavefunctions and Heavy-Quark Electroproduction

Fixed $\tau = t + z/c$



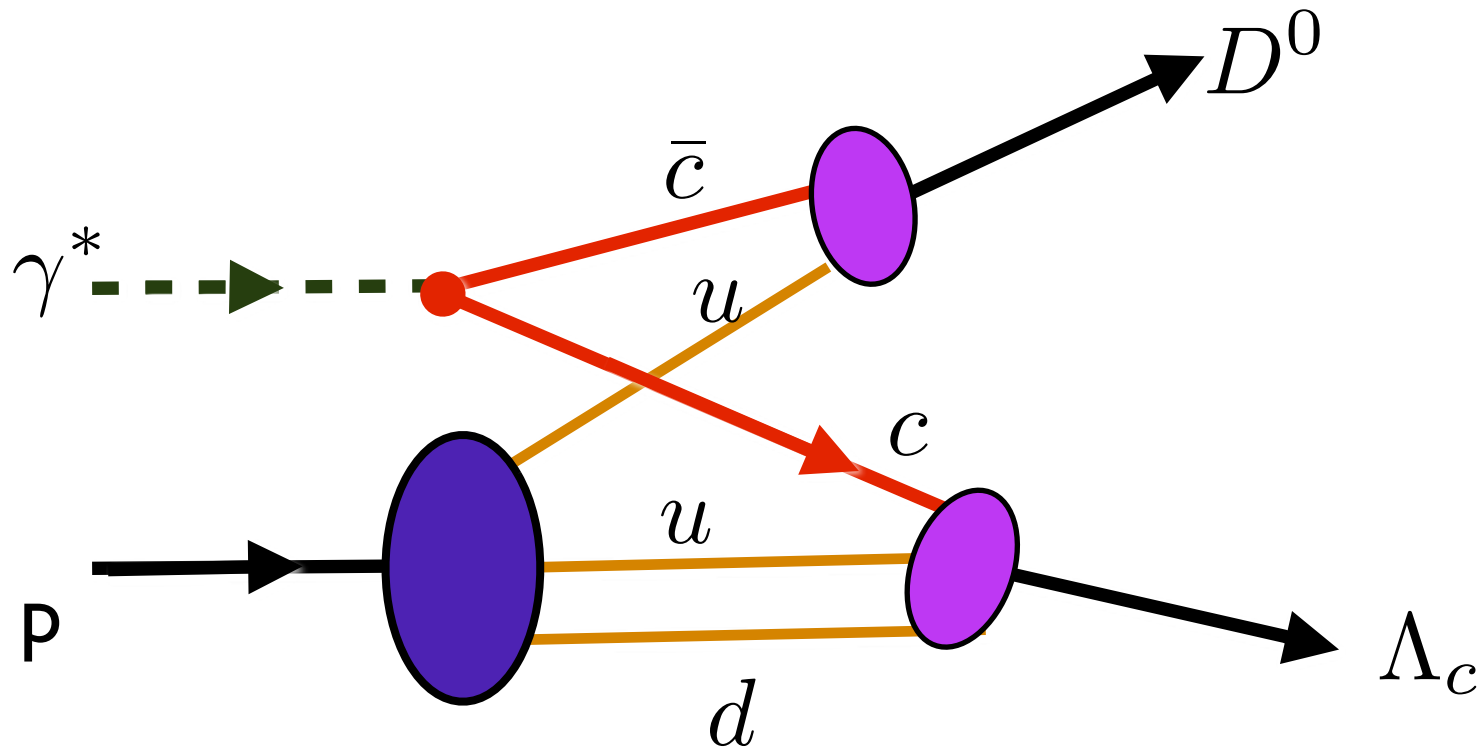
Threshold Production at JLab!

Coalescence of comovers produces $|F\rangle = |\Lambda_c \bar{D}\rangle$ Final State

Charm Produced in Target-Rapidity Domain

Open Charm Production at Threshold!

JLab 12 GeV: A Charm Factory!

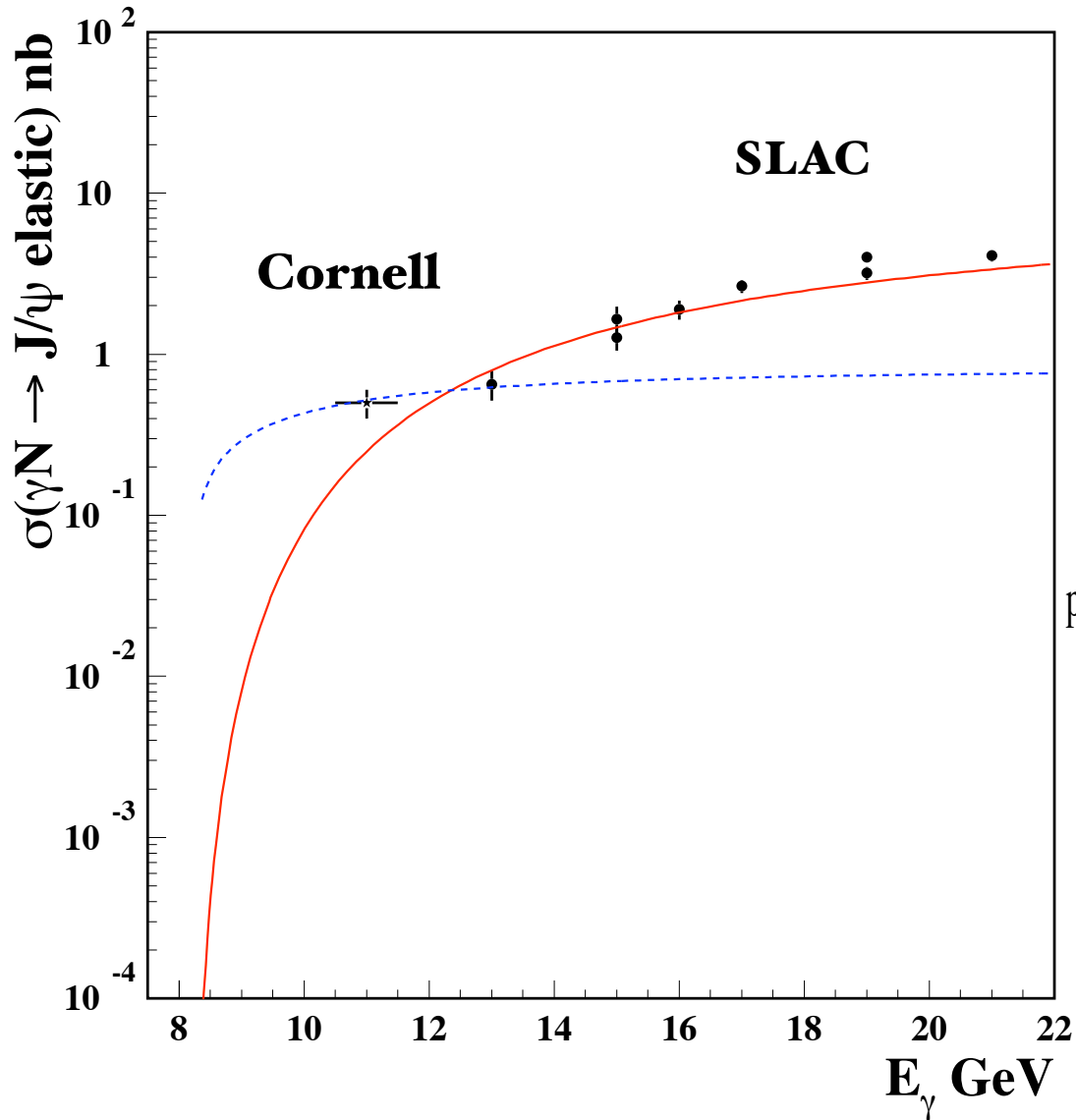


$$\gamma^* p \rightarrow \bar{D}^0 (\bar{c}u) \Lambda_c (cud)$$

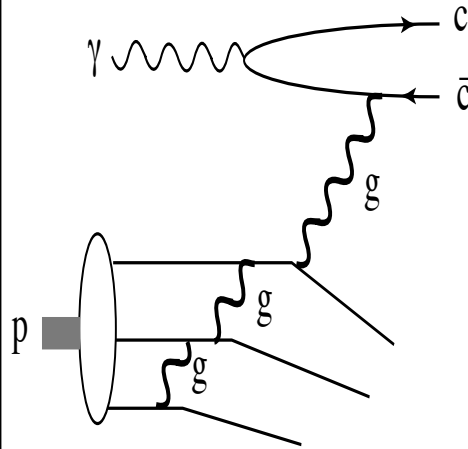
c and u quark interchange

$$\gamma p \rightarrow J/\psi p$$

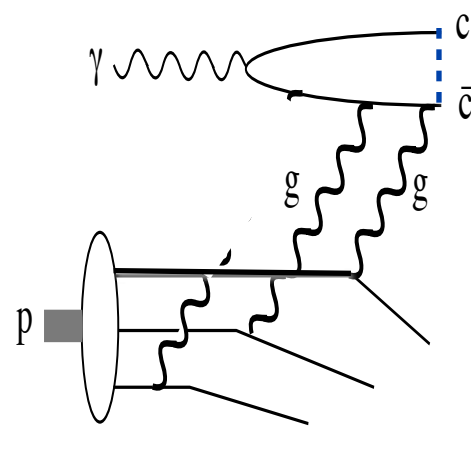
Chudakov, Hoyer, Laget, sjb



cross section: 1 nb



Leading twist contribution



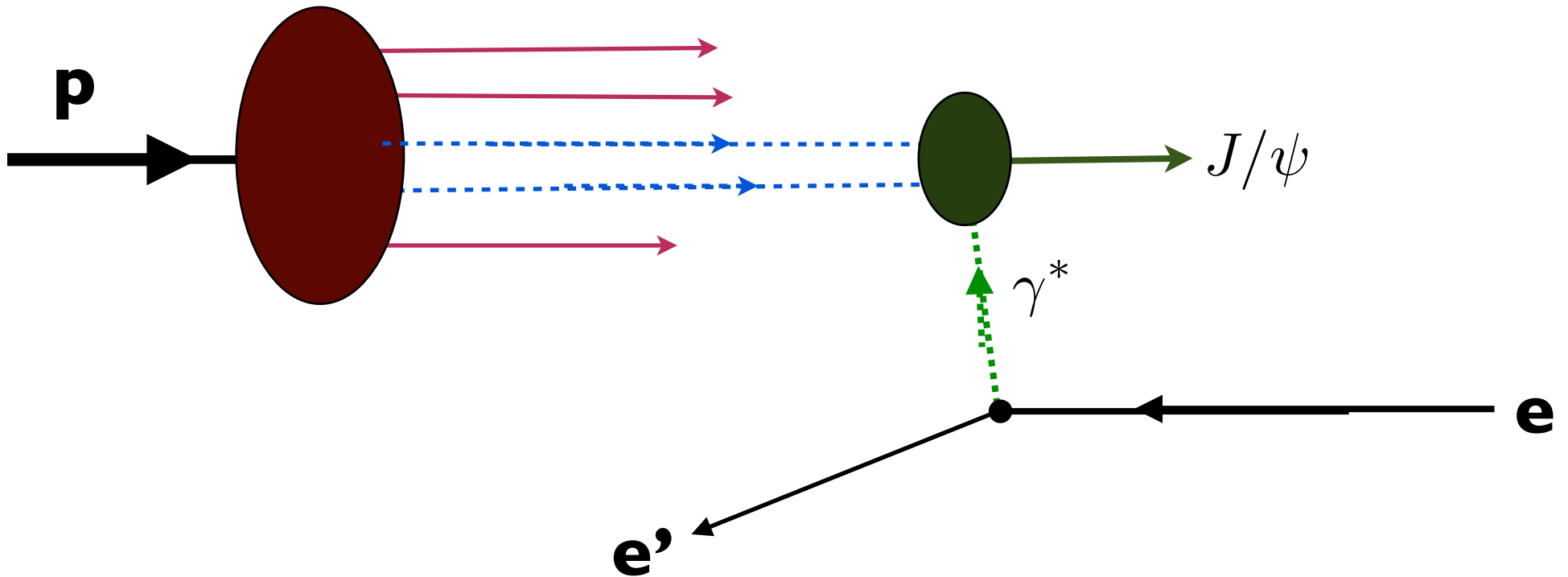
Dominant near threshold

Phase space factor β cancelled by gluonic final-state interactions

Sommerfeld-Schwinger-Sakharov Effect

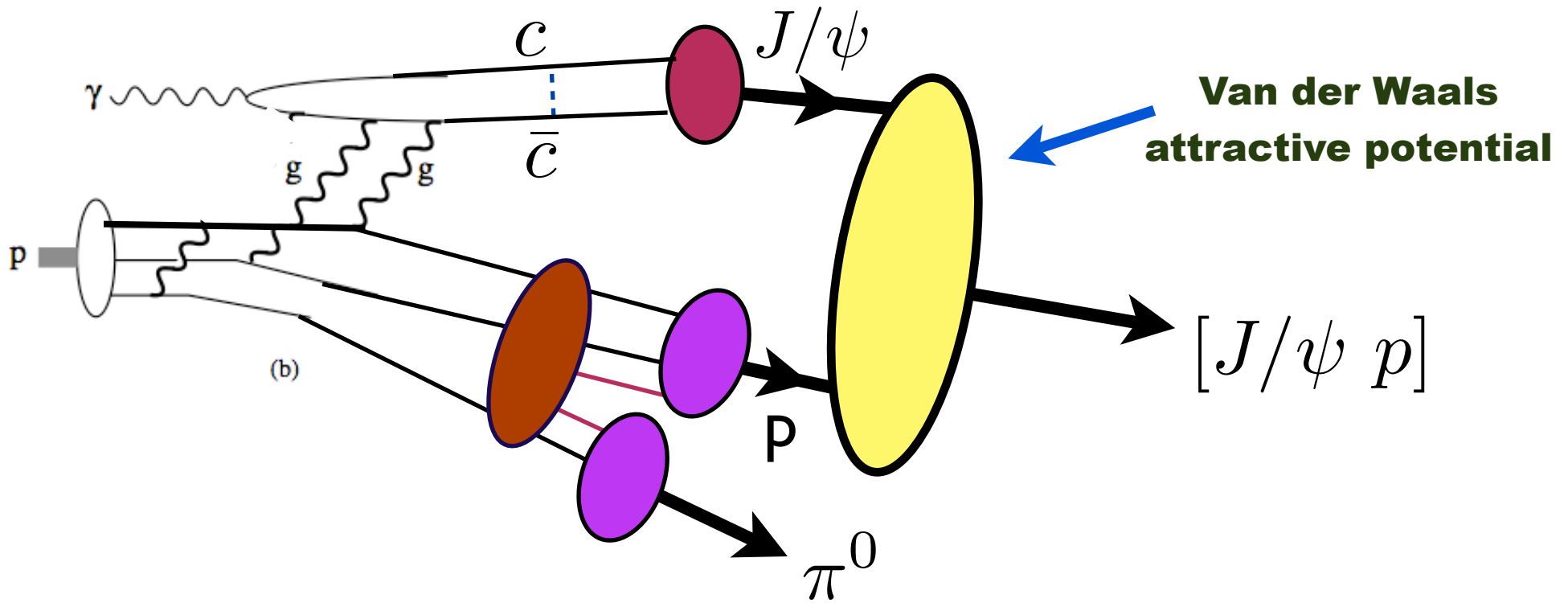
$$\gamma^* p \rightarrow J/\psi X$$

$$(gg)_{1C} + \gamma^* \rightarrow J/\psi$$



***Digluon-initiated subprocess
in ep and γp collisions***

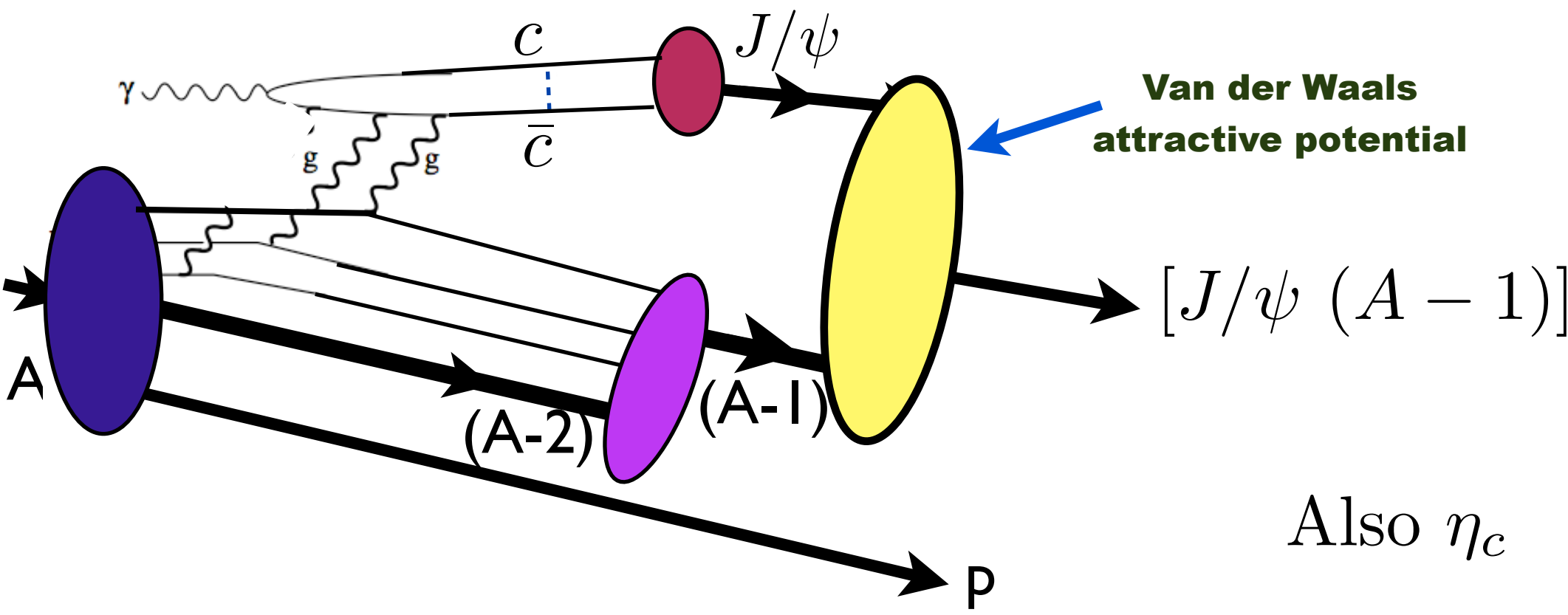
Charmonium Production at Threshold



$$\gamma p \rightarrow [J/\psi p] \pi^0 \quad \gamma p \rightarrow [J/\psi n] \pi^+$$

Form proton-charmonium bound state! $|uudc\bar{c}\rangle$

Charmonium Production on Nuclei at Threshold



$$\gamma A \rightarrow [J/\psi (A-1)] p$$

Also η_c

Form "nuclear-bound" charmonium bound-states!

JLab 12 GeV: An Exotic Charm Factory!

$\gamma^* p \rightarrow J/\psi + p$ threshold
at $\sqrt{s} \simeq 4$ GeV, $E_{\text{lab}}^{\gamma^*} \simeq 7.5$ GeV.

$\gamma^* p \rightarrow X(3872) + p'$
 $|c\bar{c}q\bar{q}\rangle$ *tetraquark*

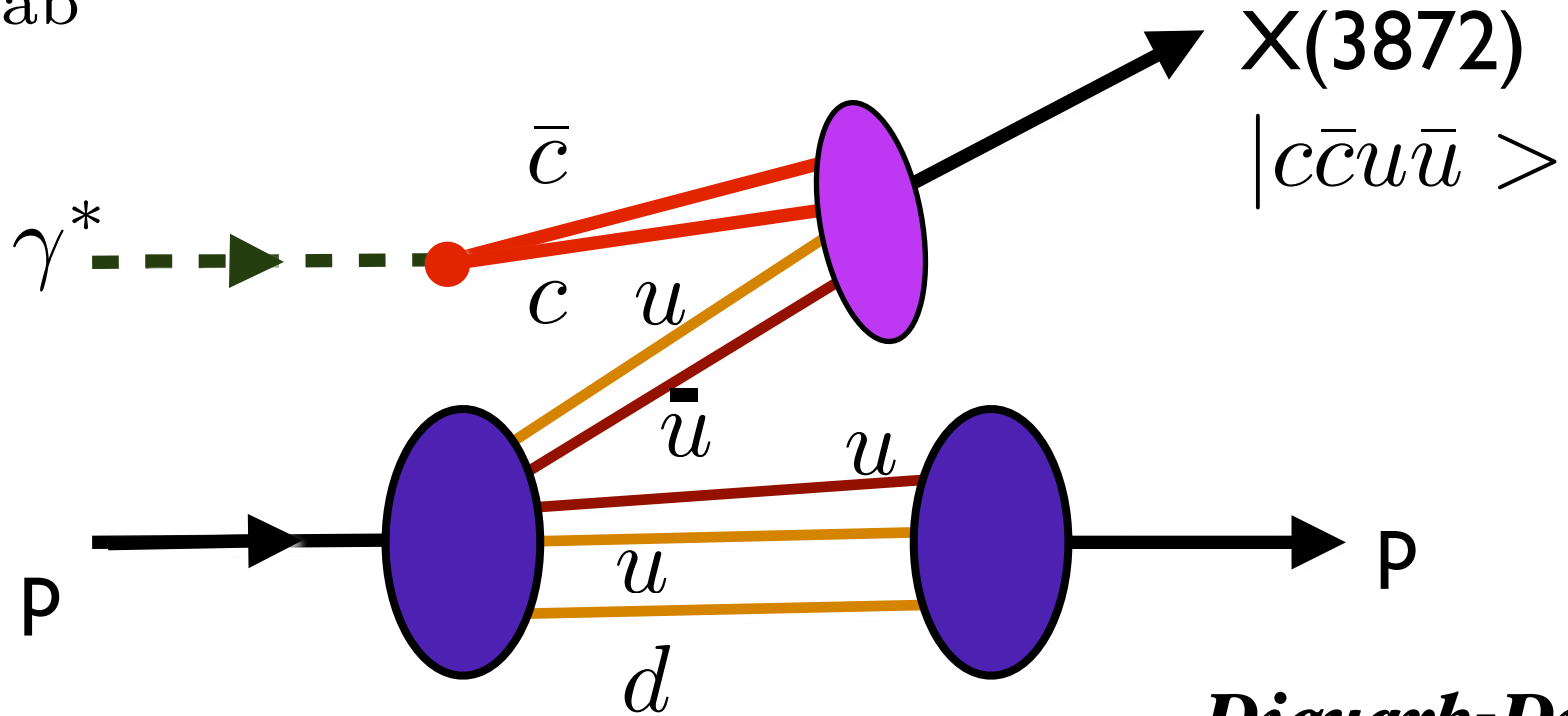
Produce $[J/\psi + p]$ bound state
 $|uudc\bar{c}\rangle$ *pentaquark*

$\gamma^* d \rightarrow J/\psi + d$ threshold
at $\sqrt{s} \simeq 5$ GeV, $E_{\text{lab}}^{\gamma^*} \simeq 6$ GeV.

Produce $[J/\psi + d]$ nuclear-bound quarkonium state
 $|uudduc\bar{c}\rangle$ *octoquark!*

Tetraquark Production at Threshold

$$E_{\text{lab}}^{\gamma} > 11.9 \text{ GeV}$$



$$X(3872)$$

$$|c\bar{c}u\bar{u}\rangle$$

***Diquark-Diquark
vs Molecular State?***

$$\gamma^* p \rightarrow X(3872) + p'$$

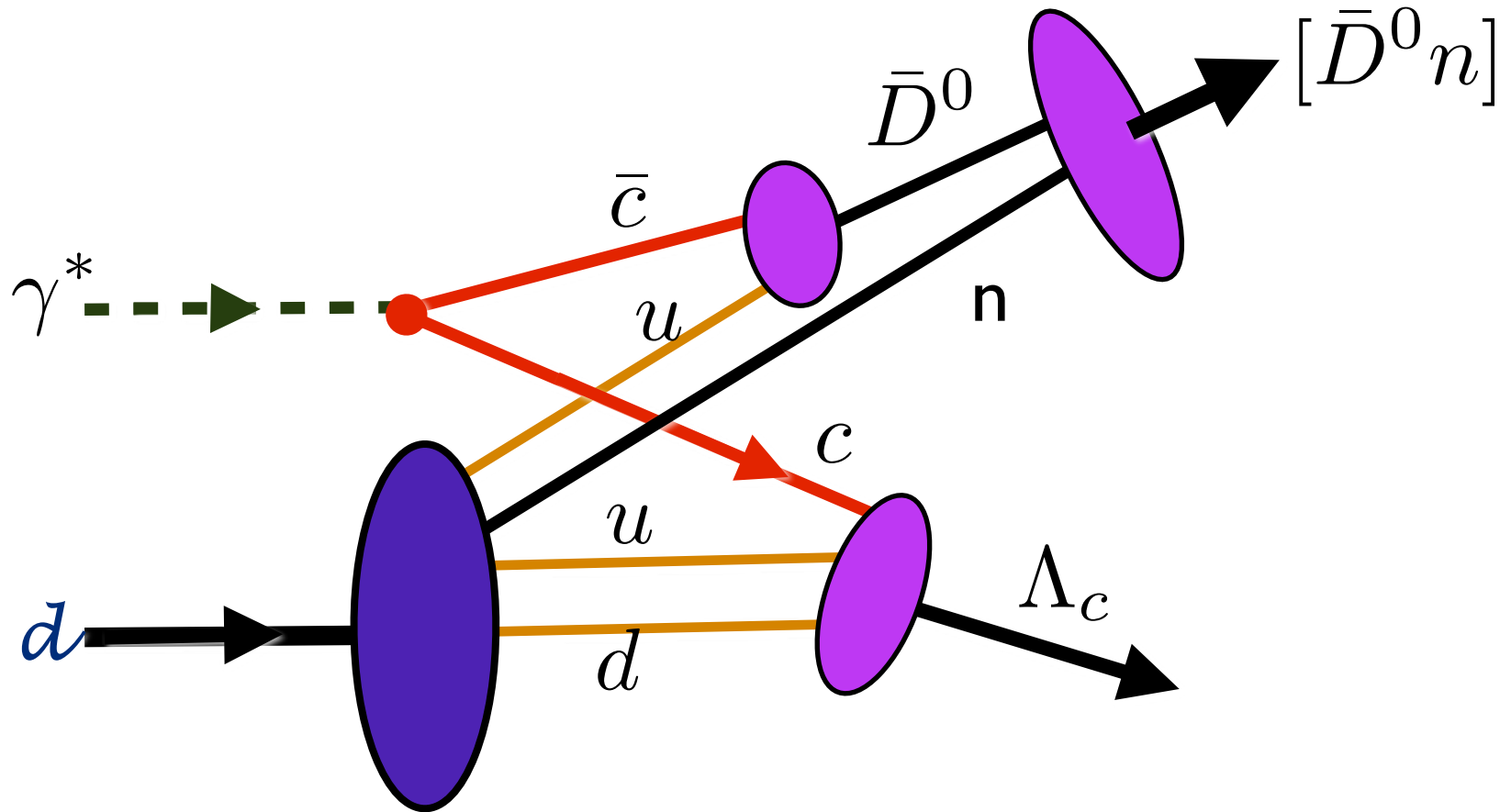
$$|c\bar{c}q\bar{q}\rangle$$

***New approach
to hadronic decays***

Dominance of Ψ' vs J/Ψ decays

Lebed, Hwang, sjb

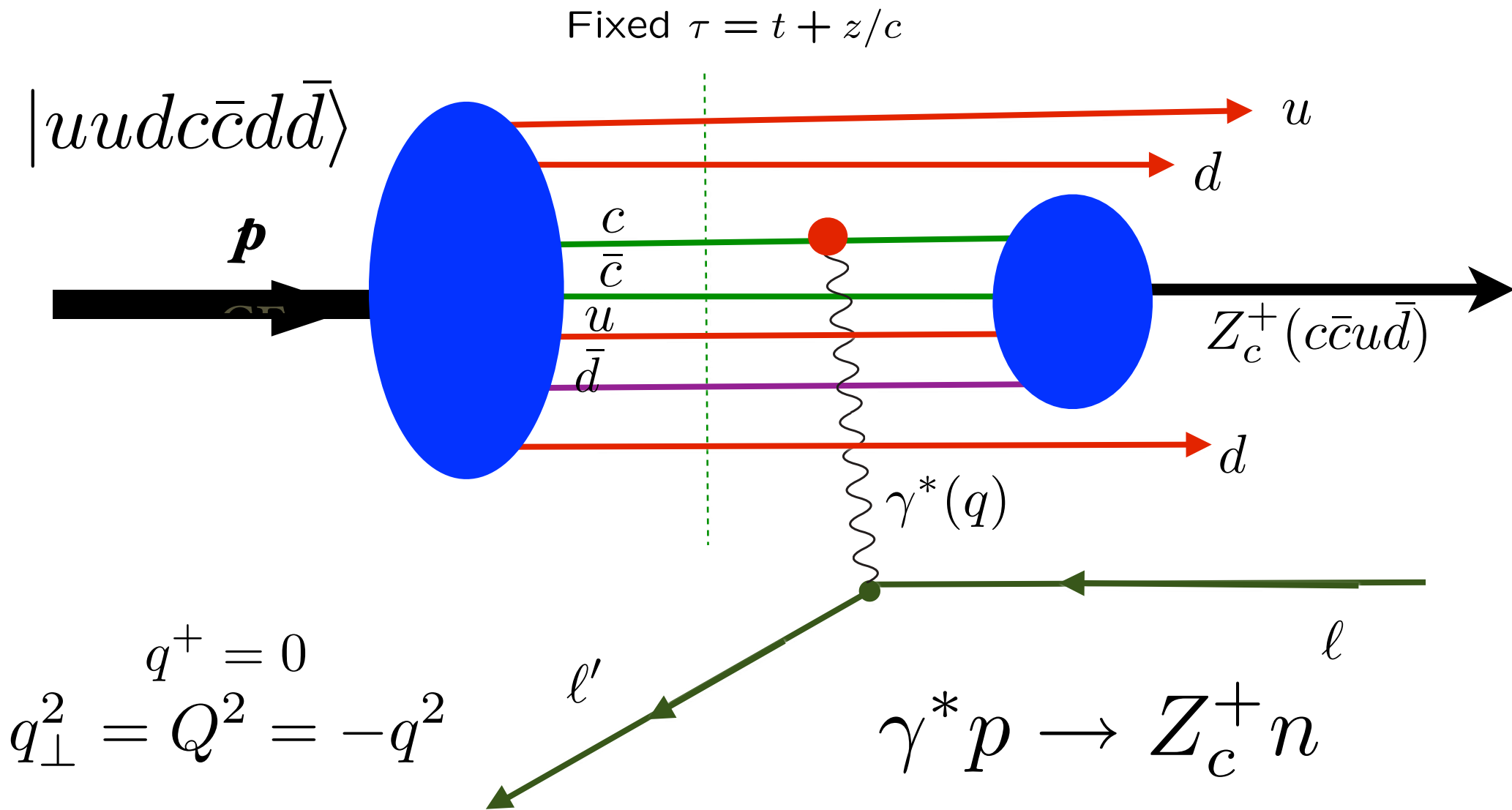
Open Charm Production at Threshold



$$\gamma^* d \rightarrow \Lambda_c + [\bar{D}^0 (\bar{c}u)n] (\bar{c}uudd)$$

Create pentaquark on deuteron at low relative velocity

Light-Front Wavefunctions and Heavy-Quark Electroproduction

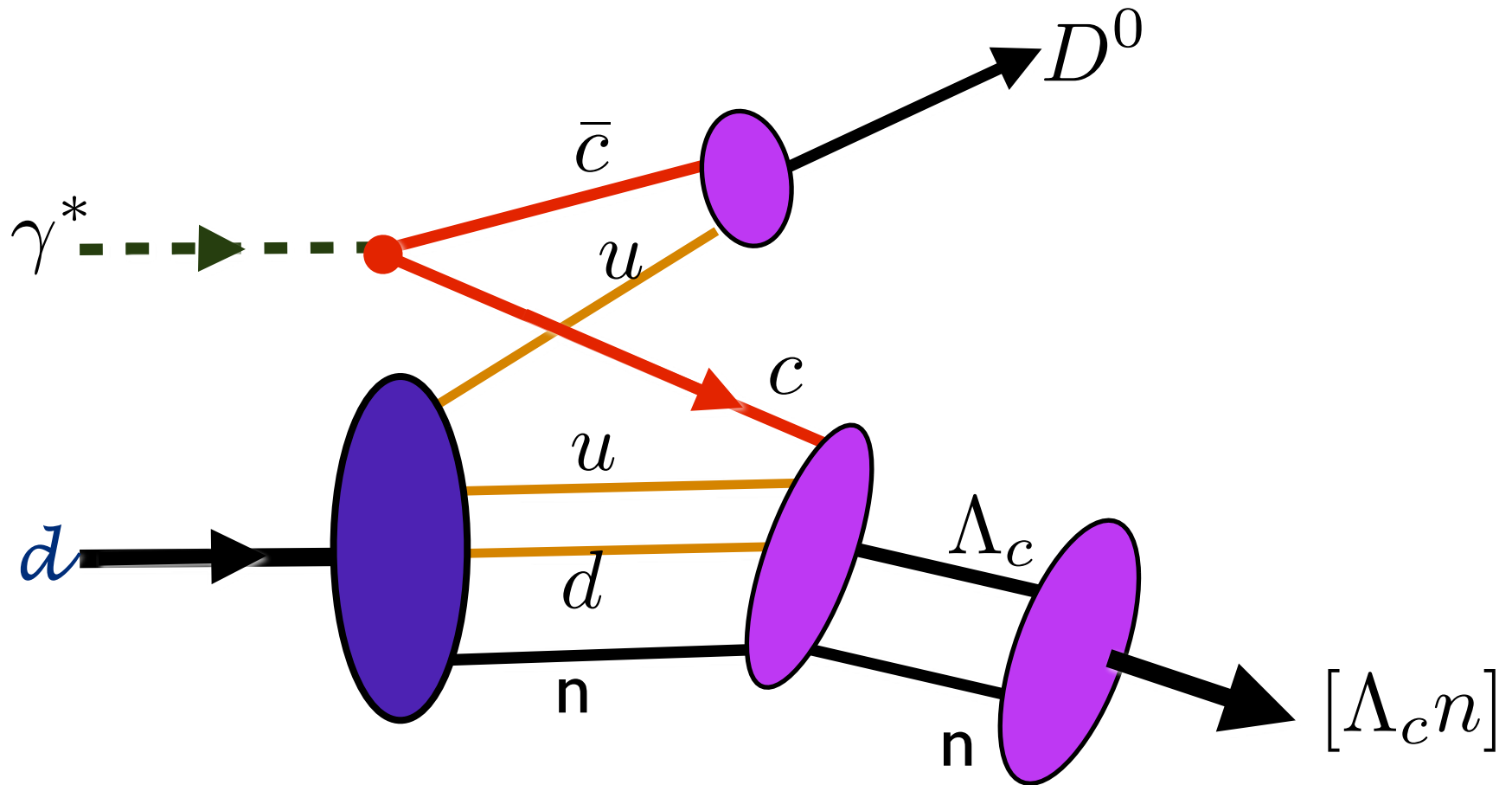


Produce Charged Tetraquarks at JLab!

Coalescence of comovers at threshold produces Z_c^+ tetraquark resonance

Open Charm Production at Threshold

Nuclear binding at low relative velocity



$$\gamma^* d \rightarrow \bar{D}^0 (\bar{c}u) [\Lambda_c n] (cududd)$$

Possible charmed $B=2$ nucleus

Produce Charge $Q=4, I=3, B=2$ Hidden-Color Dibaryon State at JLab

- First suggested by F. Dyson and N-H Xuong (1964)

“Hexaquark”

$$[B = 2, Q = +4] \leftrightarrow |u_R^\uparrow u_B^\uparrow u_Y^\uparrow u_R^\downarrow u_B^\downarrow u_Y^\downarrow \rangle$$

- Hidden-Color Six-Quark Configuration
- Decays to $\Delta^{++}\Delta^{++}$

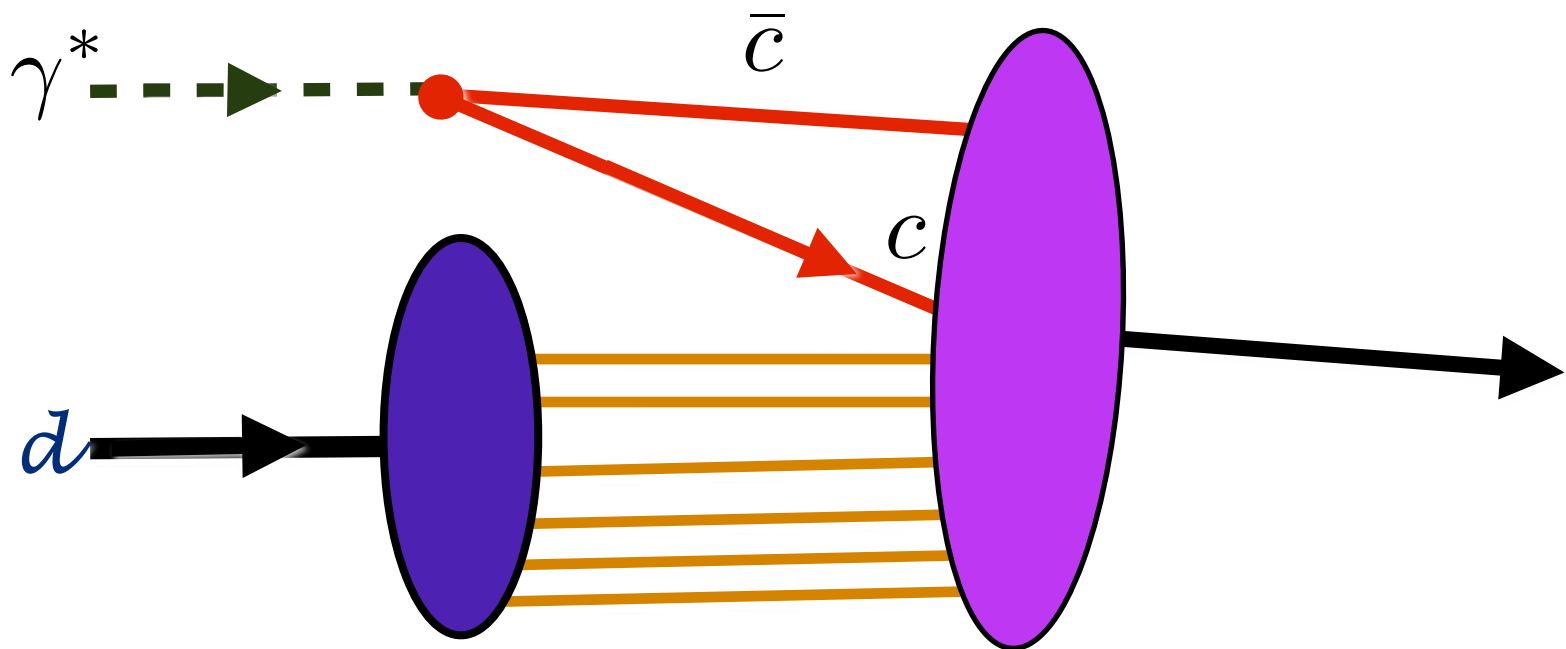
$$\gamma d \rightarrow [B = +2, Q = +4] \pi^- \pi^- \pi^-$$

Discover at JLab!

Bashkanov, Clement, sjb

Octoquark Production at Threshold

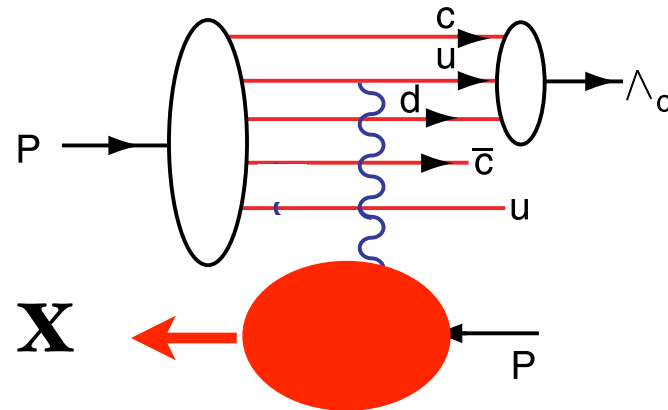
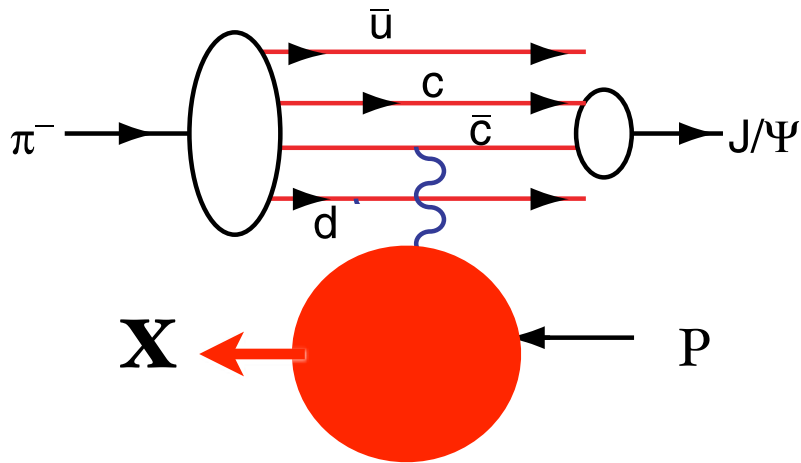
$$M_{\text{octoquark}} \sim 5 \text{ GeV}$$



$$\gamma^* D \rightarrow |uud udc\bar{c}\rangle$$

Explains Krüsch Effect!

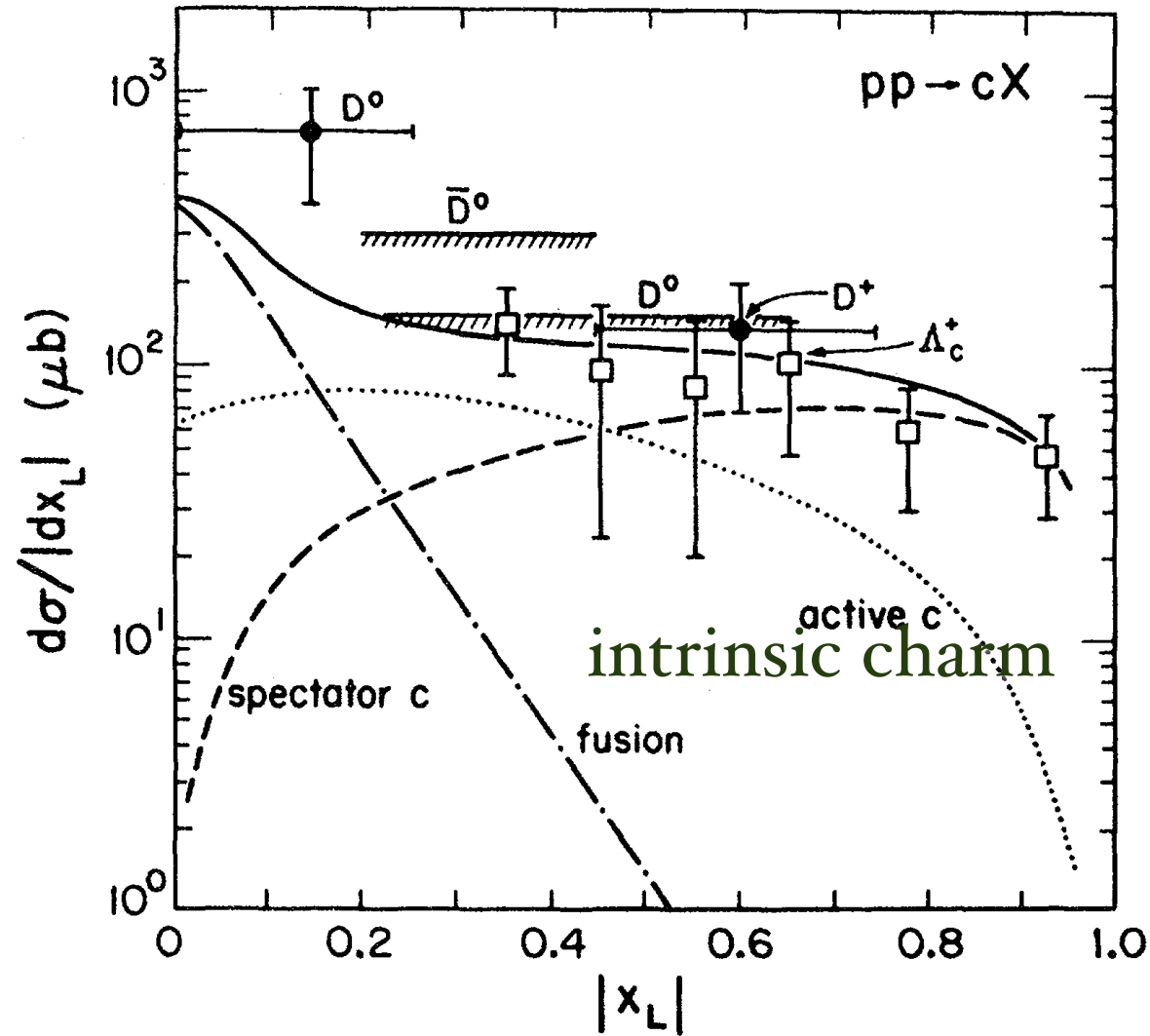
Leading Hadron Production from Intrinsic Charm



Spectator counting rules

$$\frac{dN}{dx_F} \propto (1 - x_F)^{2n_{spect} - 1}$$

Coalescence of Comoving Charm and Valence Quarks
Produce J/ψ , Λ_c and other Charm Hadrons at High x_F



Barger, Halzen, Keung

Evidence for charm at large x

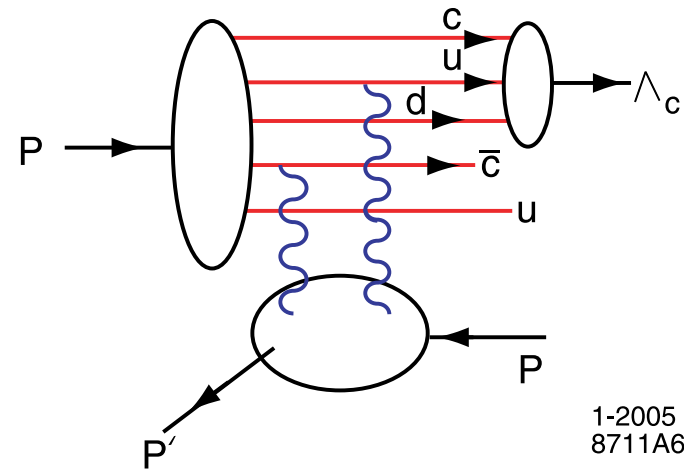
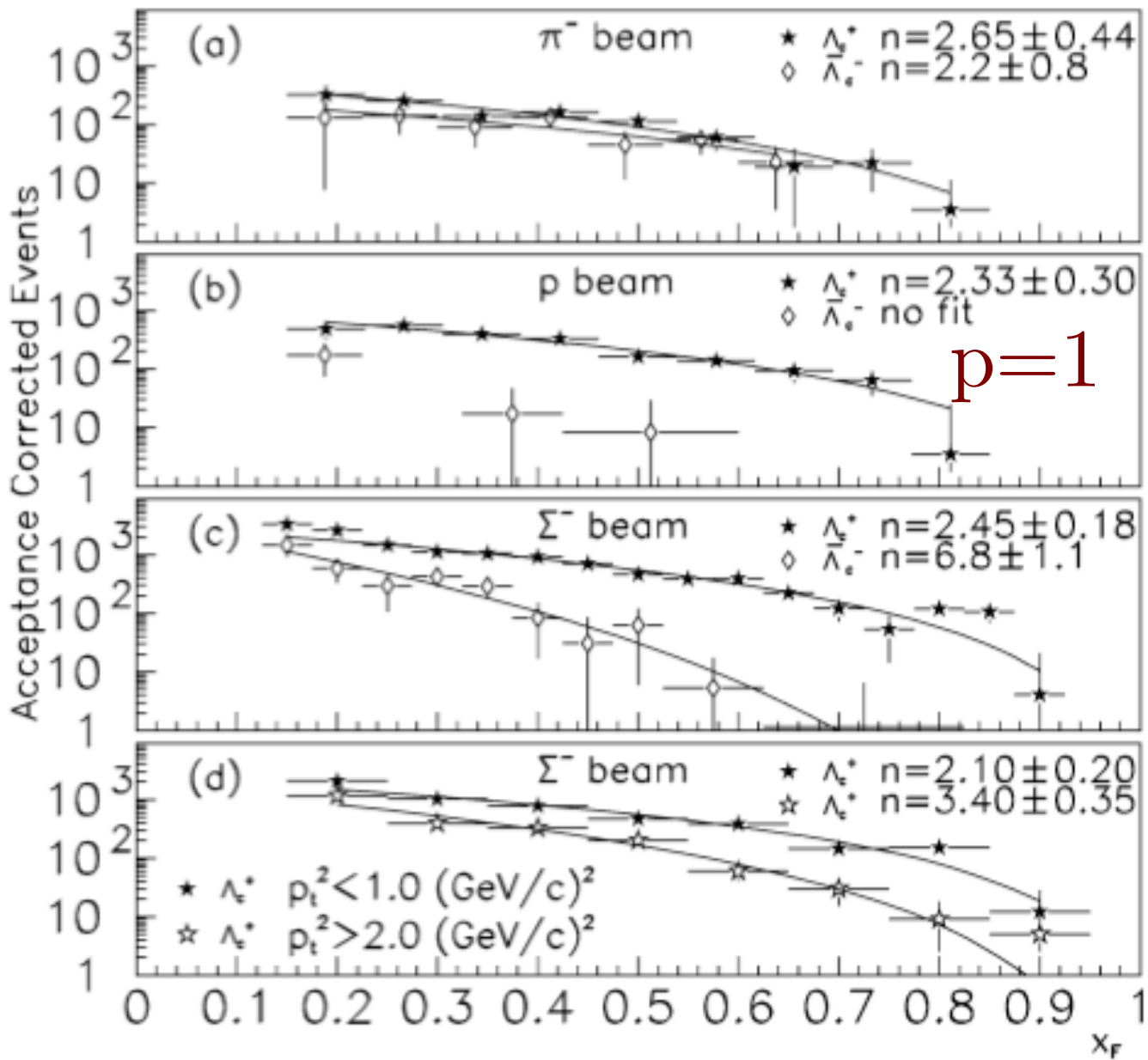
- EMC data: $c(x, Q^2) > 30 \times \text{DGLAP}$
 $Q^2 = 75 \text{ GeV}^2, x = 0.42$
- High x_F $pp \rightarrow J/\psi X$
- High x_F $pp \rightarrow J/\psi J/\psi X$
- High x_F $pp \rightarrow \Lambda_c X$
- High x_F $pp \rightarrow \Lambda_b X$
- High x_F $pp \rightarrow \Xi(ccd)X$ (SELEX)

Critical Measurements at threshold for JLab, PANDA

Interesting spin, charge asymmetry, threshold, spectator effects

Important corrections to B decays; Quarkonium decays

Gardner, Karliner, sjb



$$p(uudc\bar{c}) \rightarrow \Lambda_c(cud)$$

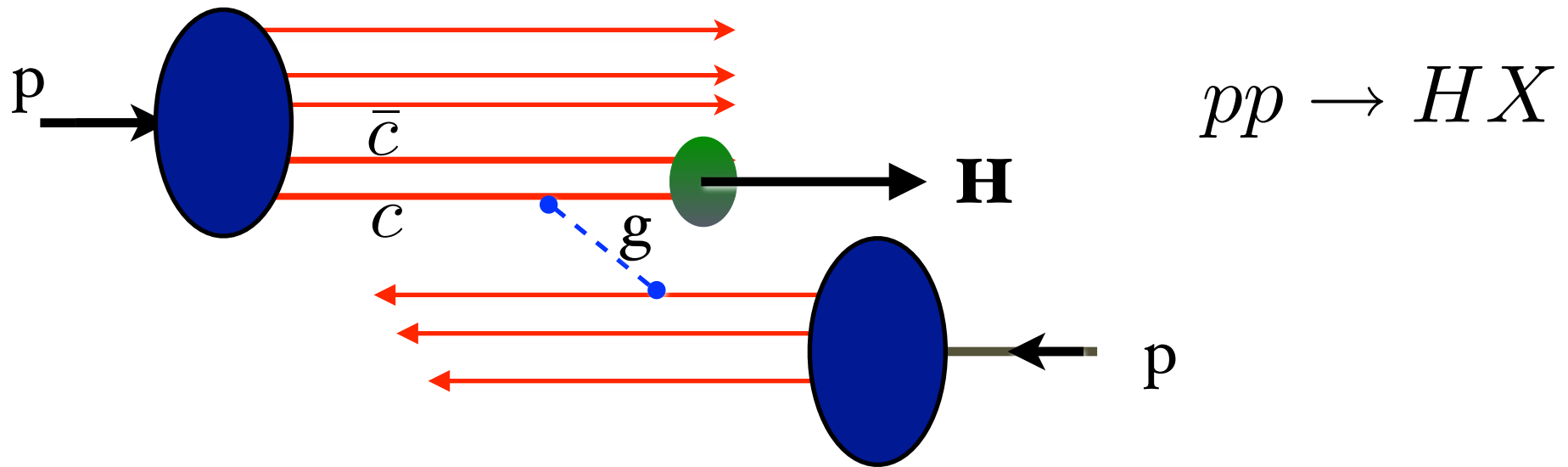
$$n_s = 2$$

**Phase space alone
gives minimum power**

$$(1 - x_F)^p, p = n_s - 1$$

*Maximum fraction
of projectile momentum
carried by charm quarks!*

Intrinsic Charm Mechanism for Inclusive High- X_F Higgs Production



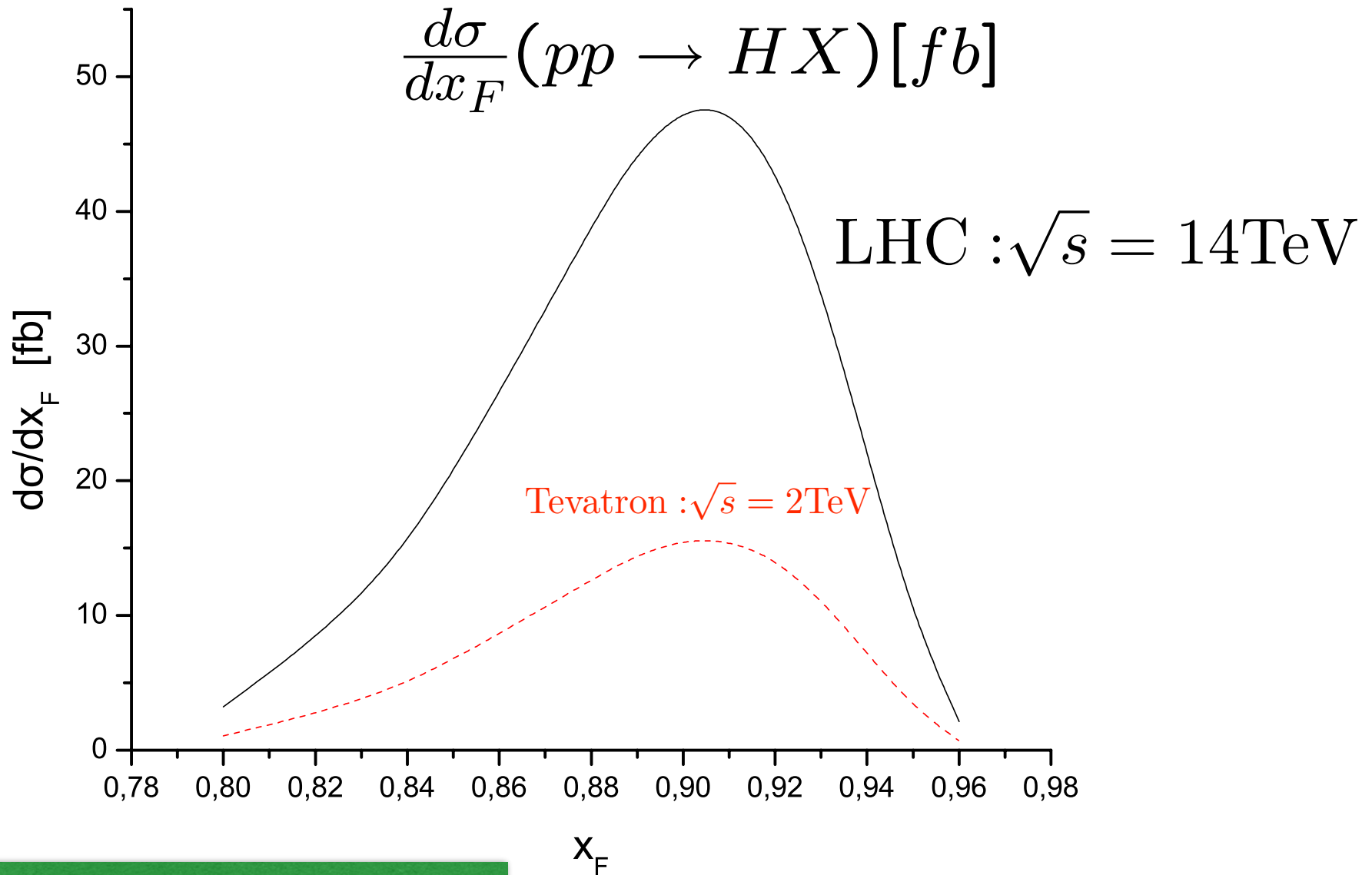
Also: intrinsic bottom, top

**Goldhaber, Soffer,
Kopeliovich, Schmidt, sjb**

Higgs can have 80% of Proton Momentum!

New search strategy for Higgs

AFTER: Higgs production at threshold!



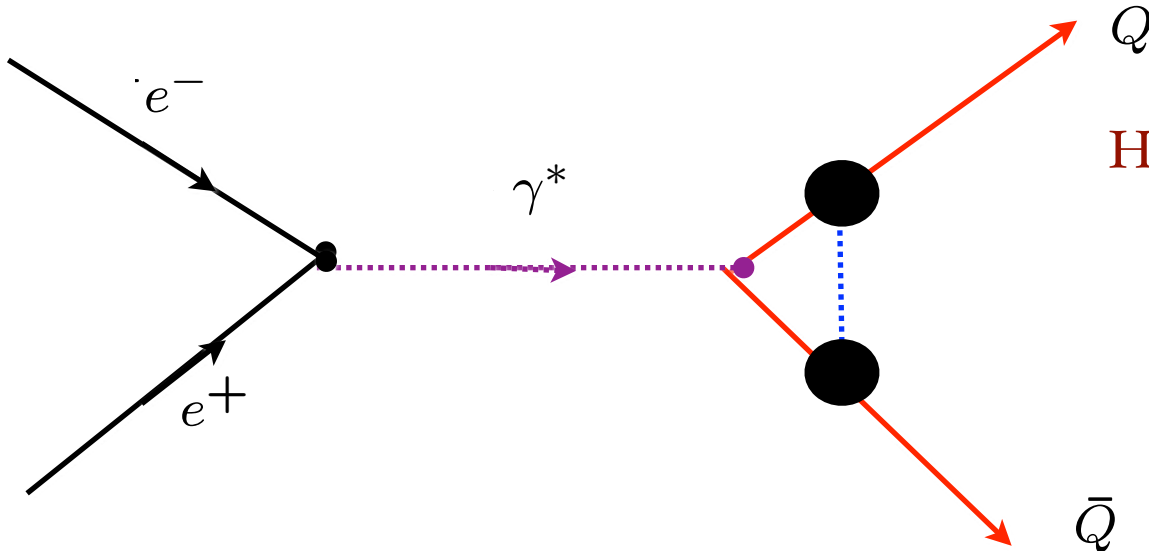
Need High x_F Acceptance

Most practical: Higgs to 2 or 4 muons

**Goldhaber, Kopeliovich,
Schmidt, Soffer, sjb**

Charm at Threshold

- *Intrinsic charm Fock state puts 80% of the proton momentum into the electroproduction process*
- *Γ /velocity enhancement from FSI*
- *CLEO data for quarkonium production at threshold*
- *Krisch effect shows $B=2$ resonance*
- *all particles produced at small relative rapidity-- resonance production*
- *Many exotic hidden and open charm resonances will be produced at JLab (12 GeV)*



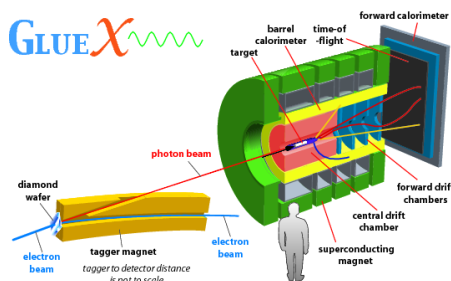
Hoang, Kuhn, Teubner, sjb

$$F_1 + F_2 = \left[1 - 2 \frac{\alpha_s (s e^{3/4} / 4)}{\pi} \right] \times \left[1 + \frac{\pi \alpha_s (s v^2)}{4v} \right]$$

Angular distributions of massive quarks close to threshold.

Example of Multiple BLM/PMC Scales

QCD coupling at small scales at low relative velocity v



Novel Nuclear
Photo- and Electroproduction Physics

Stan Brodsky

JLab, April 29, 2016

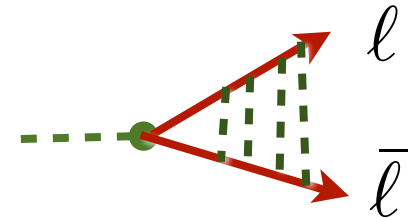
Coulomb Enhancement of Pair Production at Threshold

$$\sigma \rightarrow \sigma S(\beta)$$

$$\beta = \sqrt{1 - \frac{4m_\ell^2}{s}}$$

$$X(\beta) = \frac{\pi\alpha\sqrt{1-\beta^2}}{\beta}$$

$$S(\beta) = \frac{X(\beta)}{1 - e^{-X(\beta)}}$$

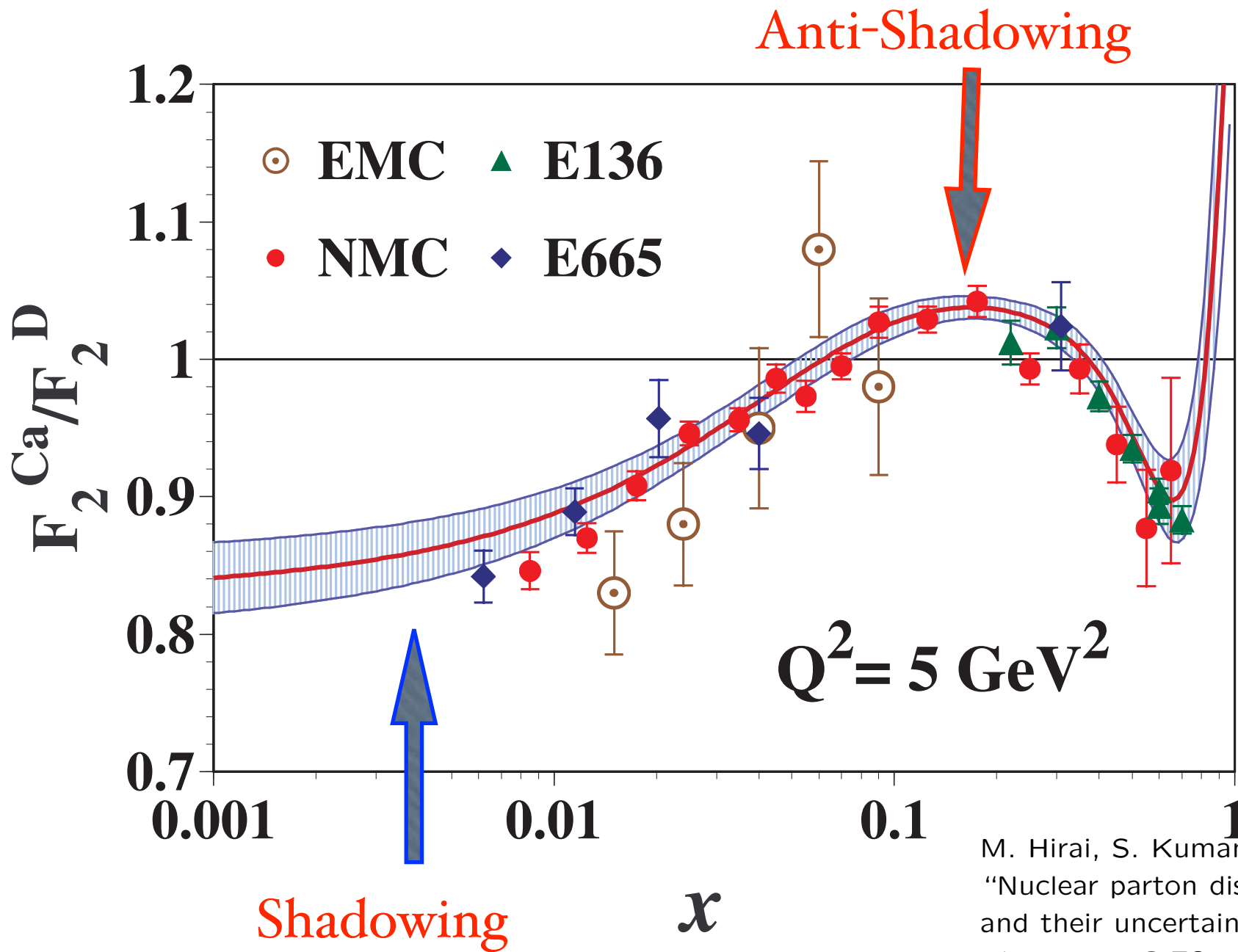


Sommerfeld-Schwinger-Sakharov Effect

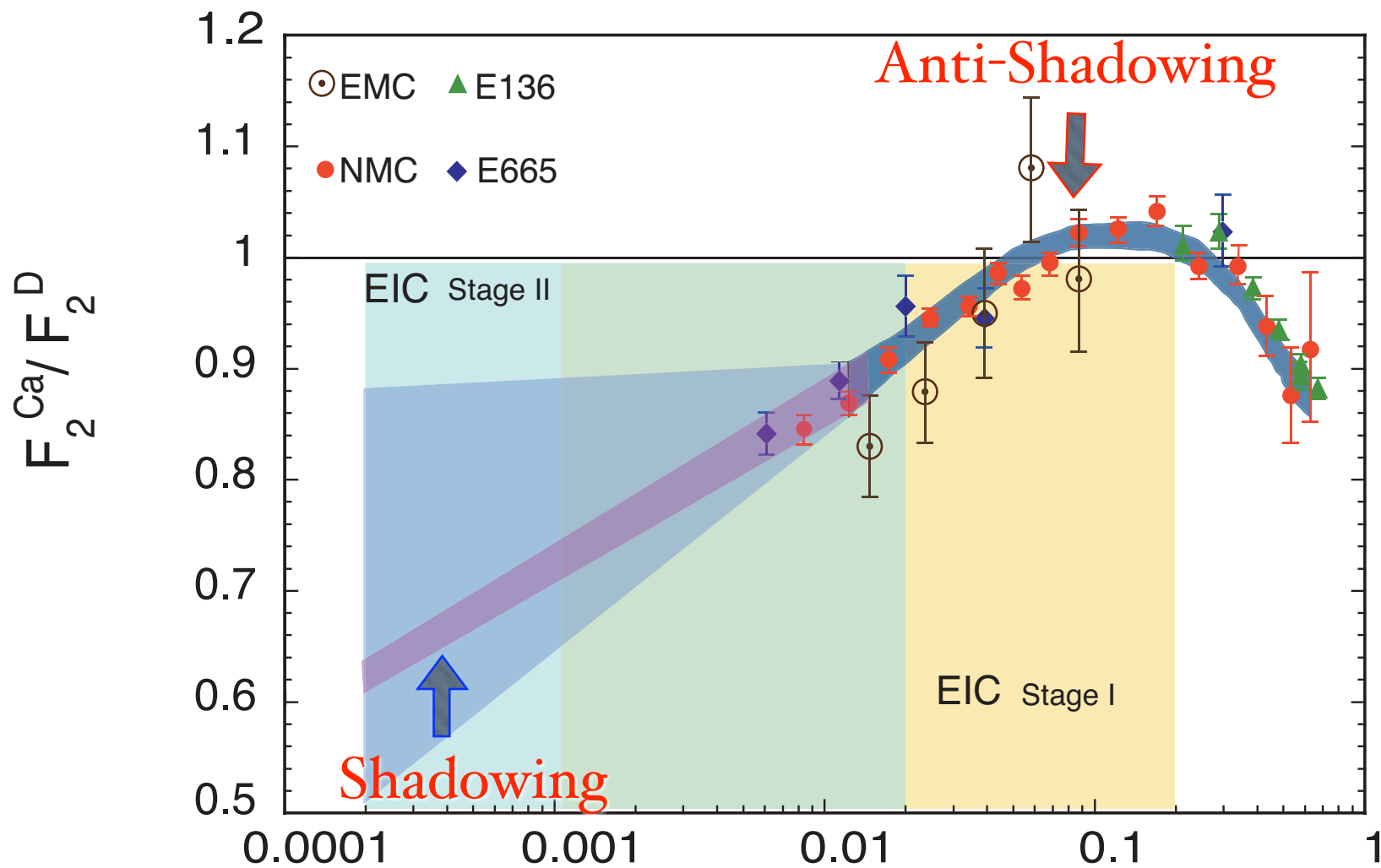
Bjorken: Analytical Connection to Rydberg Levels below Threshold

$$QCD : \pi\alpha \rightarrow \frac{4}{3}\alpha_s(\beta^2 s)$$

Kühn, Hoang, sjb

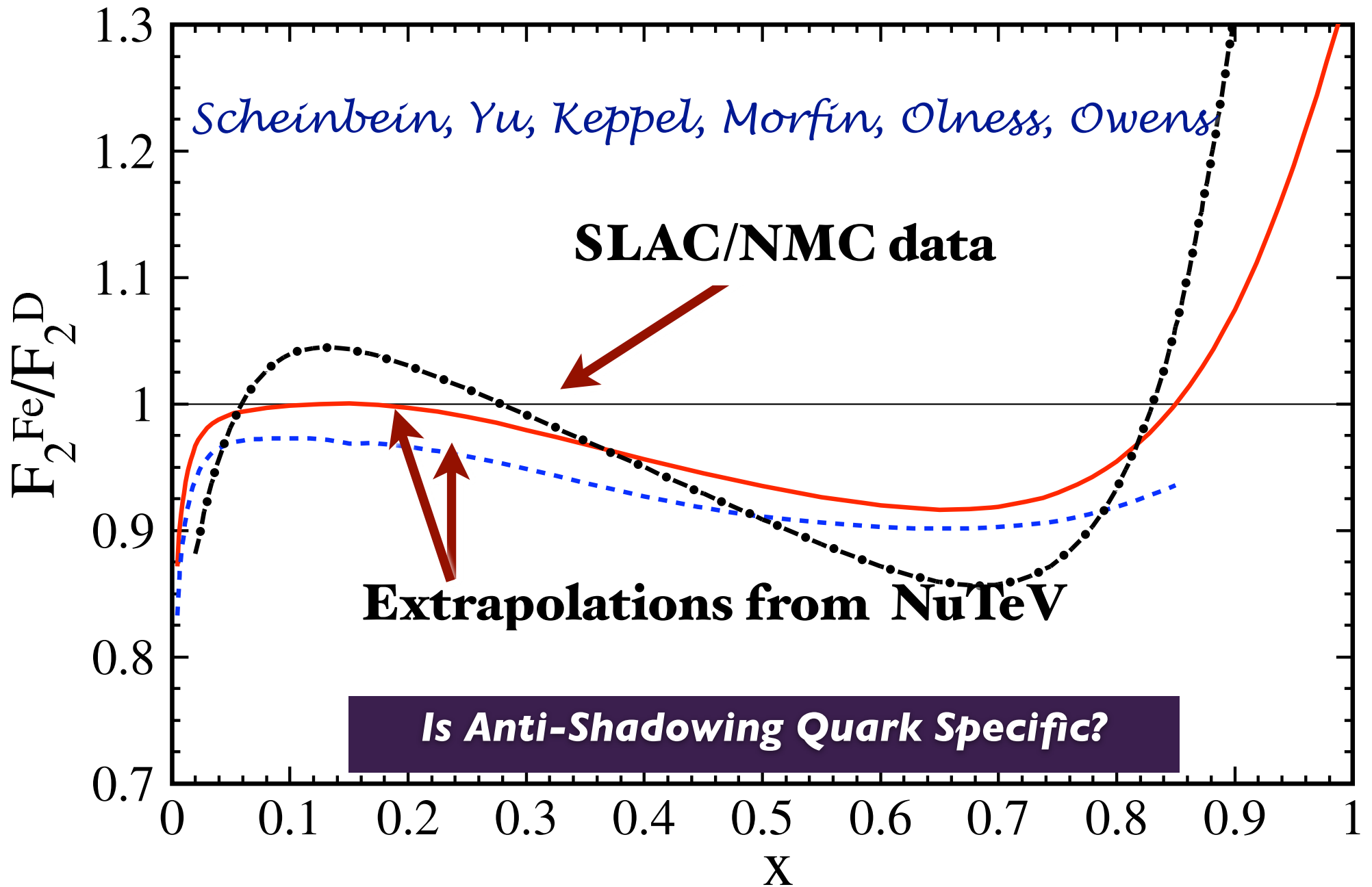


M. Hirai, S. Kumano and T. H. Nagai,
 "Nuclear parton distribution functions
 and their uncertainties,"
 Phys. Rev. C **70**, 044905 (2004)
 [arXiv:hep-ph/0404093].



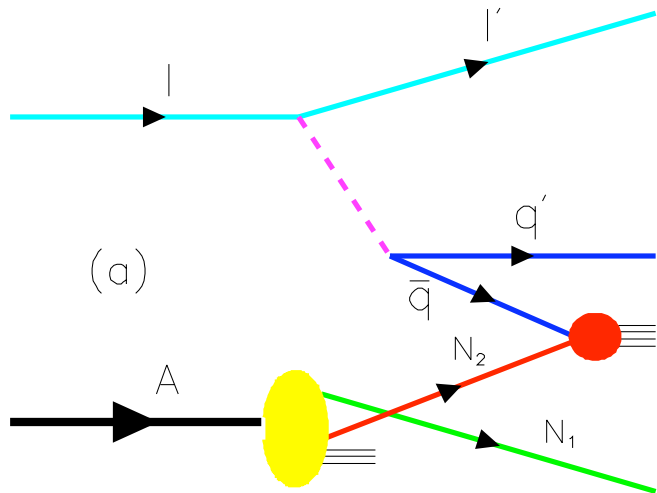
The ratio of nuclear over nucleon F_2 structure function, R_2 , as a function of Bjorken x , with data from existing fixed target DIS experiments at $Q^2 > 1 \text{ GeV}^2$, along with the QCD global fit from EPS09 [153]. Also shown are the respective coverage and resolution of the same measurements at the EIC at Stage-I and Stage-II. The purple error band is the expected systematic uncertainty at the EIC assuming a $\pm 2\%$ (a total of 4%) systematic error, while the statistical uncertainty is expected to be much smaller.

$$Q^2 = 5 \text{ GeV}^2$$



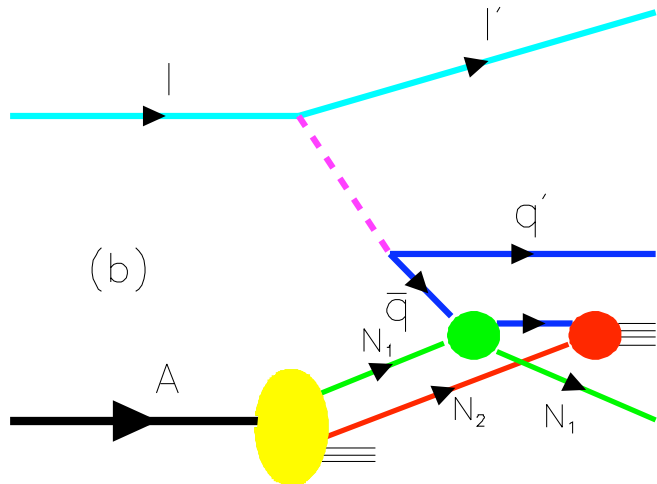
No anti-shadowing in deep inelastic neutrino scattering !

*Is Antishadowing in DIS
Non-Universal, Flavor-Dependent?*



The one-step and two-step processes in DIS on a nucleus.

Coherence at small Bjorken x_B :
 $1/Mx_B = 2\nu/Q^2 \geq L_A$.



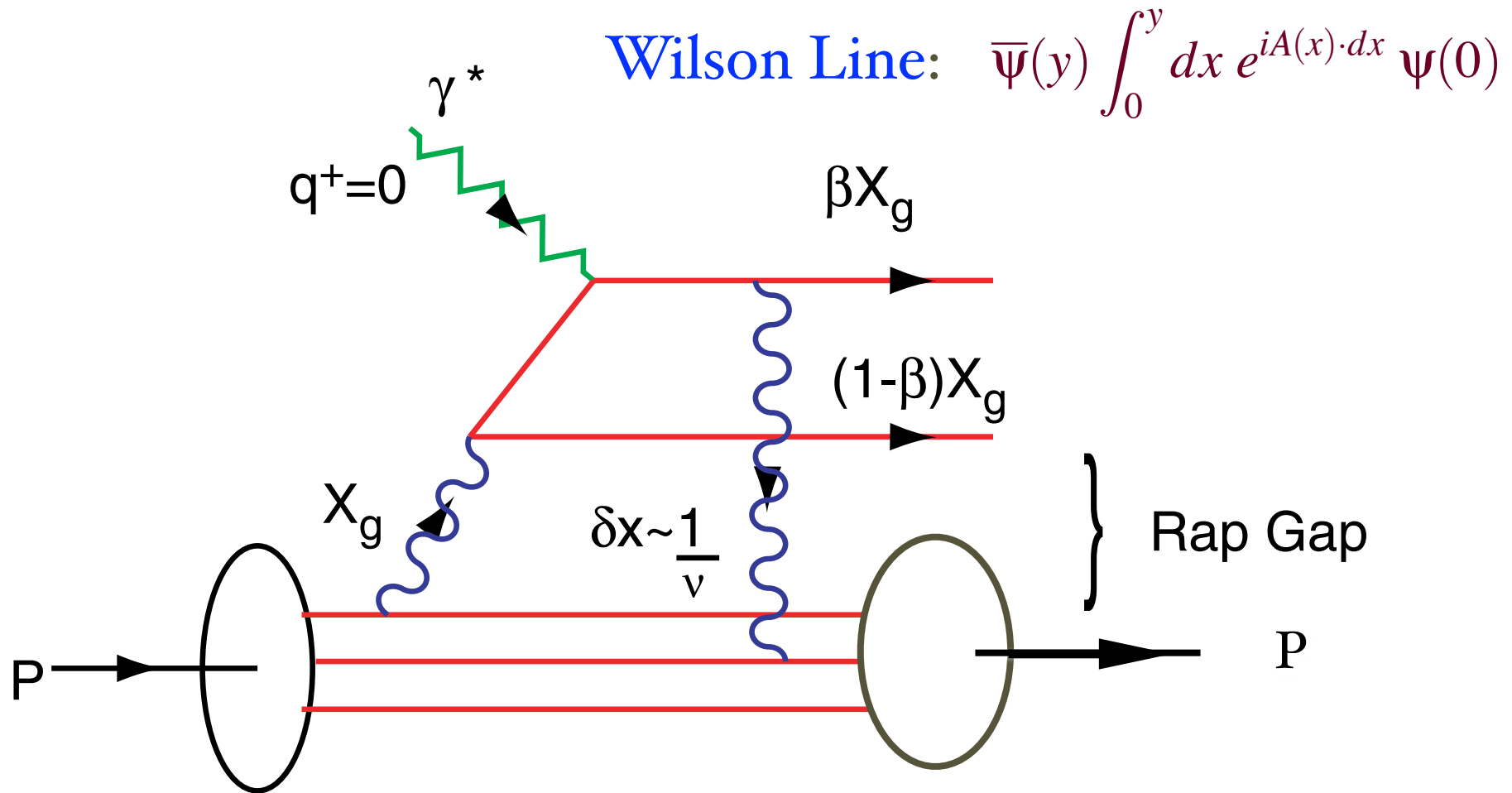
If the scattering on nucleon N_1 is via pomeron exchange, the one-step and two-step amplitudes are opposite in phase, thus diminishing the \bar{q} flux reaching N_2 .

Interior nucleons shadowed

→ Shadowing of the DIS nuclear structure functions.

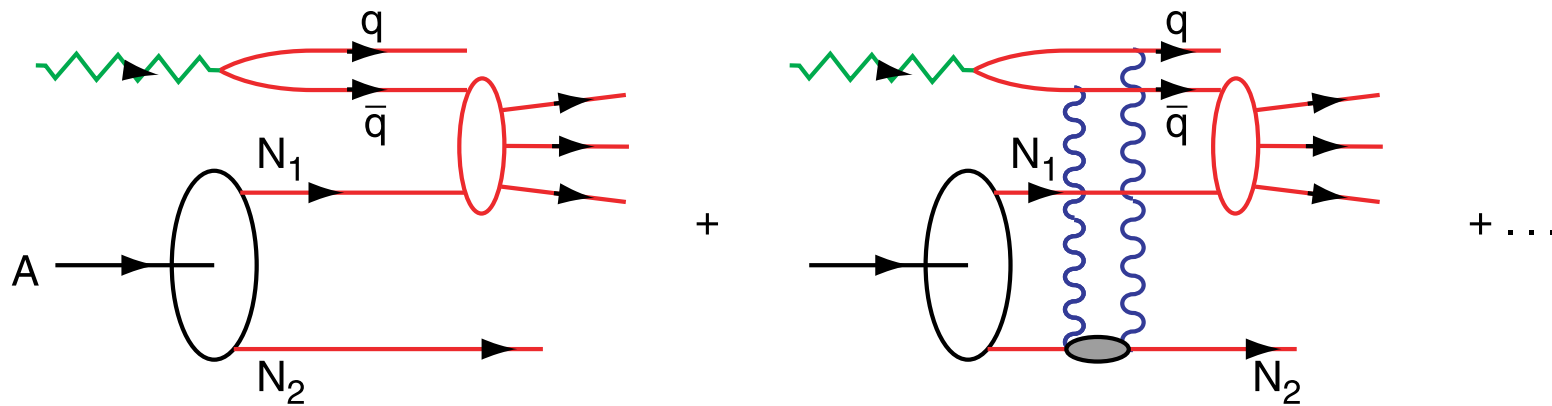
Observed HERA DDIS produces nuclear shadowing

QCD Mechanism for Rapidity Gaps



Reproduces lab-frame color dipole approach

Nuclear Shadowing in QCD



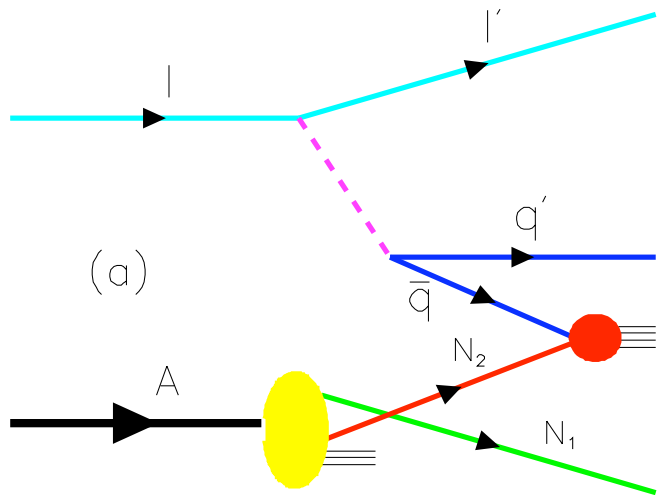
Shadowing depends on understanding leading twist-diffraction in DIS

Nuclear Shadowing not included in nuclear LFWF !

Dynamical effect due to virtual photon interacting in nucleus

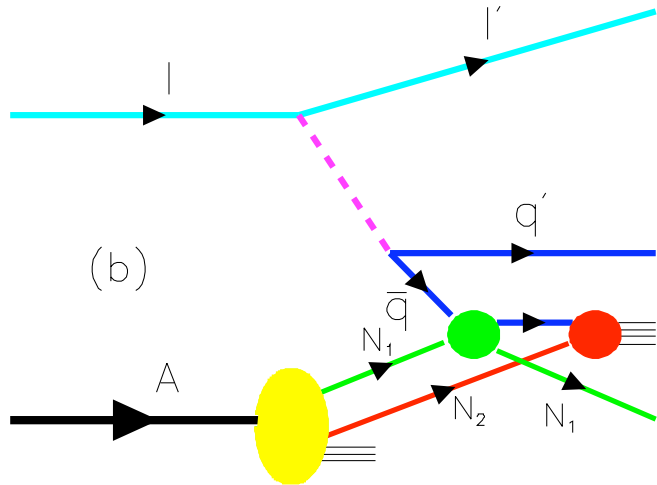
Diffraction via Reggeon gives constructive interference!

Anti-shadowing not universal



The one-step and two-step processes in DIS on a nucleus.

Coherence at small Bjorken x_B :
 $1/Mx_B = 2\nu/Q^2 \geq L_A$.



If the scattering on nucleon N_1 is via pomeron exchange, the one-step and two-step amplitudes are opposite in phase, thus diminishing the \bar{q} flux reaching N_2 .

→ Shadowing of the DIS nuclear structure functions.

Diffraction via Pomeron gives destructive interference!

Shadowing

Origin of Regge Behavior of Inelastic Structure Functions

Deep

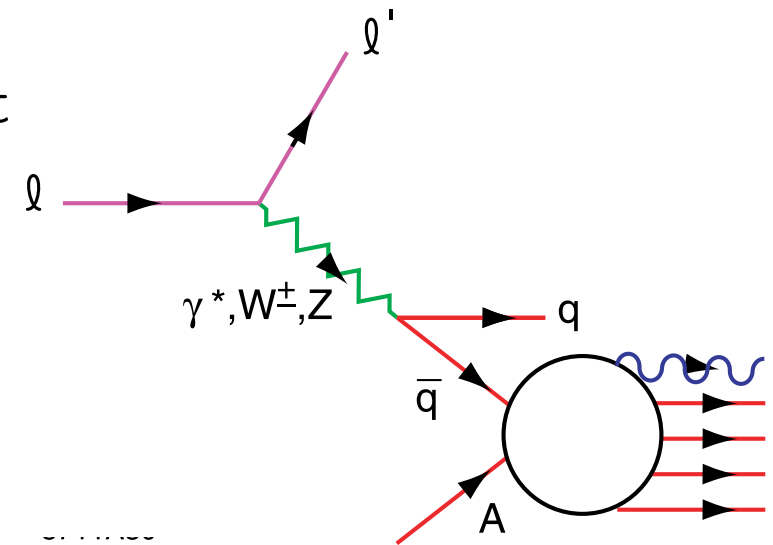
$$F_{2p}(x) - F_{2n}(x) \propto x^{1/2}$$

Antiquark interacts with target nucleus at energy $\hat{s} \propto \frac{1}{x_{bj}}$

Regge contribution: $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R - 1}$

Nonsinglet Kuti-Weisskoff $F_{2p} - F_{2n} \propto \sqrt{x_{bj}}$ at small x_{bj} .

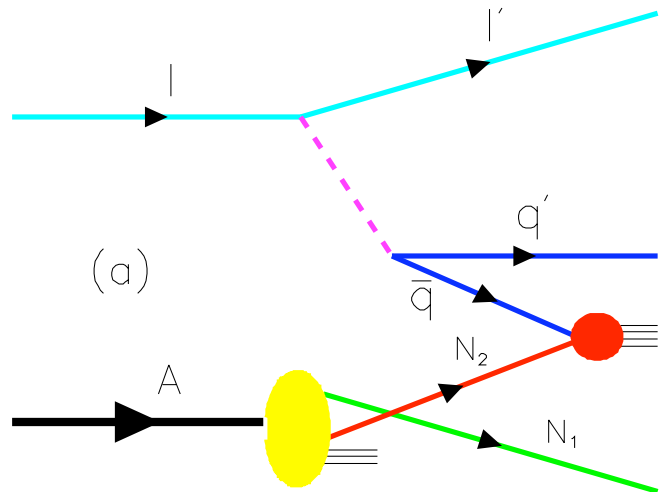
Shadowing of $\sigma_{\bar{q}M}$ produces shadowing of nuclear structure function.



**Landshoff,
Polkinghorne, Short**

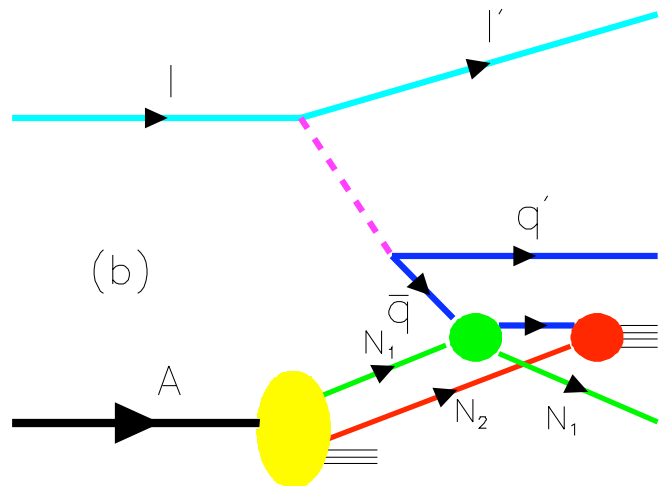
Close, Gunion, sjb

**Schmidt, Yang, Lu,
sjb**



The one-step and two-step processes in DIS on a nucleus.

Coherence at small Bjorken x_B :
 $1/Mx_B = 2\nu/Q^2 \geq L_A$.



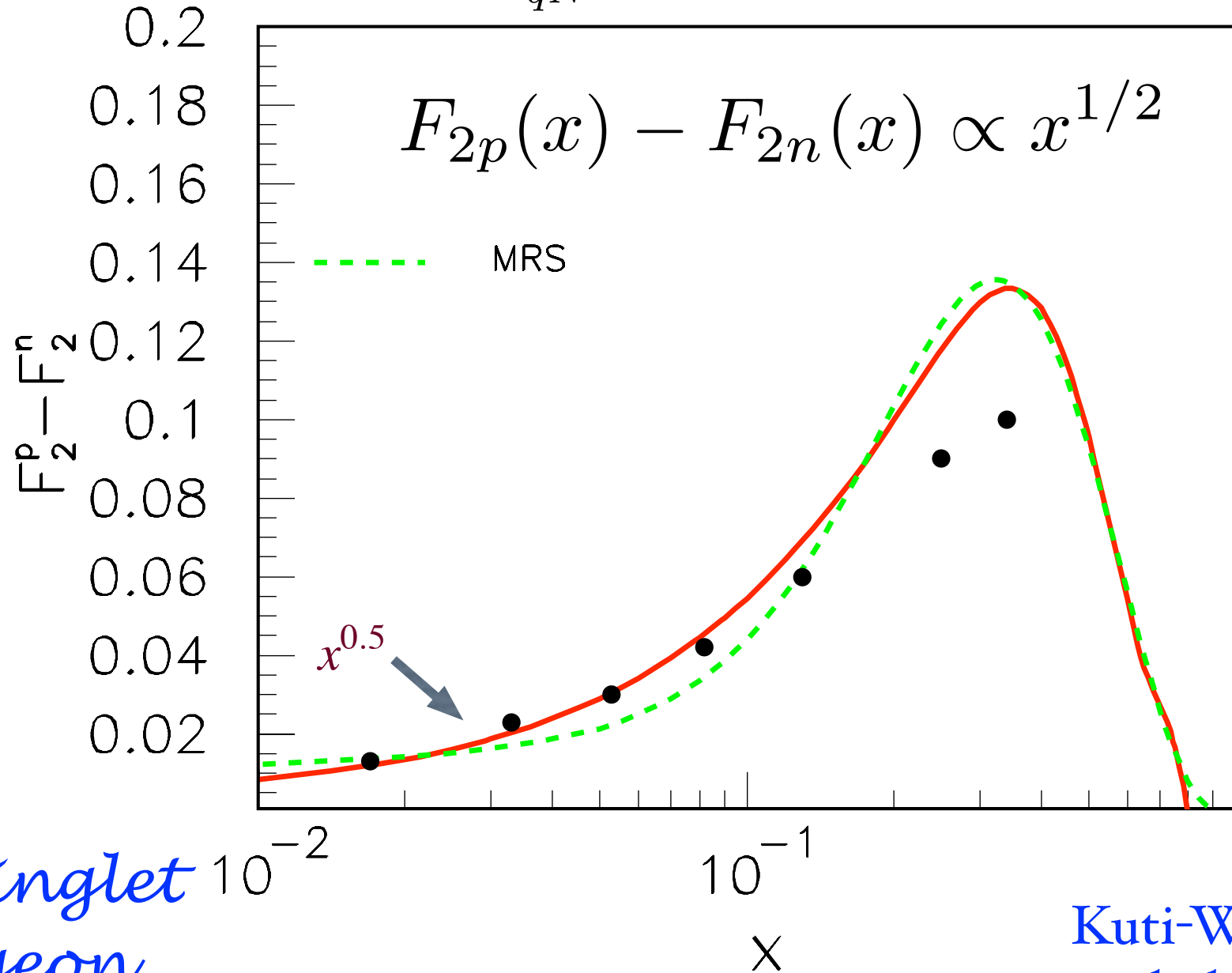
If the scattering on nucleon N_1 is via ~~pomeron~~ exchange, the one-step and two-step amplitudes are ~~opposite in phase~~, thus diminishing the ~~\bar{q} flux reaching N_2~~ .

Regge
constructive in phase
 thus **increasing** the flux reaching N_2

Interior nucleons anti-shadowed

Regge Exchange in DDIS produces nuclear anti-shadowing

Regge contribution: $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R - 1}$ $\alpha_R \simeq 1/2$



*Non-singlet
Reggeon
Exchange*

*Kuti-Weisskopf
behavior*

Reggeon Exchange

Phase of two-step amplitude relative to one step:

$$\frac{1}{\sqrt{2}}(1 - i) \times i = \frac{1}{\sqrt{2}}(i + 1)$$

Constructive Interference

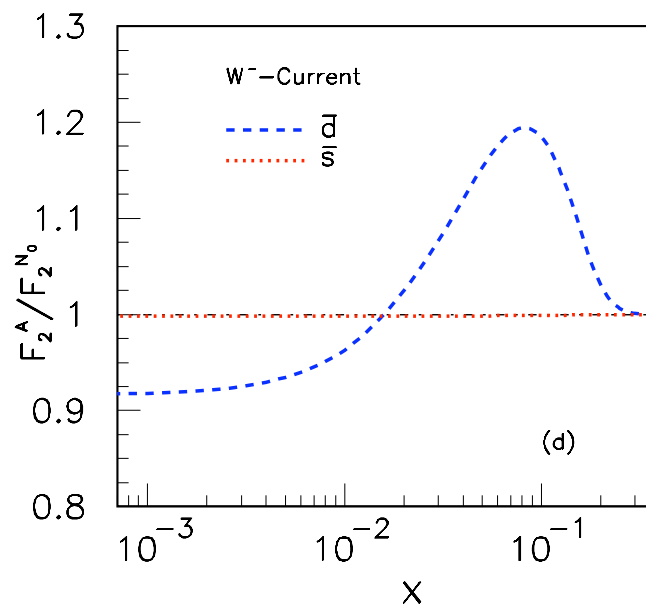
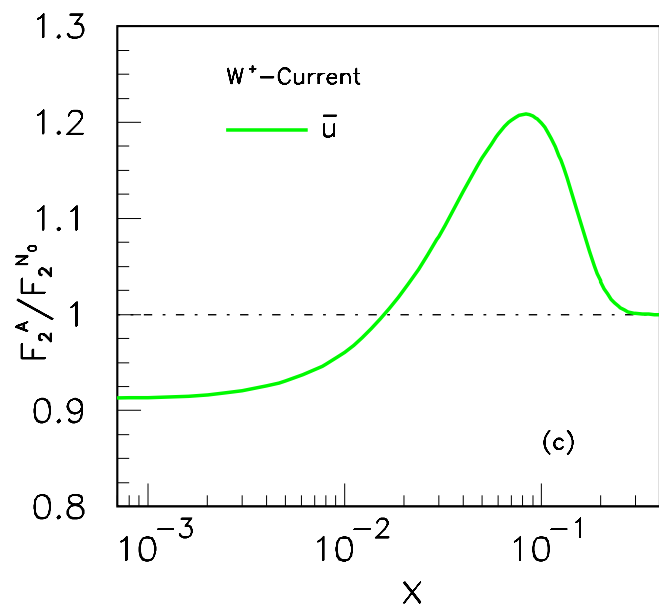
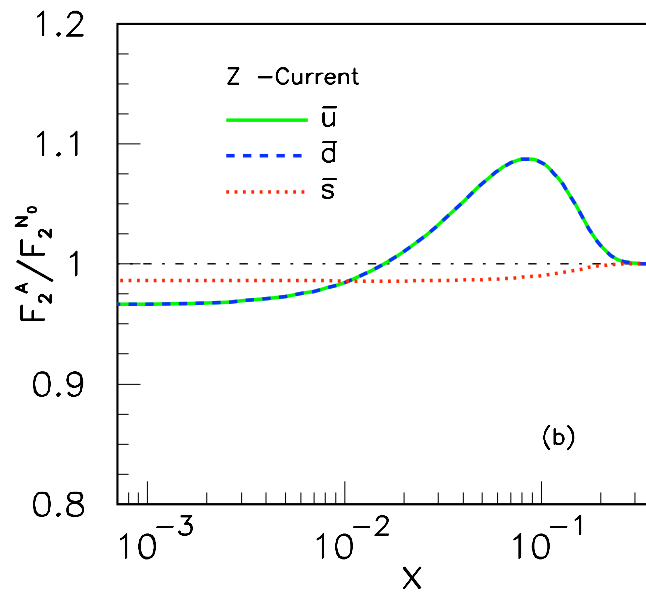
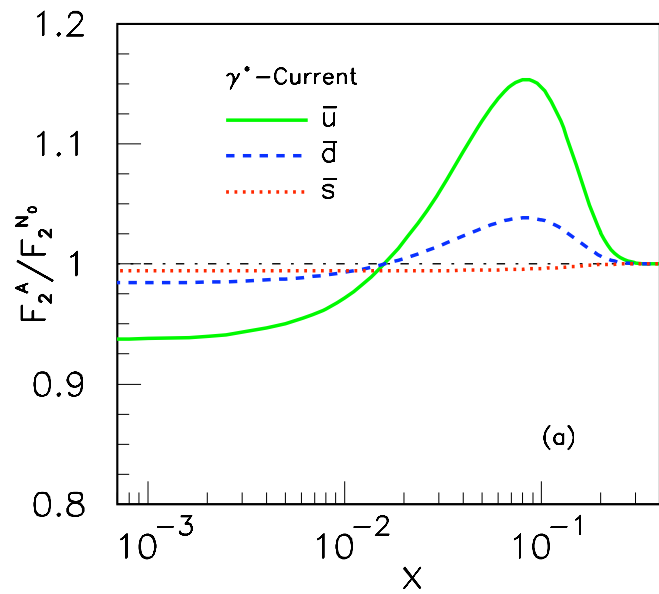
Depends on quark flavor!

Thus antishadowing is not universal

Different for couplings of γ^* , Z^0 , W^\pm

Critical test: Tagged Drell-Yan

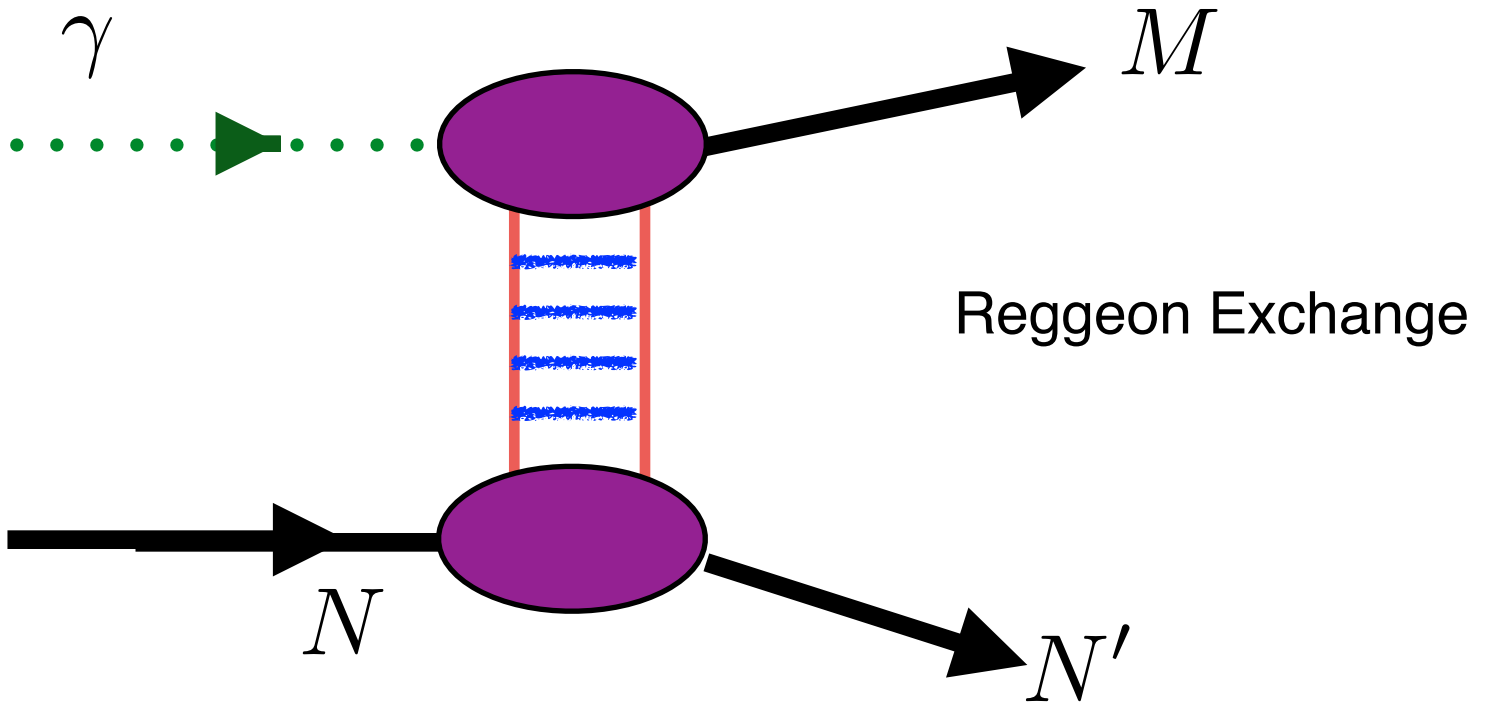
Schmidt, Yang; sjb



Modifies
NuTeV extraction of
 $\sin^2 \theta_W$

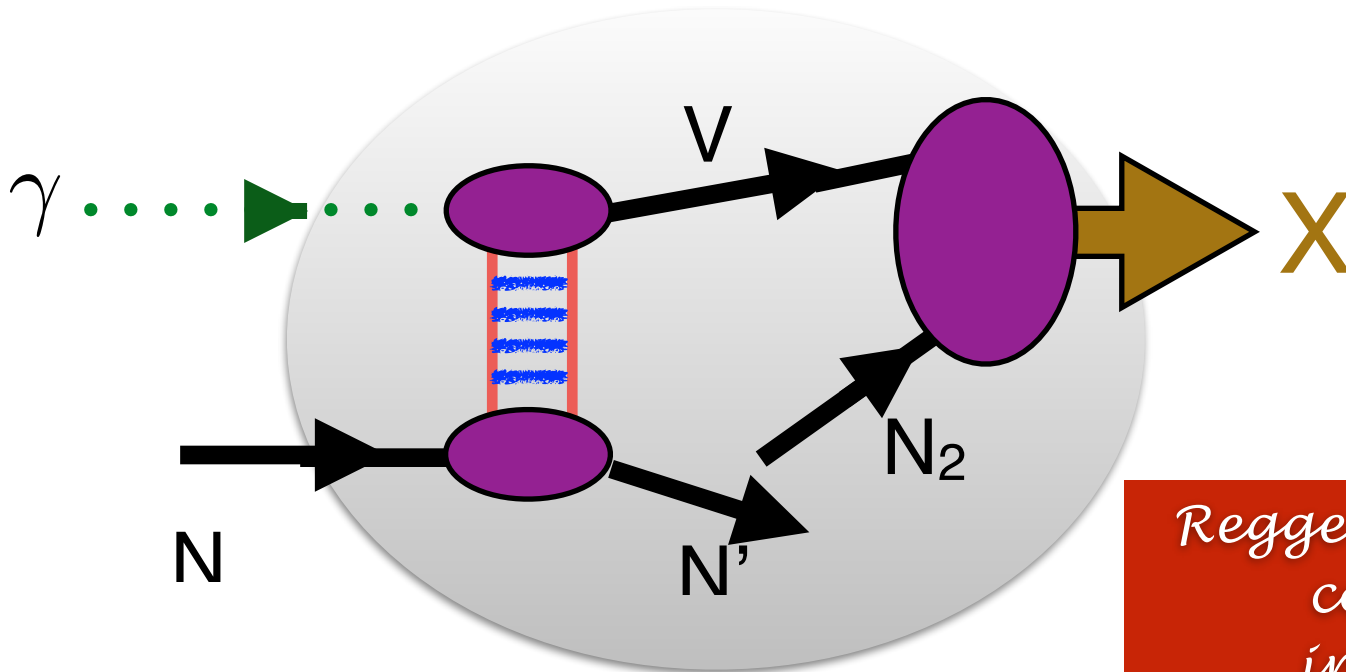
Test in flavor-tagged
DIS at the EIC

Nuclear Antishadowing not universal !

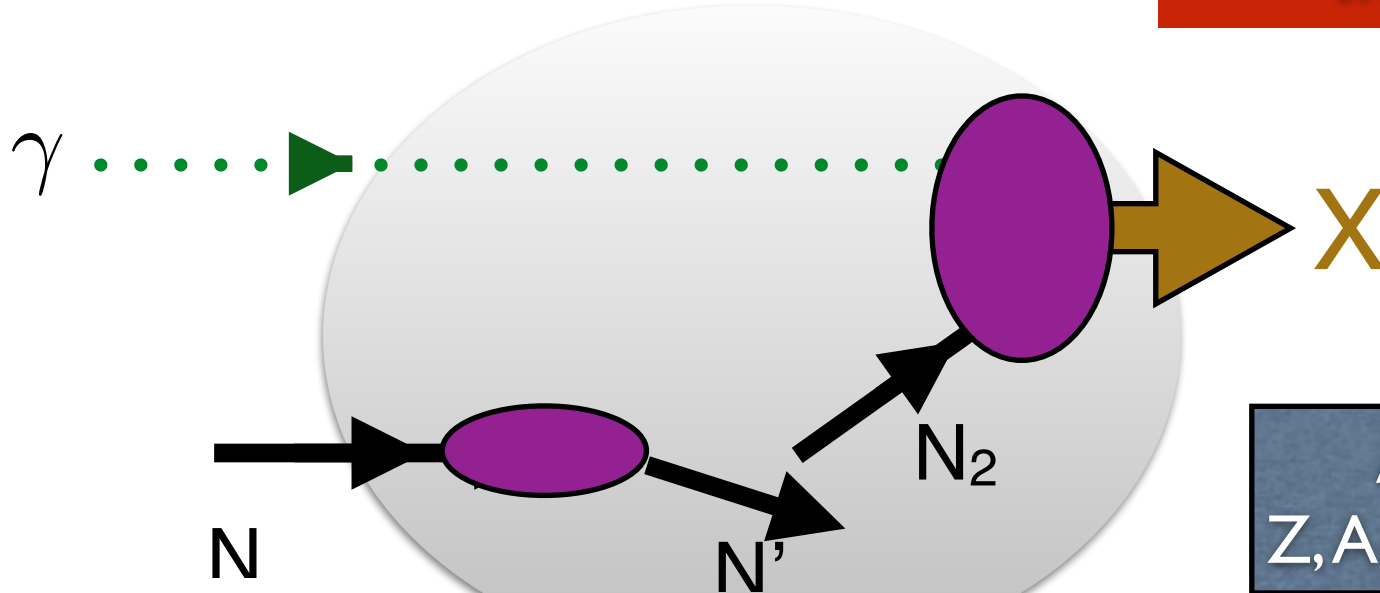


Two-step and One-Step Glauber processes

$l=1$ Reggeon Exchange on N_1



Regge Phase can give constructive interference!



Anomalous
Z,A-Z dependence

Novel QCD Physics at the EIC

- **Control Collisions of Flux Tubes and Ridge Phenomena**
- **Study Flavor-Dependence of Anti-Shadowing**
- **Heavy Quarks at Large x ; Exotic States**
- **Direct, color-transparent hard subprocesses and the baryon anomaly**
- **Tri-Jet Production and the proton's LFWF**
- **Odderon-Pomeron Interference**
- **Digluon-initiated subprocesses and anomalous nuclear dependence of quarkonium production**
- **Factorization-Breaking Lensing Corrections**

Regge Behavior of Scattering Amplitudes

$$M = \sum_R s^{\alpha_R(t)} F_R(t) e^{i\phi_R} \quad \frac{d\sigma}{dt} \propto \frac{|M|^2}{s^2}$$

$$F_2(x) \sim x^{1-\alpha_R}$$

R = Pomeron ($\alpha_{\mathcal{P}} \simeq 1 + \epsilon$), $C = +$, *phase = Imaginary*

Odderon ($\alpha_{\mathcal{O}} \simeq 1$), $C = -$, *phase = Real*

Reggeon ($\alpha_{\mathcal{R}} \simeq 1/2$), $C = \pm$, *phase = Real + Imaginary*

FP ($\alpha_{\mathcal{FP}} \simeq 0$), $C = +$, *phase = Real*

Reggeon Exchange

Regge contribution: $\sigma_{\bar{q}N} \sim \hat{s}^{\alpha_R - 1}$ $\alpha_R \simeq 1/2$

Phase of two-step amplitude relative to one step:

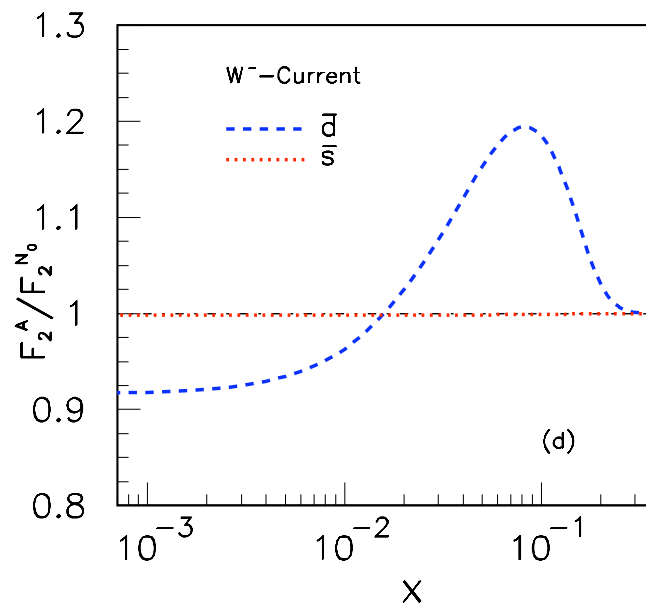
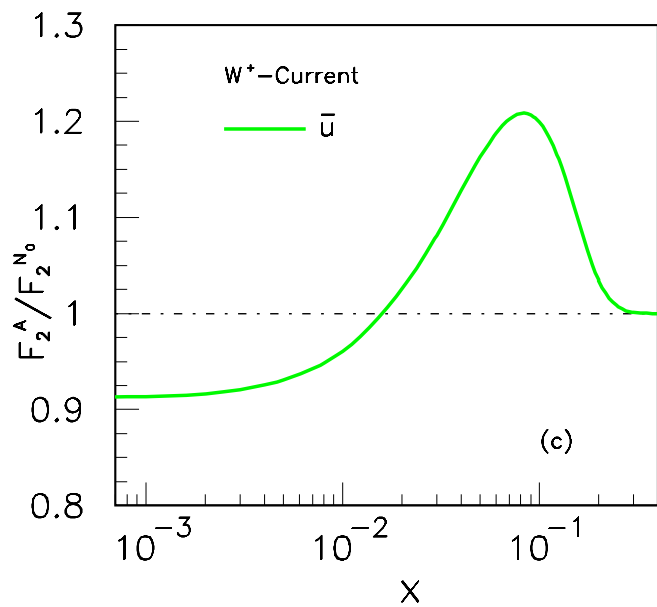
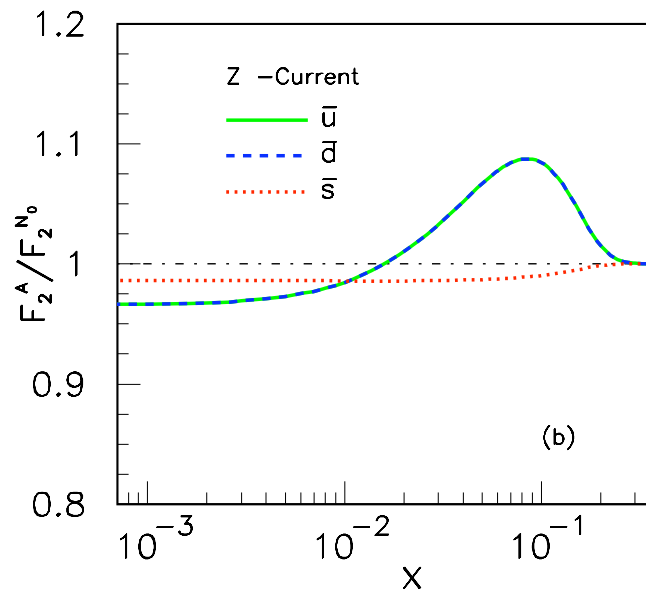
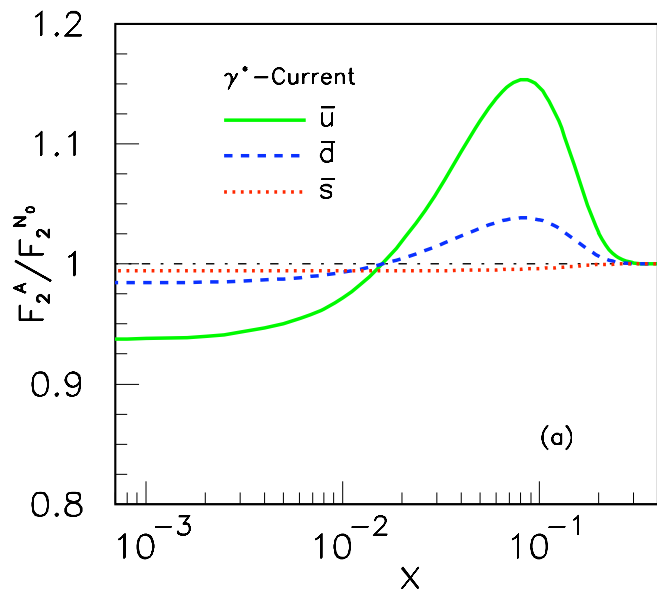
$$\frac{1}{\sqrt{2}}(1 - i) \times i = \frac{1}{\sqrt{2}}(i + 1)$$

Constructive Interference

Depends on quark flavor!

Thus antishadowing is not universal

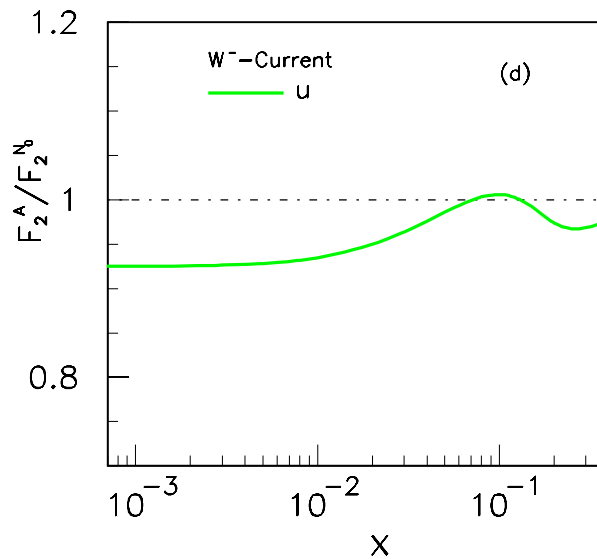
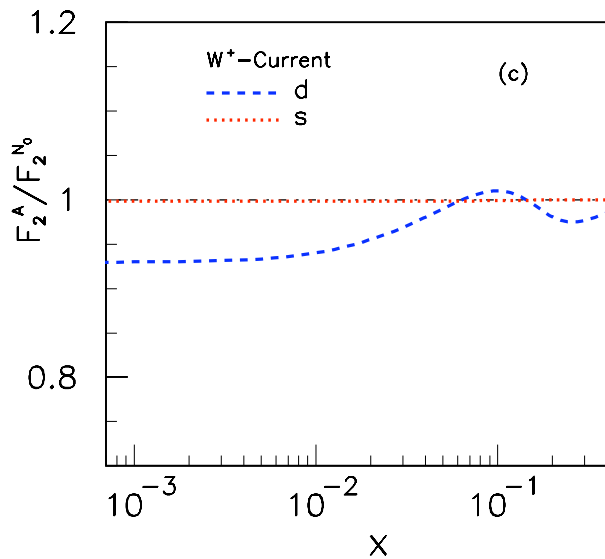
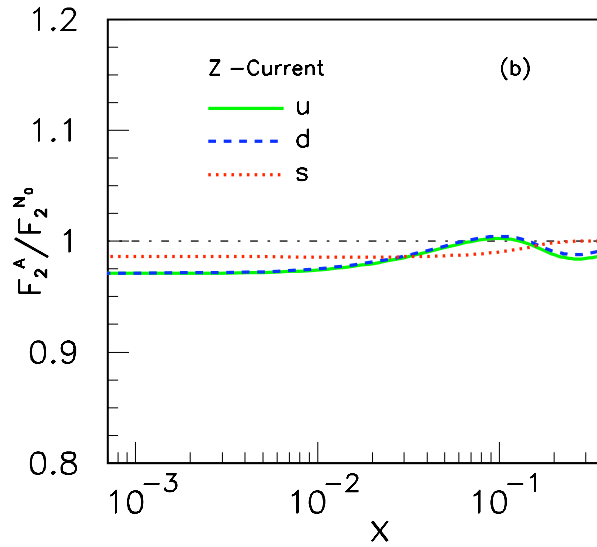
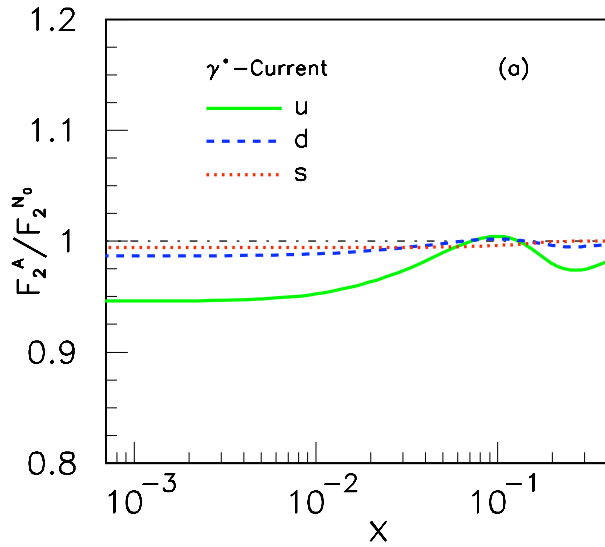
Different for couplings of γ^* , Z^0 , W^\pm



Schmidt, Lu, Yang, sjb

Nuclear Antishadowing not universal !

Shadowing and Antishadowing of DIS Structure Functions



S. J. Brodsky, I. Schmidt and J. J. Yang,
“Nuclear Antishadowing in
Neutrino Deep Inelastic Scattering,”
Phys. Rev. D 70, 116003 (2004)
[arXiv:hep-ph/0409279].

Modifies
NuTeV extraction of
 $\sin^2 \theta_W$

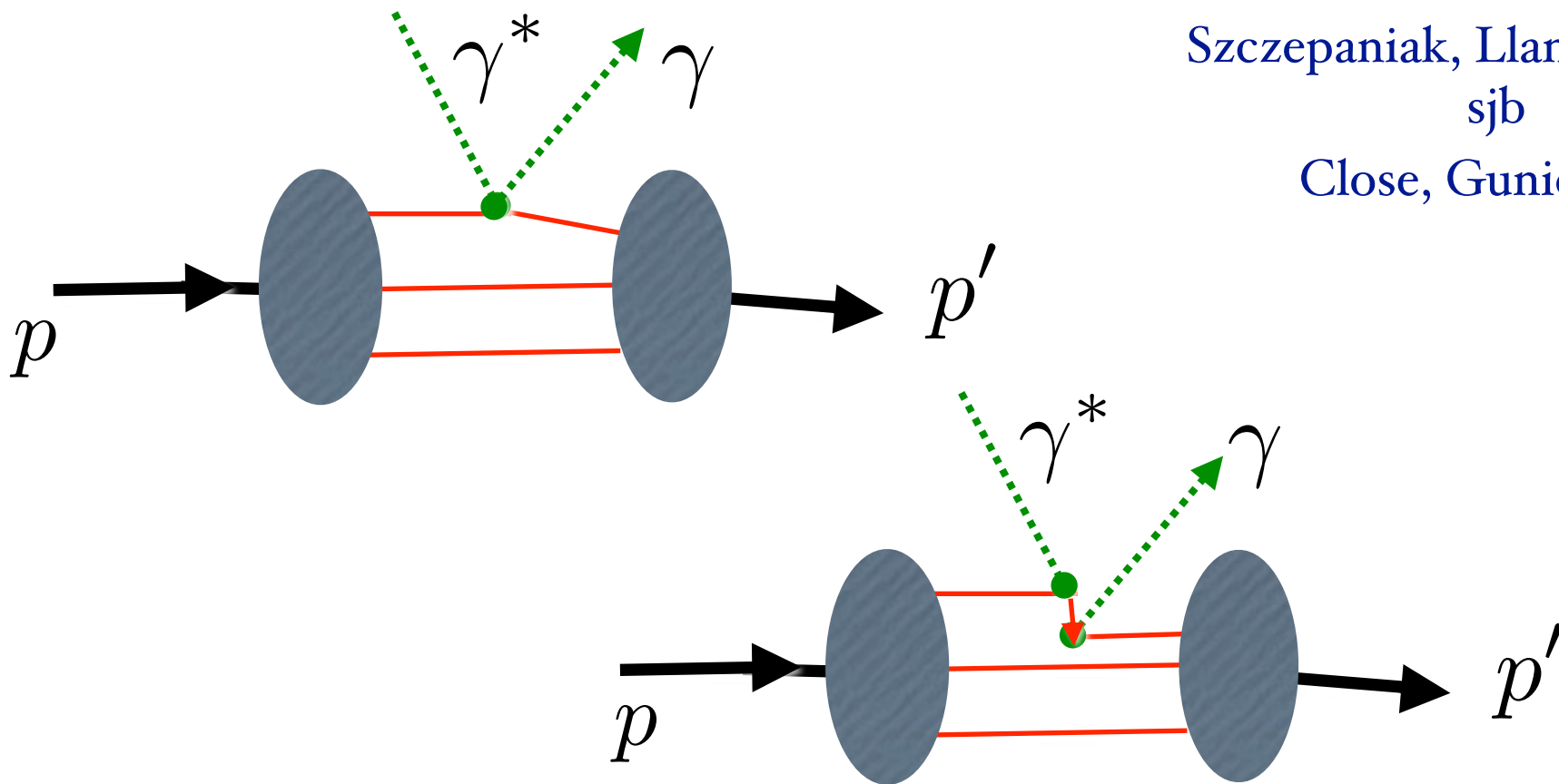
**Test in flavor-tagged
lepton-nucleus collisions**

Crucial JLab Experiments

- **Measure Diffractive DIS: Agree with Shadowing of Nuclear Structure Functions?**
- **Isospin Dependence of Diffractive DIS — Reggeon Exchange**
- **Flavor Dependence of Antishadowing: Tagged Quark Distributions?**
- **Test for Odderon Exchange in DDIS**

$J=0$ Fixed Pole Contribution to DVCS

- $J=0$ fixed pole -- direct test of QCD locality -- from seagull or instantaneous contribution to Feynman propagator

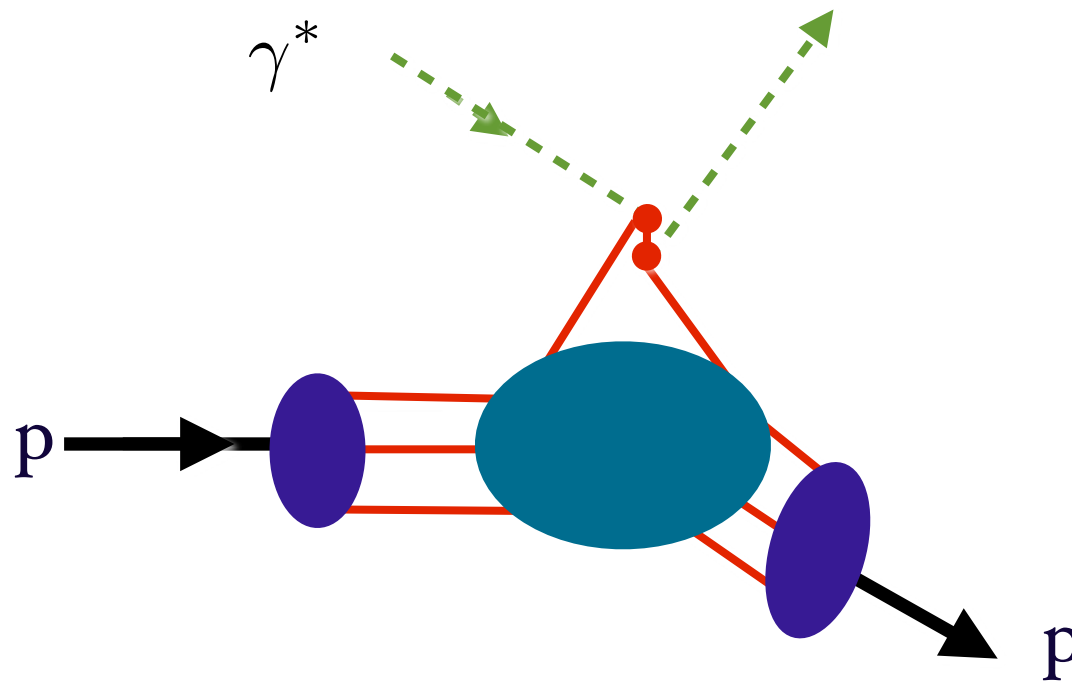


Szczepaniak, Llanes-Estrada,
sjb
Close, Gunion, sjb

Real amplitude, independent of Q^2 at fixed t

Deeply Virtual Compton Scattering

$$\gamma^* p \rightarrow \gamma p$$



*Seagull interaction
(instantaneous quark
exchange or Z-graph)*

$$s \gg -t, Q^2 \gg \Lambda_{QCD}^2$$

*Hard Reggeon
Domain*

$$T(\gamma^*(q)p \rightarrow \gamma(k) + p) \sim \epsilon \cdot \epsilon' \sum_R s_R^\alpha(t) \beta_R(t)$$

$$\alpha_R(t) \rightarrow 0$$

Reflects elementary coupling of two photons to quarks

$$\beta_R(t) \sim \frac{1}{t^2}$$

$$\frac{d\sigma}{dt} \sim \frac{1}{s^2} \frac{1}{t^4} \sim \frac{1}{s^6} \text{ at fixed } \frac{Q^2}{s}, \frac{t}{s}$$

J=0 Fixed pole in real and virtual Compton scattering

Damashek, Gilman;
Close, Gunion, sjb
Llanes-Estrada,
Szczepaniak, sjb

Effective two-photon contact term

Seagull for scalar quarks

Real phase

$$M = s^0 \sum e_q^2 F_q(t)$$

Independent of Q^2 at fixed t

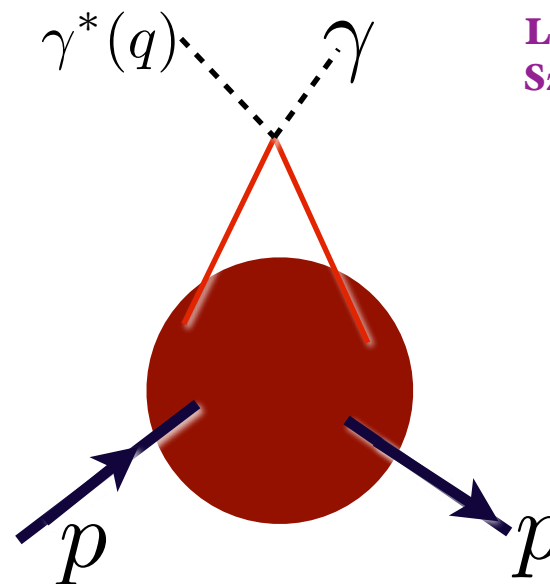
$\langle 1/x \rangle$ Moment: Related to Feynman-Hellman Theorem

Fundamental test of local gauge theory

Q^2 -independent contribution to Real DVCS amplitude

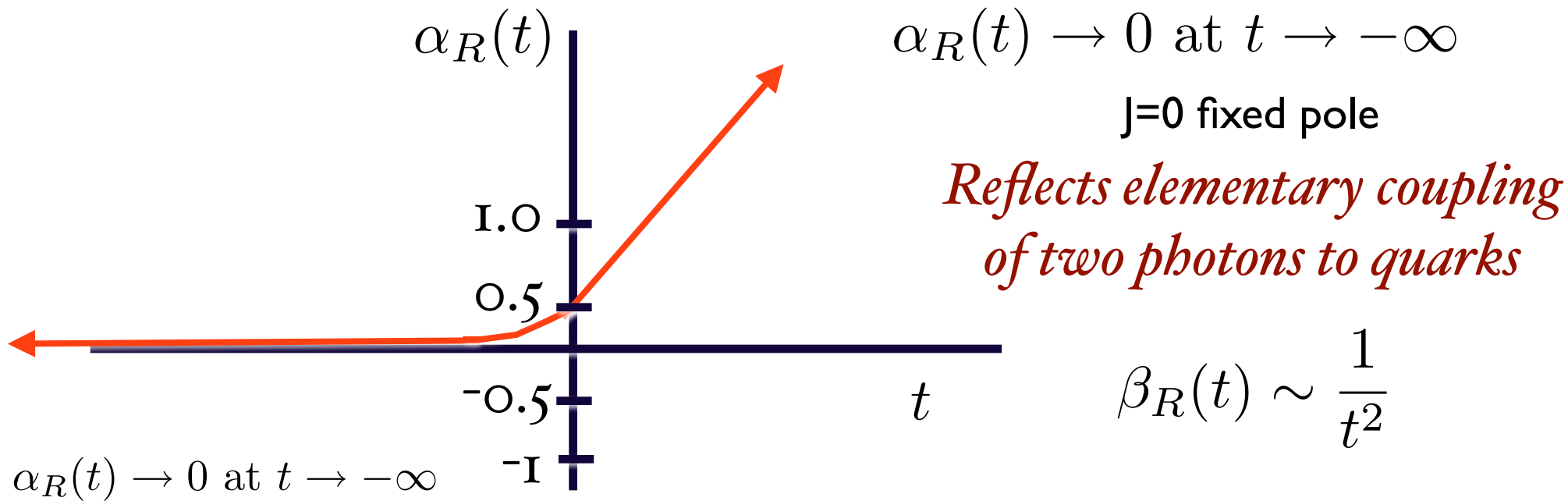
$$s^2 \frac{d\sigma}{dt} (\gamma^* p \rightarrow \gamma p) = F^2(t)$$

independent of s



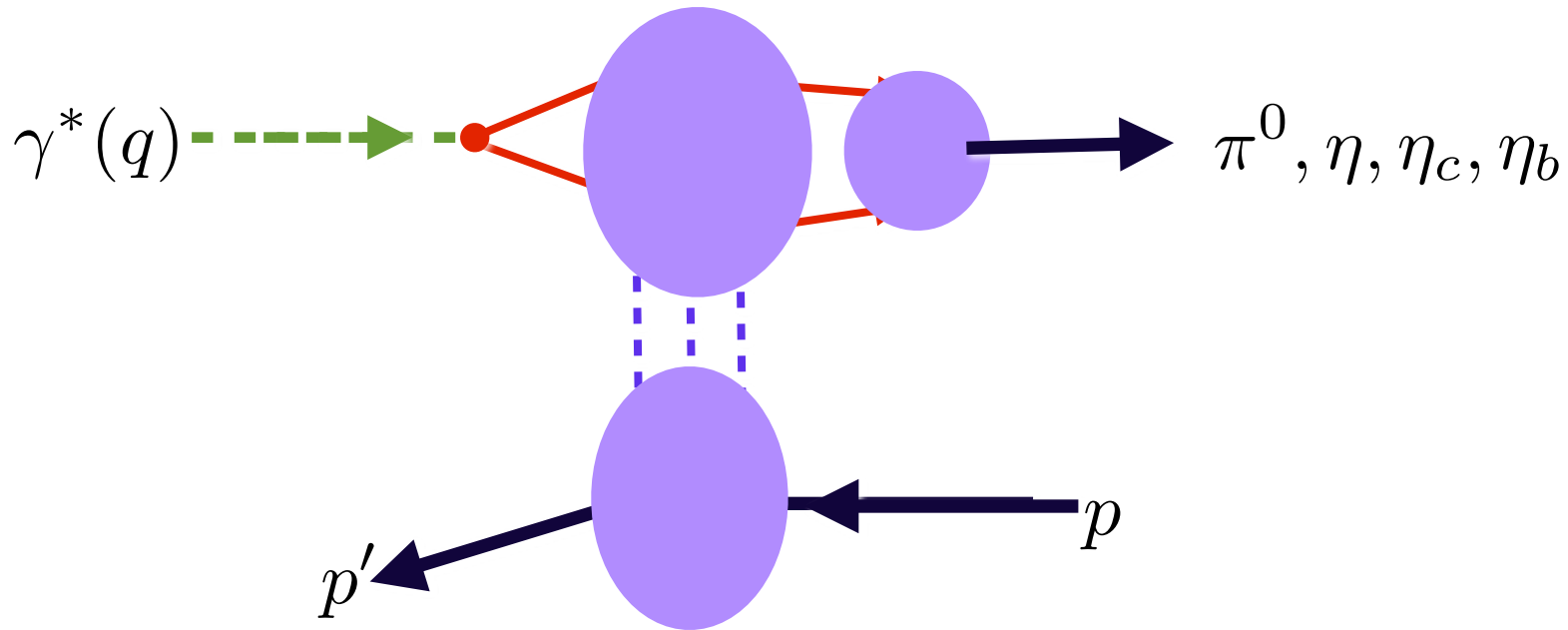
Regge domain

$$T(\gamma^* p \rightarrow \pi^+ n) \sim \epsilon \cdot p_i \sum_R s_R^{\alpha_R(t)} \beta_R(t) \quad s \gg -t, Q^2$$



$$\frac{d\sigma}{dt}(\gamma^* p \rightarrow \gamma p) \rightarrow \frac{1}{s^2} \beta_R^2(t) \sim \frac{1}{s^2 t^4} \sim \frac{1}{s^6} \text{ at fixed } \frac{t}{s}, \frac{Q^2}{s}$$

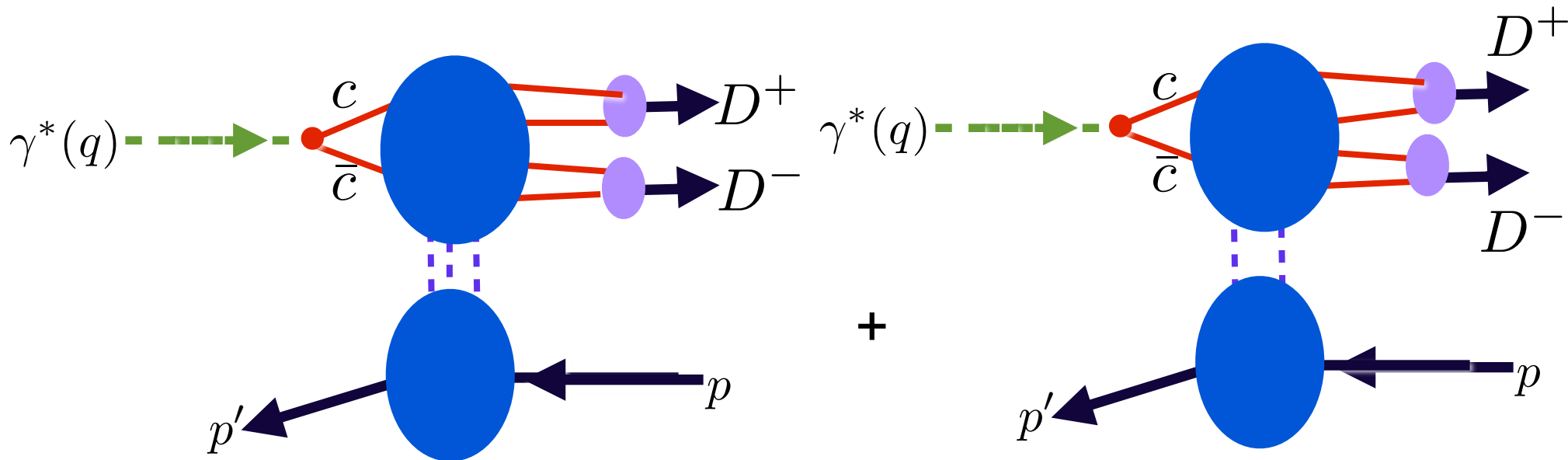
Fundamental test of QCD



Odderon has never been observed!

Look for Charge Asymmetries from Odderon-Pomeron Interference

**Merino, Rathsman,
sjb**



Odderon-Pomeron Interference leads to $K^+ K^-$, $D^+ D^-$ and $B^+ B^-$ charge and angular asymmetries

Odderon at amplitude level

Strong enhancement at heavy-quark pair threshold from QCD Sakharov-Schwinger-Sommerfeld effect

Merino, Rathsman, sjb

$$\frac{\pi\alpha_s(\beta^2 s)}{\beta}$$

Hoang, Kuhn, sjb

Single-spin asymmetries

Leading Twist Sivers Effect

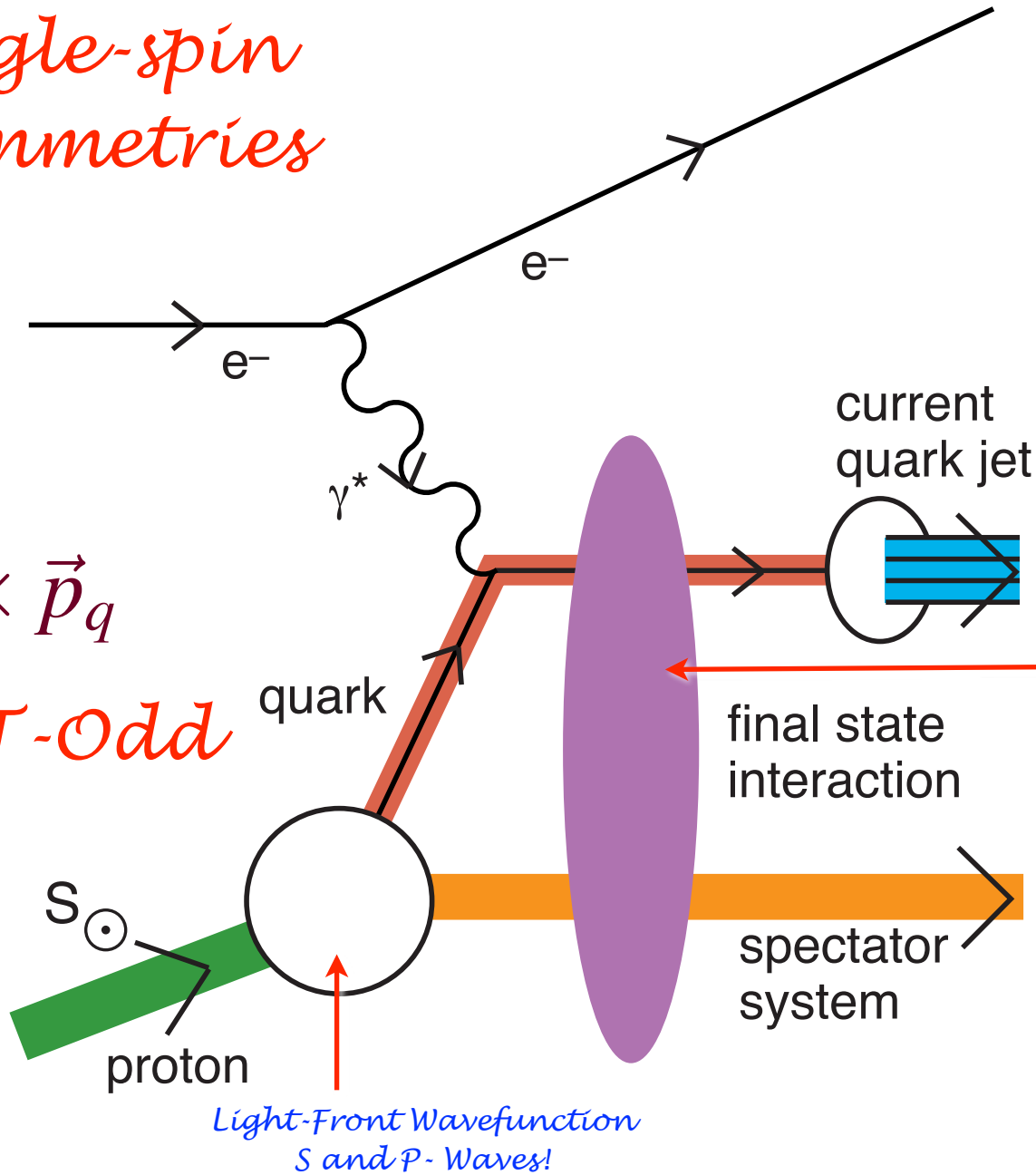
Hwang, Schmidt, sjb

Collins, Burkardt, Ji, Yuan. Xiao, Pasquini, ...

QCD S- and P-Coulomb Phases --Wilson Line

“Lensing Effect”

Leading-Twist Rescattering Violates pQCD Factorization!



$$i \vec{S}_p \cdot \vec{q} \times \vec{p}_q$$

Pseudo-T-Odd

**QED:
Lensing
involves soft
scales**

S_p
proton

*Light-Front Wavefunction
S and P-Waves!*

quark

final state
interaction

current
quark jet

spectator
system

Sign reversal in DY!

Single-spin asymmetries in exclusive channels

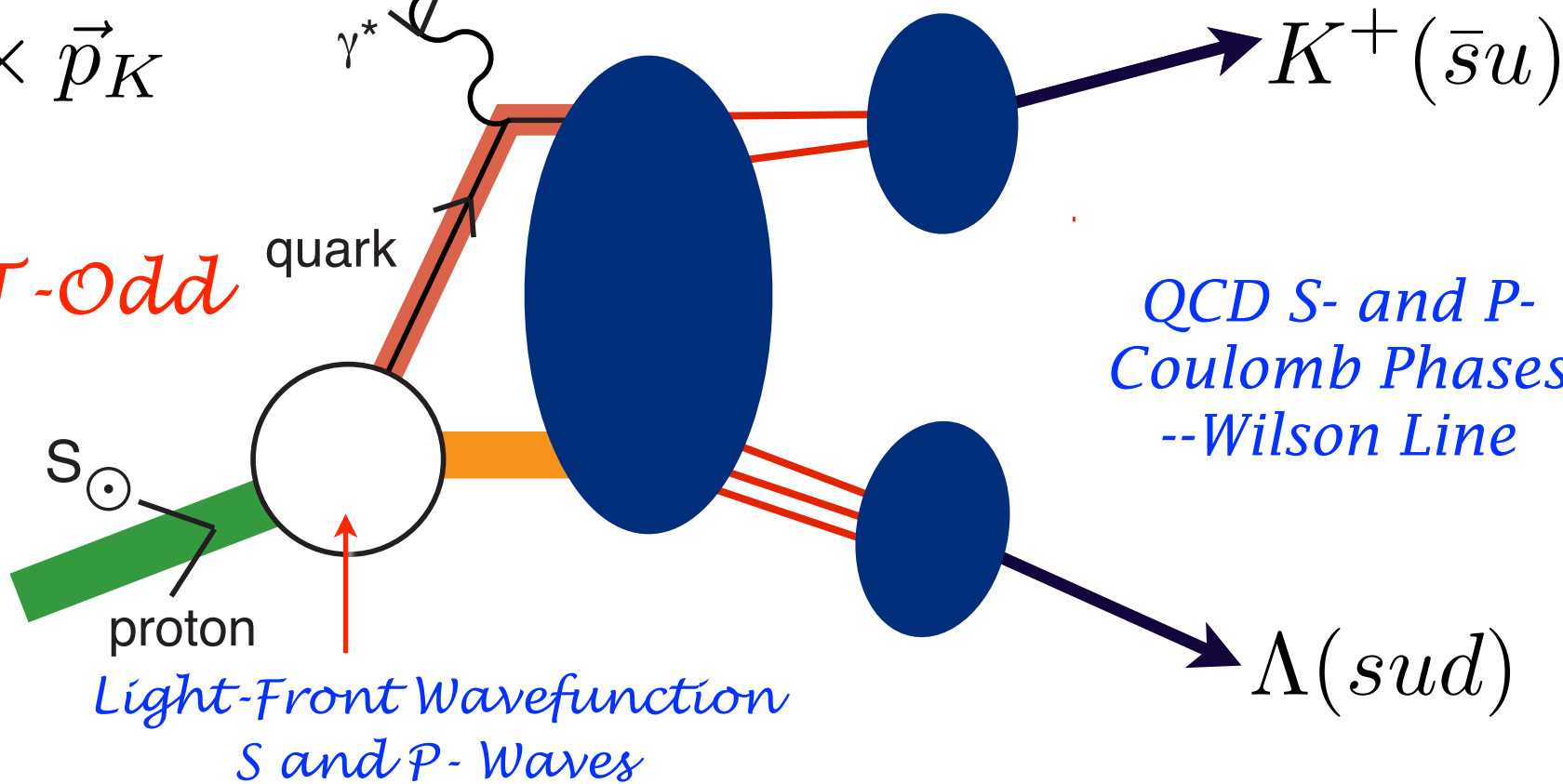
$$i\vec{S}_\Lambda \cdot \vec{q} \times \vec{p}_K$$

$$i\vec{S}_p \cdot \vec{q} \times \vec{p}_K$$

$$e^- \gamma^* p_\uparrow \rightarrow K^+ \Lambda$$

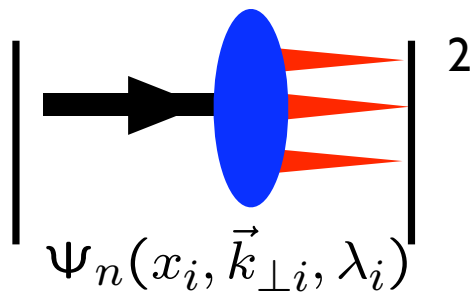
Exclusive Sivers Effect connects to Inclusive Effect

Pseudo-T-Odd




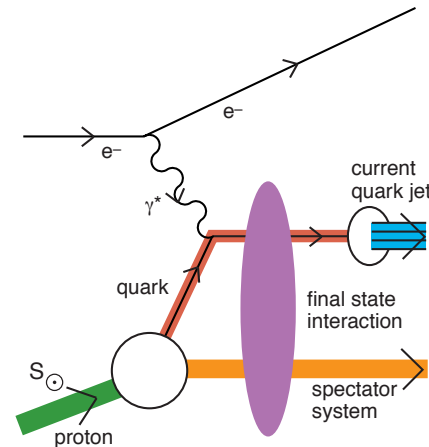
Static

- Square of Target LFWFs
- No Wilson Line
- Probability Distributions
- Process-Independent
- T-even Observables
- No Shadowing, Anti-Shadowing
- Sum Rules: Momentum and J^z
- DGLAP Evolution; mod. at large x
- No Diffractive DIS



Dynamic

- Modified by Rescattering: ISI & FSI
- Contains Wilson Line, Phases
- No Probabilistic Interpretation
- Process-Dependent - From Collision
- T-Odd (Sivers, Boer-Mulders, etc.)
- Shadowing, Anti-Shadowing, Saturation
- Sum Rules Not Proven 
- DGLAP Evolution
- Hard Pomeron and Odderon Diffractive DIS



What is measured!

Hwang, Schmidt, sjb,

Mulders, Boer

Qiu, Sterman

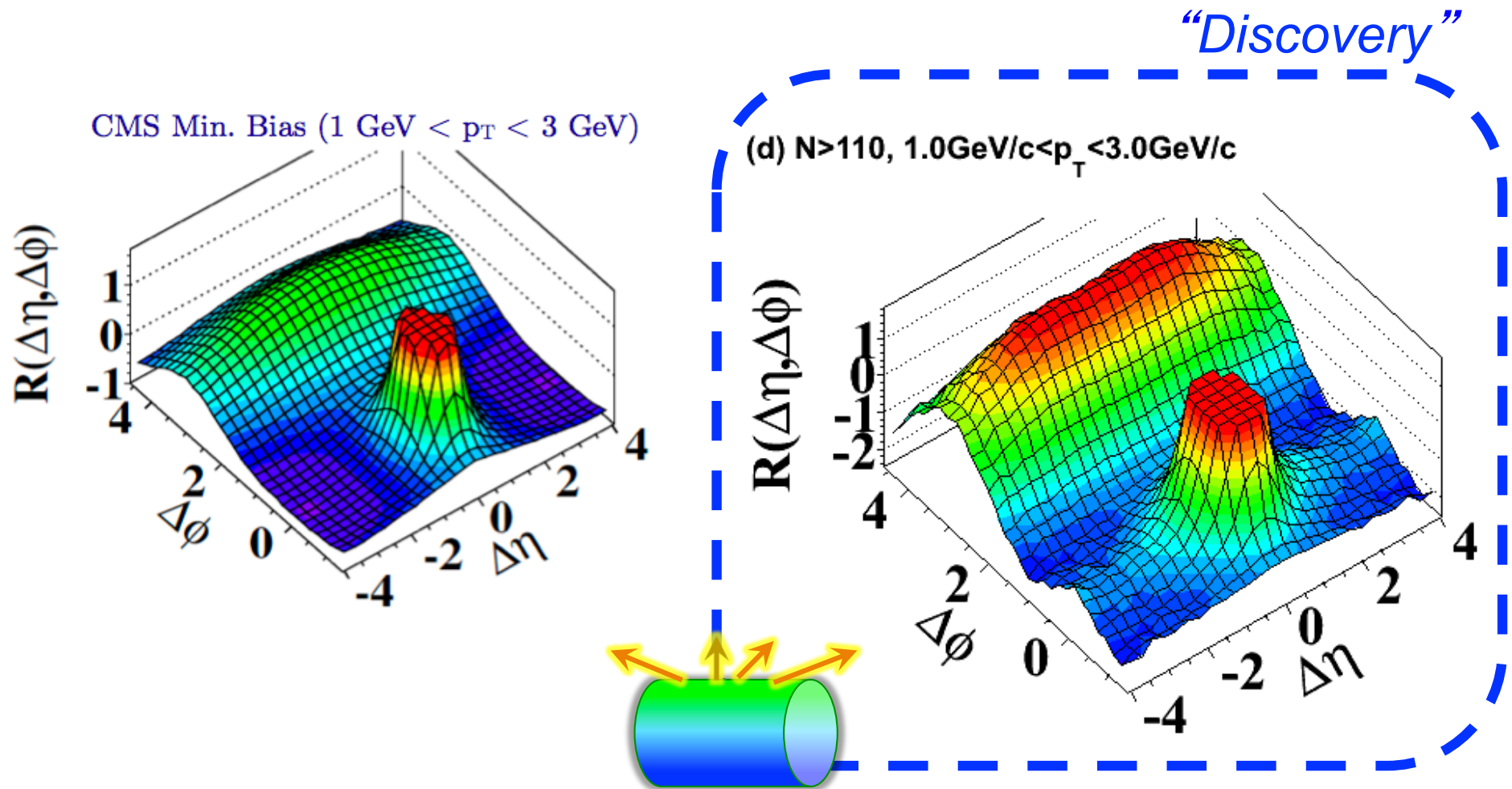
Collins, Qiu

Pasquini, Xiao, Yuan, sjb

Liuti, sjb

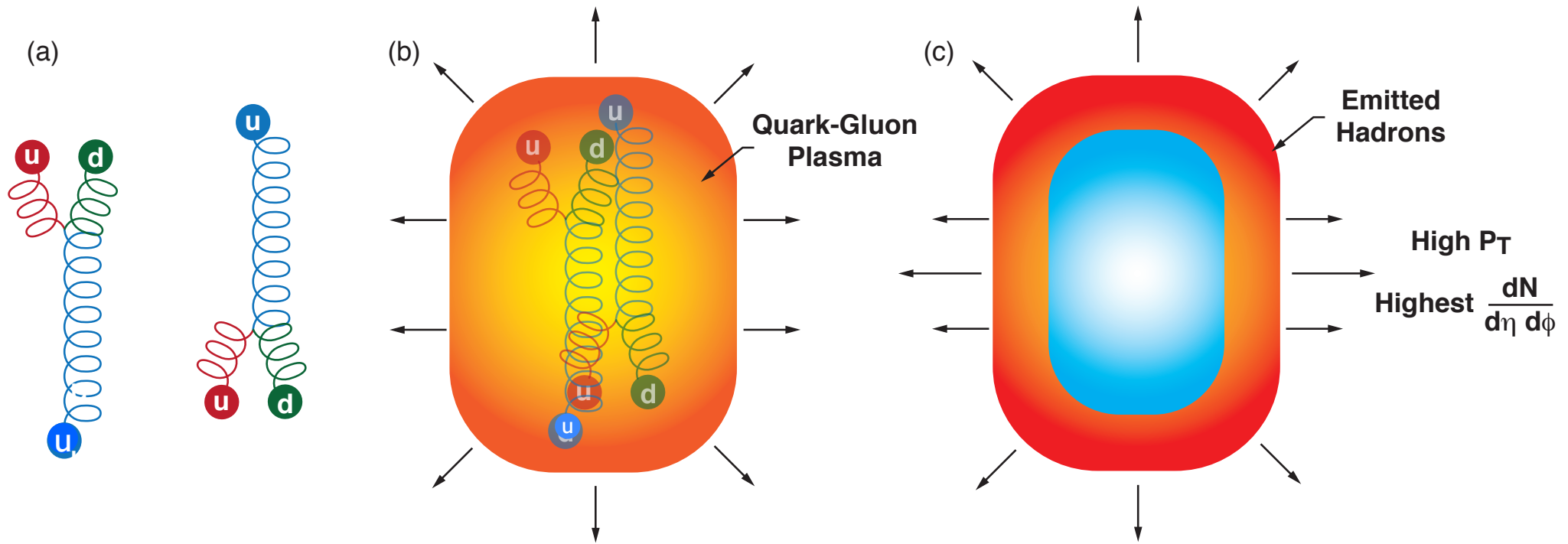
Ridge in high-multiplicity $p p$ collisions

Two-particle correlations: CMS results



- ◆ Ridge: Distinct long range correlation in η collimated around $\Delta\Phi \approx 0$ for two hadrons in the intermediate $1 < p_T, q_T < 3 \text{ GeV}$

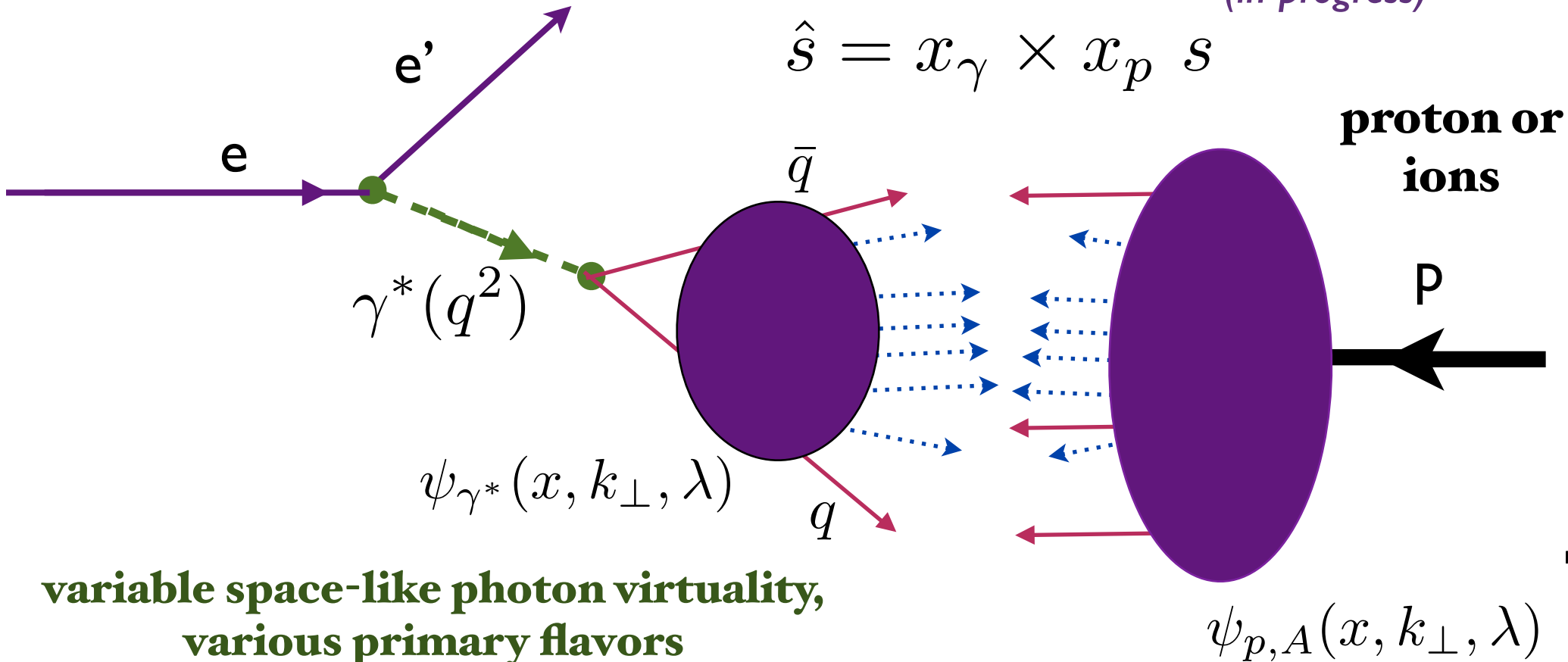
Ridge may reflect collision of aligned flux tubes



Electron-Ion Collider: Virtual Photon-Ion Collider

Perspective from the e-p collider frame

S. Glazek, P. Kubiczek, sjb
(in progress)

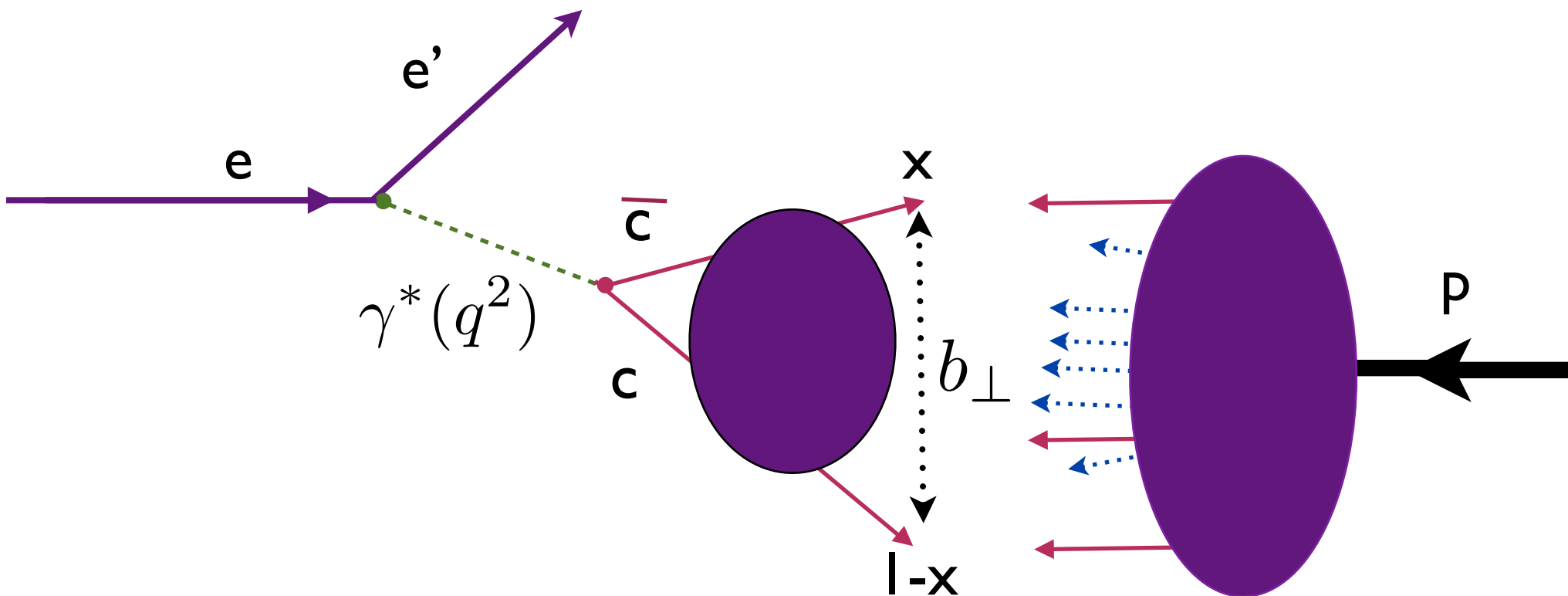


$\bar{q} q$ plane aligned with lepton scattering plane $\sim \cos^2\phi$

Front-surface dynamics: shadowing/antishadowing

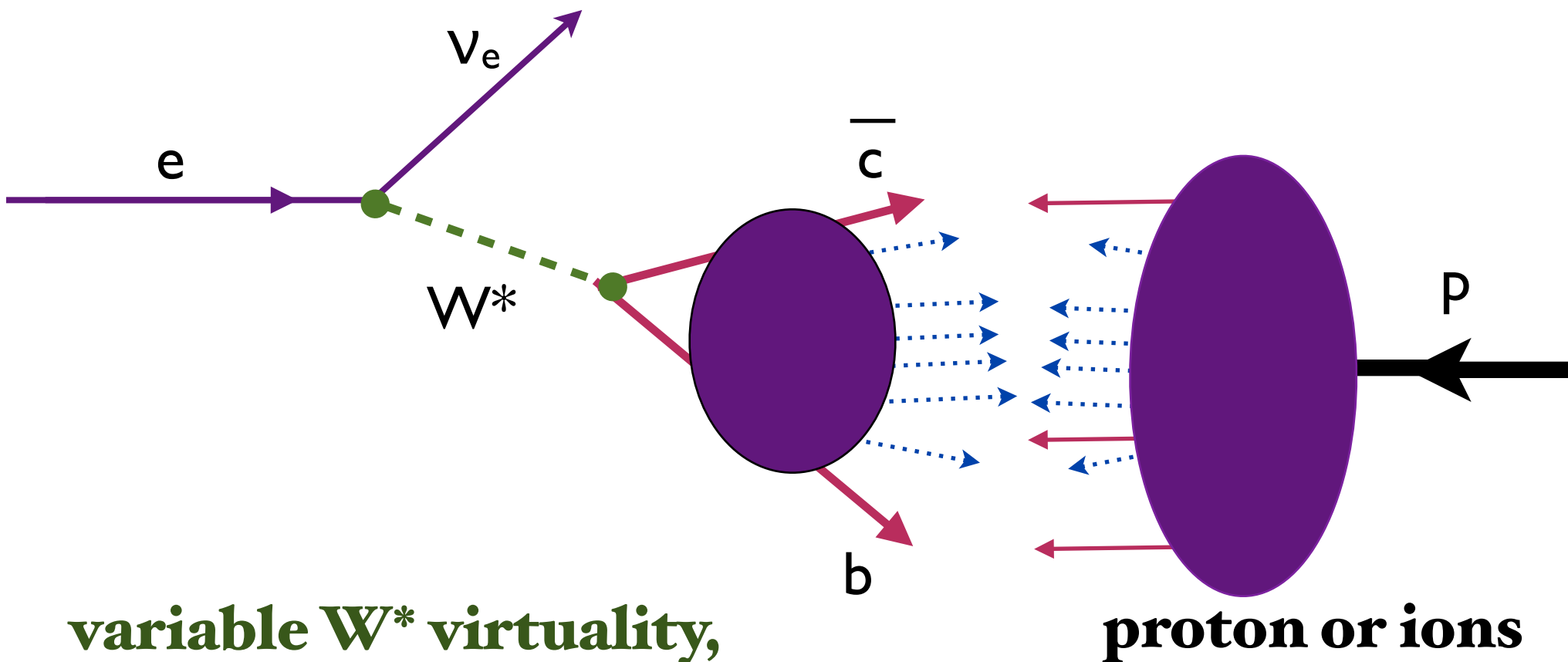
$\bar{c}c$ acts as a 'drill'

$$\langle b_{\perp}^2 \rangle \sim \frac{1}{Q^2 x(1-x) + m_c^2}$$



High Q^2 virtual photon at an EIC acts as a precision, small bore, linearly oriented, flavor-dependent probe acting on a proton or nuclear target.
Study final-state hadron multiplicity distributions, ridges, nuclear dependence, etc.

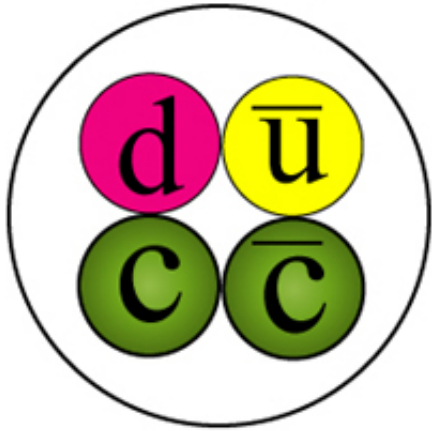
EIC: Virtual Weak Boson-Proton Collider



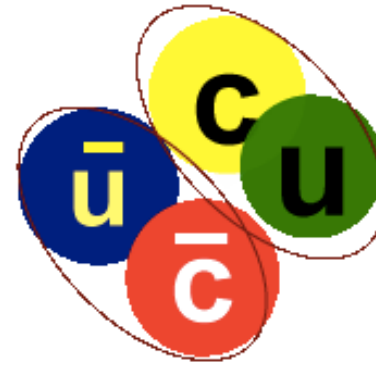
**variable W^* virtuality,
variable flavors**

proton or ions

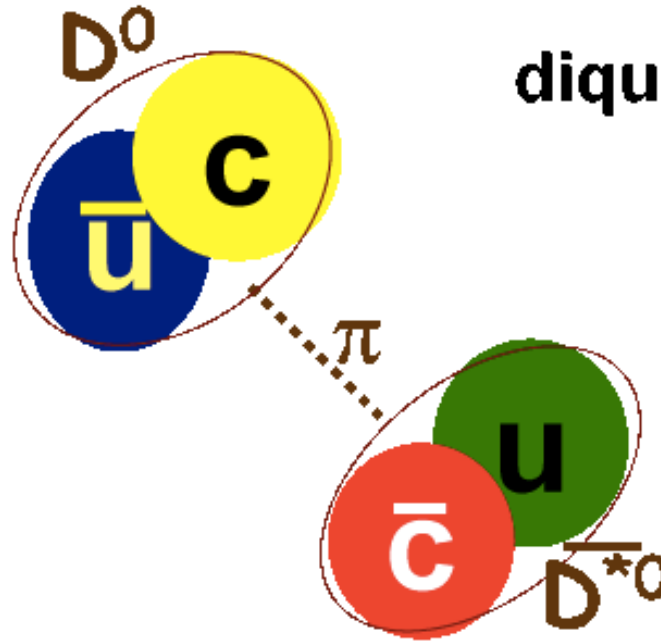
Z(4430)



$[\bar{u}\bar{c}]_{3C} [uc]_{\bar{3}C}$ diquarks



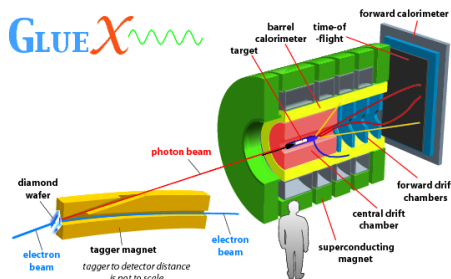
diquark-diantiquark



D⁰ – D^{*0} “molecule”

*Novel Nuclear
Photo- and Electroproduction Physics*

JLab, April 29, 2016



Stan Brodsky



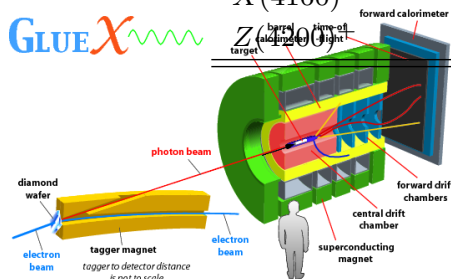
Four-Quark Hadrons: an Updated Review

arXiv:1411.5997v2

A. ESPOSITO, L. GUERRIERI, F. PICCININI, A. PILLONI and A. POLOSA

State	M (MeV)	Γ (MeV)	J^{PC}	Process (mode)	Experiment ($\#\sigma$)
$X(3823)$	3823.1 ± 1.9	< 24	$?^{? -}$	$B \rightarrow K(\chi_{c1}\gamma)$	Belle ²³ (4.0)
$X(3872)$	3871.68 ± 0.17	< 1.2	1^{++}	$B \rightarrow K(\pi^+\pi^- J/\psi)$ $p\bar{p} \rightarrow (\pi^+\pi^- J/\psi) \dots$ $pp \rightarrow (\pi^+\pi^- J/\psi) \dots$ $B \rightarrow K(\pi^+\pi^-\pi^0 J/\psi)$ $B \rightarrow K(\gamma J/\psi)$ $B \rightarrow K(\gamma \psi(2S))$	Belle ^{24,25} (>10), BABAR ²⁶ (8.6) CDF ^{27,28} (11.6), D0 ²⁹ (5.2) LHCb ^{30,31} (np) Belle ³² (4.3), BABAR ³³ (4.0) Belle ³⁴ (5.5), BABAR ³⁵ (3.5) LHCb ³⁶ (> 10) BABAR ³⁵ (3.6), Belle ³⁴ (0.2) LHCb ³⁶ (4.4)
$Z_c(3900)^+$	3888.7 ± 3.4	35 ± 7	1^{+-}	$Y(4260) \rightarrow \pi^-(D\bar{D}^*)^+$ $Y(4260) \rightarrow \pi^-(\pi^+ J/\psi)$	BES III ³⁹ (np) BES III ⁴⁰ (8), Belle ⁴¹ (5.2) CLEO data ⁴² (>5)
$Z_c(4020)^+$	4023.9 ± 2.4	10 ± 6	1^{+-}	$Y(4260) \rightarrow \pi^-(\pi^+ h_c)$ $Y(4260) \rightarrow \pi^-(D^* \bar{D}^*)^+$	BES III ⁴³ (8.9) BES III ⁴⁴ (10)
$Y(3915)$	3918.4 ± 1.9	20 ± 5	0^{++}	$B \rightarrow K(\omega J/\psi)$ $e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle ⁴⁵ (8), BABAR ^{33,46} (19) Belle ⁴⁷ (7.7), BABAR ⁴⁸ (7.6)
$Z(3930)$	3927.2 ± 2.6	24 ± 6	2^{++}	$e^+e^- \rightarrow e^+e^-(D\bar{D})$	Belle ⁴⁹ (5.3), BABAR ⁵⁰ (5.8)
$X(3940)$	3942^{+9}_{-8}	37^{+27}_{-17}	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D\bar{D}^*)$	Belle ^{51,52} (6)
$Y(4008)$	3891 ± 42	255 ± 42	1^{--}	$e^+e^- \rightarrow (\pi^+\pi^- J/\psi)$	Belle ^{41,53} (7.4)
$Z(4050)^+$	4051^{+24}_{-43}	82^{+51}_{-55}	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+\chi_{c1})$	Belle ⁵⁴ (5.0), BABAR ⁵⁵ (1.1)
$Y(4140)$	4145.6 ± 3.6	14.3 ± 5.9	$?^{?+}$	$B^+ \rightarrow K^+(\phi J/\psi)$	CDF ^{56,57} (5.0), Belle ⁵⁸ (1.9), LHCb ⁵⁹ (1.4), CMS ⁶⁰ (>5) DØ ⁶¹ (3.1)
$X(4160)$	4156^{+29}_{-25}	139^{+113}_{-65}	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D^* \bar{D}^*)$	Belle ⁵² (5.5)
$Z(4200)^0$	4196^{+35}_{-30}	370^{+99}_{-110}	1^{+-}	$\bar{B}^0 \rightarrow K^-(\pi^+ J/\psi)$	Belle ⁶² (7.2)

GLUEX



Novel Nuclear
Photo- and Electroproduction Physics

Stan Brodsky

JLab, April 29, 2016

SLAC
NATIONAL ACCELERATOR LABORATORY

New World of Tetraquarks

$$3_C \times 3_C = \bar{3}_C + 6_C$$

Bound!

- Diquark Color-Confined Constituents: Color $\bar{3}_C$
- Diquark-Antidiquark bound states
- Confinement Force Similar to quark-antiquark $\bar{3}_C \times 3_C = 1_C$ mesons
- Isospin $I = 0, \pm 1, \pm 2$ Charge $Q = 0, \pm 1, \pm 2$

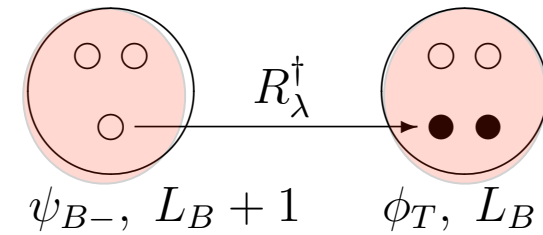
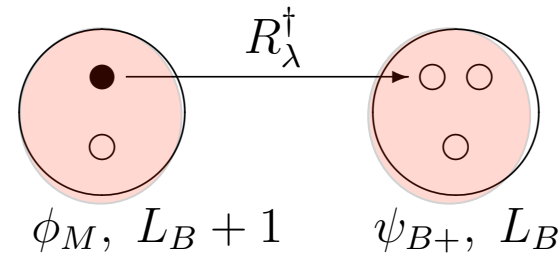
Complete Regge spectrum in n, L



Superconformal Algebra

2X2 Hadronic Multiplets $\begin{pmatrix} \phi_M(L_M = L_B + 1) & \psi_{B-}(L_B + 1) \\ \psi_{B+}(L_B) & \phi_T(L_T = L_B) \end{pmatrix}$

- quark-antiquark meson ($L_M = L_{B+I}$)
- quark-diquark baryon (L_B)
- quark-diquark baryon (L_{B+I})
- diquark-antidiquark tetraquark ($L_T = L_B$)
- Universal Regge slopes $\lambda = \kappa^2$



$$M_H^2/\lambda = \underbrace{(2n + L_H + 1)}_{\text{kinetic}} + \underbrace{(2n + L_H + 1)}_{\text{potential}} + \underbrace{2(L_H + s) + 2\chi}_{\text{contribution from AdS and superconformal algebra}} + \left\langle \sum_i \frac{m_i^2}{x_i} \right\rangle$$

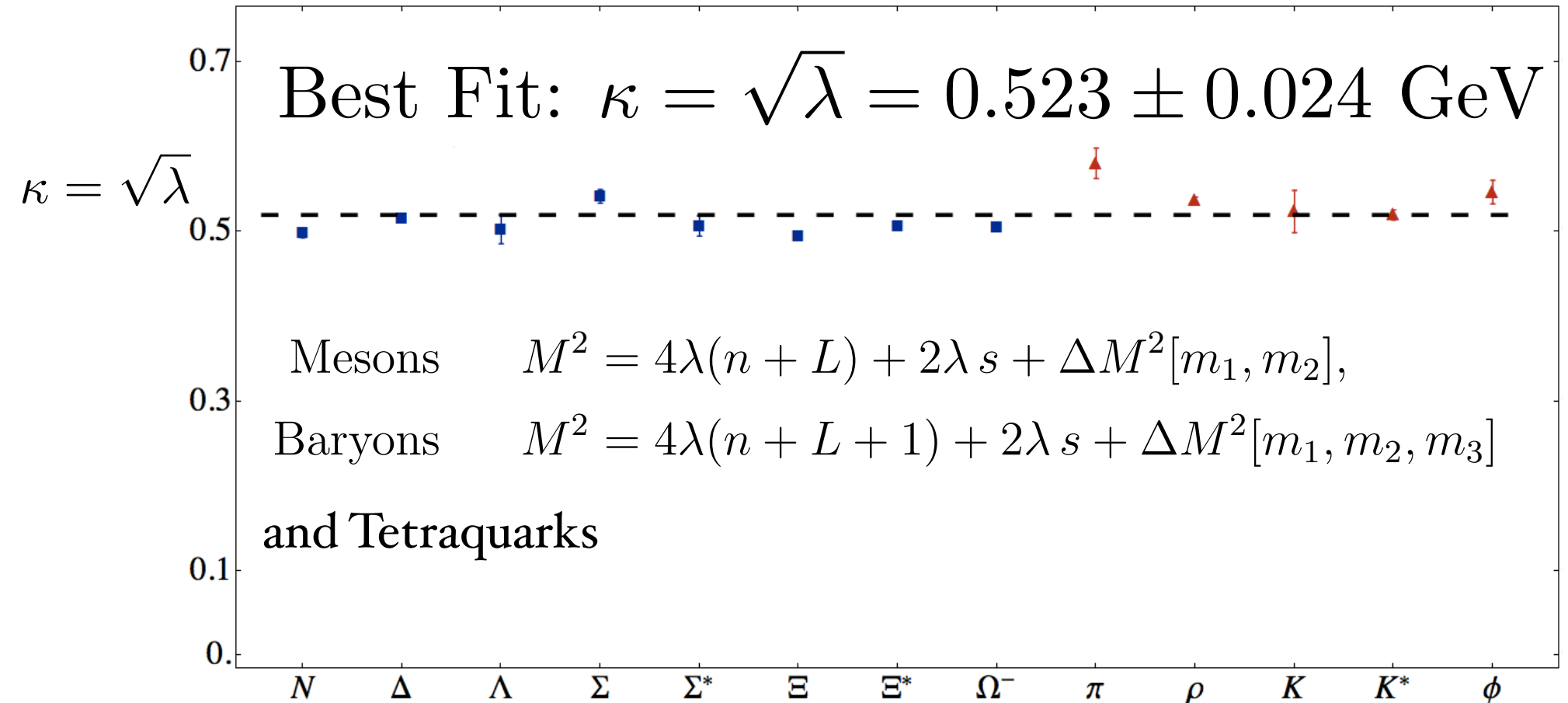
$$\chi(\text{mesons}) = -1$$

$$\chi(\text{baryons, tetraquarks}) = +1$$

- Universal Regge slopes

*Dosch, de Teramond,
Lorce, sjb*

$$M_H^2 = 4\lambda(n + L) + \dots$$



Best fit for the value of the hadronic scale $\sqrt{\lambda}$ for the different Regge trajectories for baryons and mesons including all radial and orbital excitations using Eqs. (23) and (24). The dotted line is the average value $\sqrt{\lambda} = 0.523$ GeV; it has the standard deviation $\sigma = 0.024$ GeV. For the baryon sample alone the values are 0.509 ± 0.015 GeV and for the mesons 0.524 ± 0.023 GeV.

New World of Tetraquarks

$$3_C \times 3_C = \bar{3}_C + 6_C$$

Bound!

- Diquark: Color-Confined Constituents: Color $\bar{3}_C$
- Diquark-Antidiquark bound states $\bar{3}_C \times 3_C = 1_C$

$$\sigma(TN) \simeq 2\sigma(pN) - \sigma(\pi N)$$

$$2[\sigma(\{\{qq\}N) + \sigma(qN)] - [\sigma(qN) + \sigma(\bar{q}N)] = [\sigma(\{qq\}N) + \sigma(\{qq\}N)]$$

Candidates $f_0(980)I = 0, J^P = 0^+$, partner of proton

$a_1(1260)I = 0, J^P = 1^+$, partner of $\Delta(1233)$

Belle, BaBar:

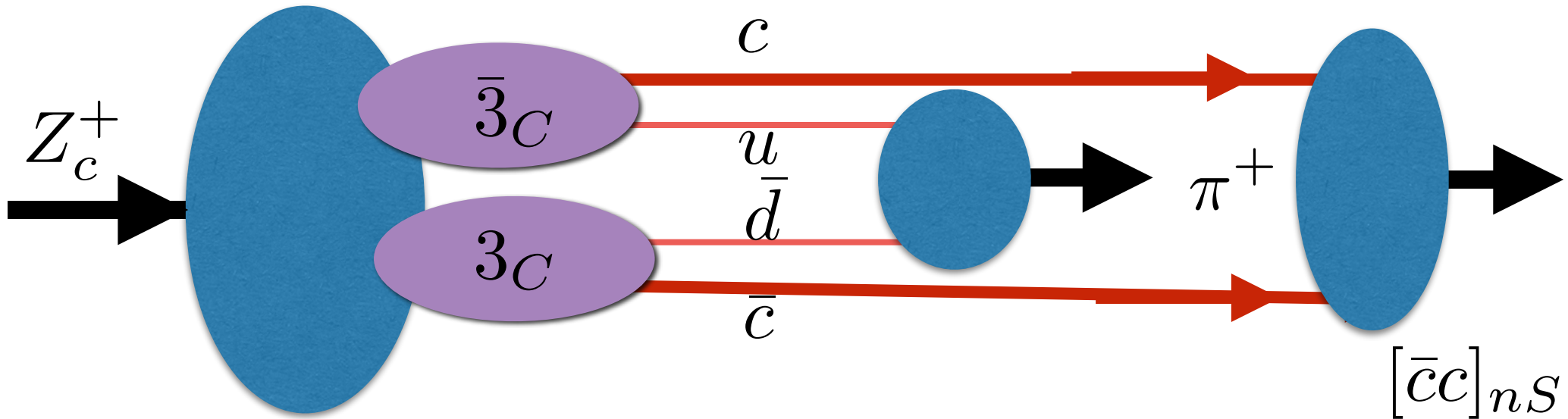
$$\mathcal{B}(B^0 \rightarrow K^+ Z(4430)^-) \times \mathcal{B}(Z(4430)^- \rightarrow \psi(2S)\pi^-) = (6.0_{-2.0}^{+1.7+2.5}) \times 10^{-5}.$$

$$\mathcal{B}(B^0 \rightarrow K^+ Z(4430)^-) \times \mathcal{B}(Z(4430)^- \rightarrow J/\psi \pi^-) = (5.4_{-1.0}^{+4.0+1.1}) \times 10^{-6}.$$

Surprising Result:

Dominance of large size $\psi'(2S)$ vs. J/ψ decays

Diquark Anti-diquark Model



$$Z_c^+ ([cu]_{3C} [\bar{c}\bar{d}]_{\bar{3}C}) \rightarrow \pi^+ \psi'$$

Formation of charmonium at large separation:

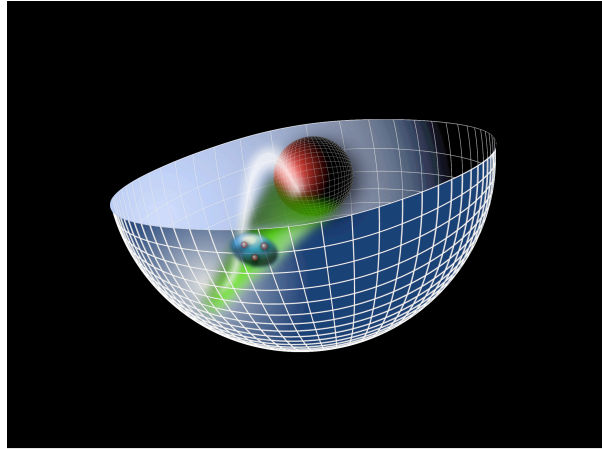
Dominance of overlap with large-size Ψ' vs J/Ψ decays

Lebed, Hwang, sjb

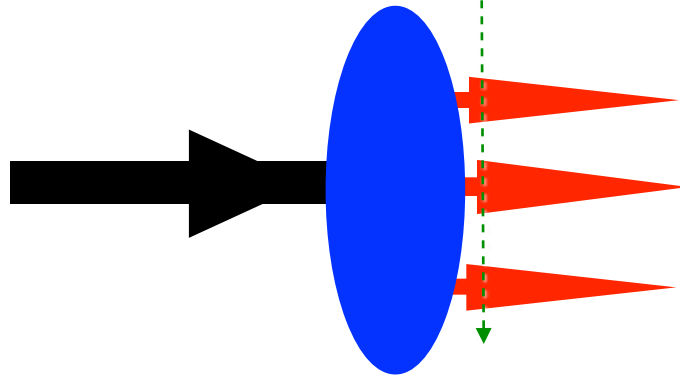
$$\phi(z)$$

AdS₅: Conformal Template for QCD

- Light-Front Holography*

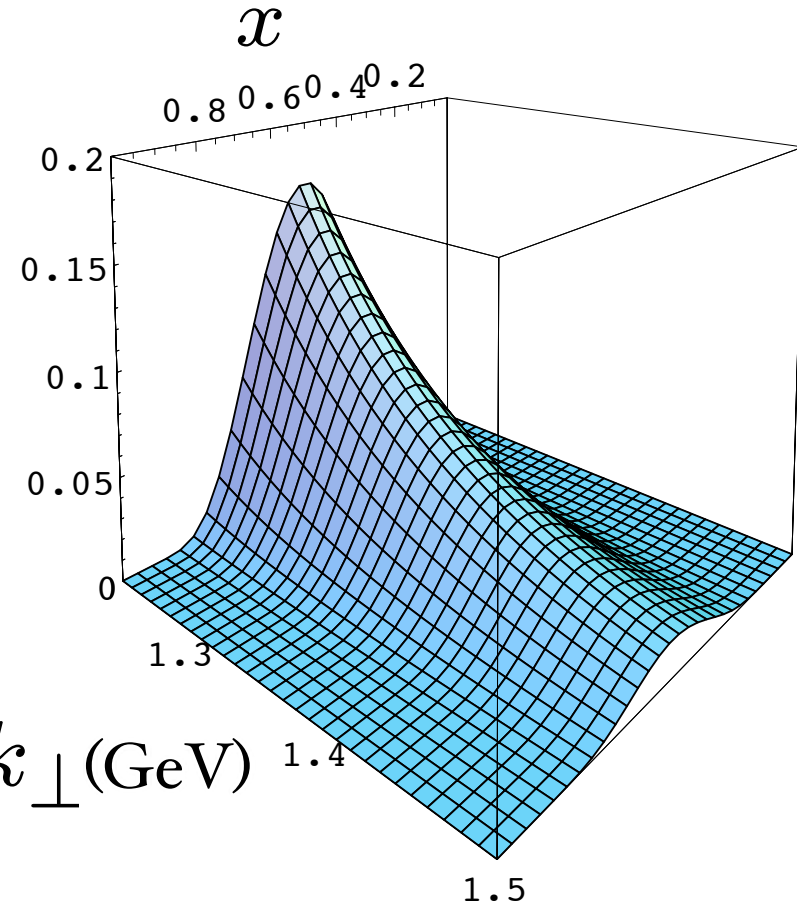


Fixed $\tau = t + z/c$



$$\Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

Duality of AdS₅ with LF Hamiltonian Theory



- Light Front Wavefunctions:*

**Light-Front Schrödinger Equation
Spectroscopy and Dynamics**

with Guy de Teramond, Alexandre Deur,
Cedric Lorce, Hans Guenter Dosch

QCD Lagrangian

$$\mathcal{L}_{QCD} = -\frac{1}{4} \text{Tr}(G^{\mu\nu} G_{\mu\nu}) + \sum_{f=1}^{n_f} i \bar{\Psi}_f D_\mu \gamma^\mu \Psi_f + \sum_{f=1}^{n_f} m_f \bar{\Psi}_f \Psi_f$$

$$iD^\mu = i\partial^\mu - gA^\mu \quad G^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu - g[A^\mu, A^\nu]$$

Classical Chiral Lagrangian is Conformally Invariant

Where does the QCD Mass Scale Λ_{QCD} come from?

How does color confinement arise?

- de Alfaro, Fubini, Furlan:

Scale can appear in Hamiltonian and EQM without affecting conformal invariance of action!

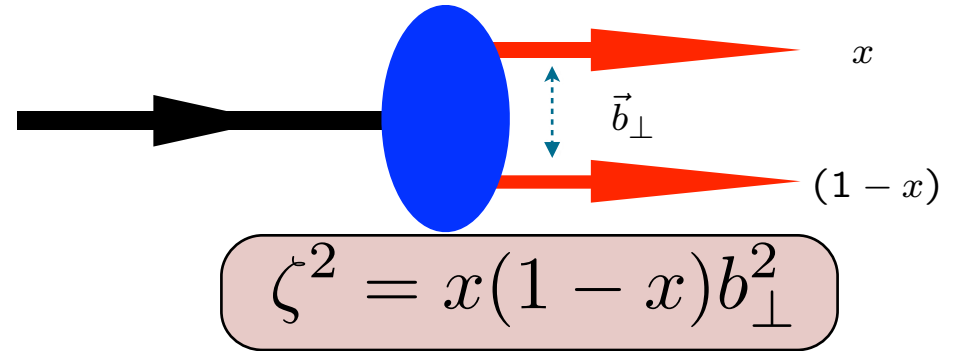
Unique confinement potential!

Light-Front QCD

Fixed $\tau = t + z/c$

\mathcal{L}_{QCD}

H_{QCD}^{LF}



Coupled Fock states

$$(H_{LF}^0 + H_{LF}^I) |\Psi\rangle = M^2 |\Psi\rangle$$

Eliminate higher Fock states and retarded interactions

$$\left[\frac{\vec{k}_\perp^2 + m^2}{x(1-x)} + V_{\text{eff}}^{LF} \right] \psi_{LF}(x, \vec{k}_\perp) = M^2 \psi_{LF}(x, \vec{k}_\perp)$$

Effective two-particle equation

$$\left[-\frac{d^2}{d\zeta^2} + \frac{1 - 4L^2}{4\zeta^2} + U(\zeta) \right] \psi(\zeta) = \mathcal{M}^2 \psi(\zeta)$$

Azimuthal Basis

$$\zeta, \phi$$

$$m_q = 0$$

AdS/QCD:

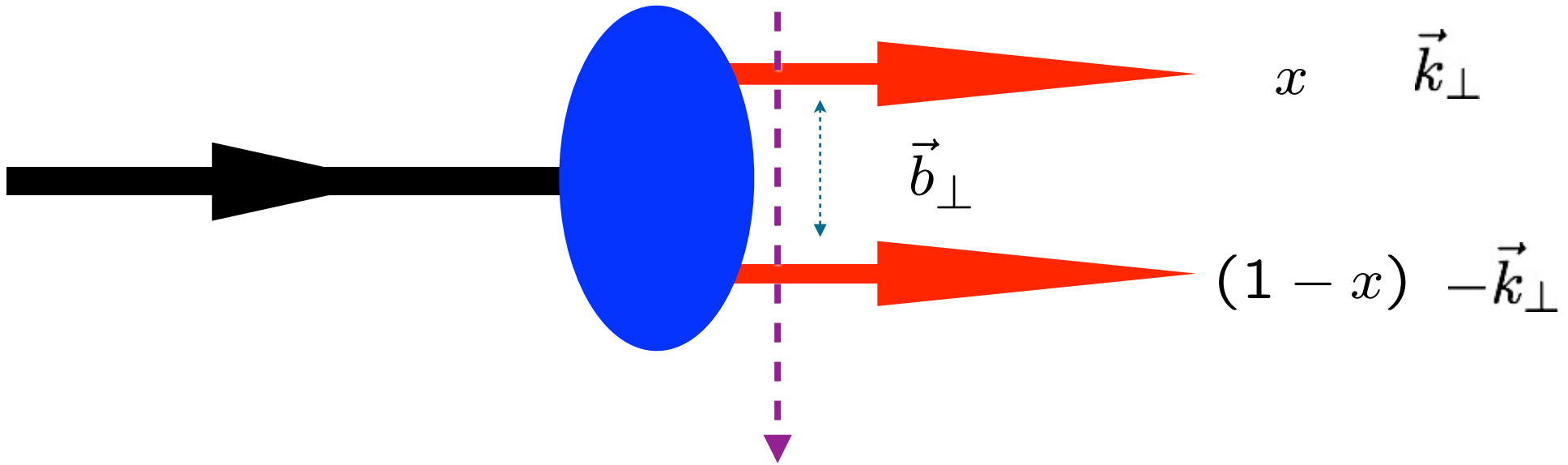
Confining AdS/QCD potential!

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2 (L + S - 1)$$

Sums an infinite # diagrams

Semiclassical first approximation to QCD

Fixed $\tau = t + z/c$



$$\zeta^2 \equiv b_{\perp}^2 x(1-x)$$

Invariant transverse separation

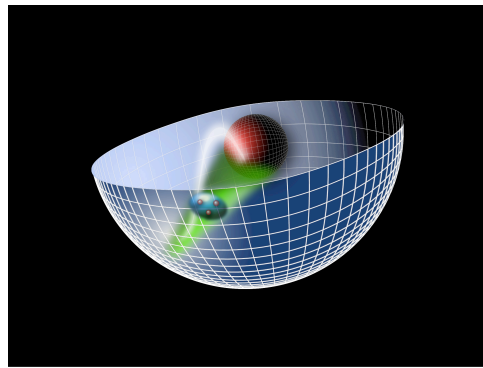
$$\zeta^2 \text{ conjugate to } \frac{k_{\perp}^2}{x(1-x)} = (p_q + p_{\bar{q}})^2 = \mathcal{M}_{q+\bar{q}}^2$$

$$\int dk^- \Psi_{BS}(P, k) \rightarrow \psi_{LF}(x, \vec{k}_{\perp})$$

*AdS/QCD
Soft-Wall Model*

$$e^{\varphi(z)} = e^{+\kappa^2 z^2}$$

*Single scheme-independent
fundamental mass scale*



Light-Front Holography

$$\zeta^2 = x(1-x)b_{\perp}^2.$$

$$\left[-\frac{d^2}{d\zeta^2} + \frac{1-4L^2}{4\zeta^2} + U(\zeta) \right] \psi(\zeta) = \mathcal{M}^2 \psi(\zeta)$$



Light-Front Schrödinger Equation

$$U(\zeta) = \kappa^4 \zeta^2 + 2\kappa^2(L + S - 1)$$

***Unique
Confinement Potential!***

*Preserves Conformal Symmetry
of the action*

Confinement scale:

$$\kappa \simeq 0.6 \text{ GeV}$$

$$1/\kappa \simeq 1/3 \text{ fm}$$

$$m_q = 0$$

- de Alfaro, Fubini, Furlan:
- Fubini, Rabinovici:

***Scale can appear in Hamiltonian and EQM
without affecting conformal invariance of action!***

Light-Front Schrödinger Equation

G. de Teramond, sjb

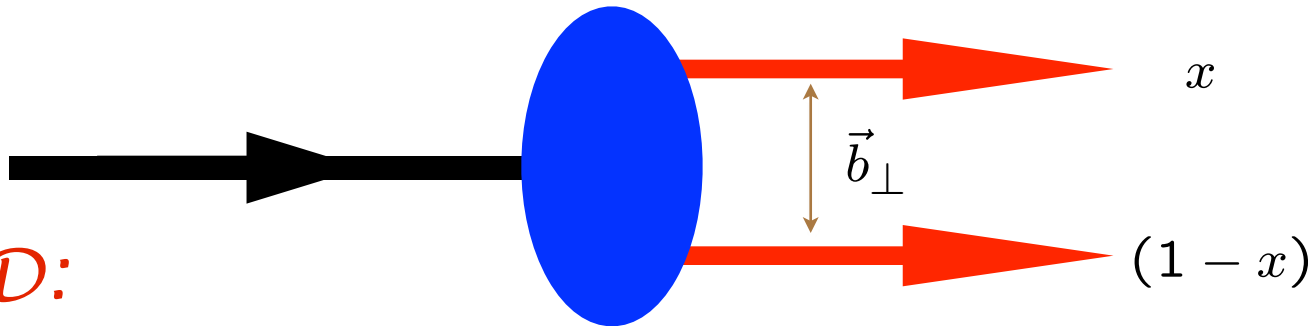
Relativistic LF single-variable radial
equation for QCD & QED

Frame Independent!

$$\left[-\frac{d^2}{d\zeta^2} + \frac{m^2}{x(1-x)} + \frac{-1 + 4L^2}{\zeta^2} + U(\zeta, S, L) \right] \psi_{LF}(\zeta) = M^2 \psi_{LF}(\zeta)$$

$$m_q \sim 0$$

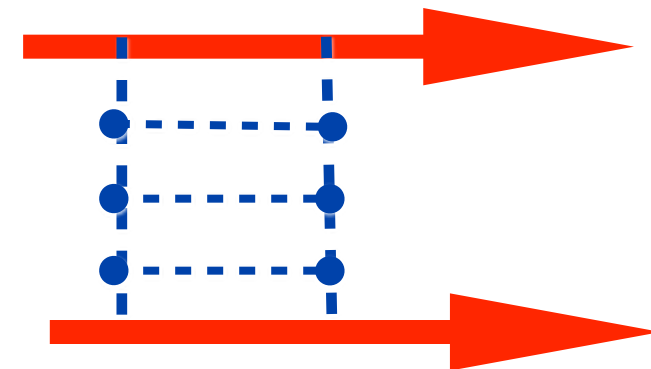
$$\zeta^2 = x(1-x)\mathbf{b}_\perp^2.$$



AdS/QCD:

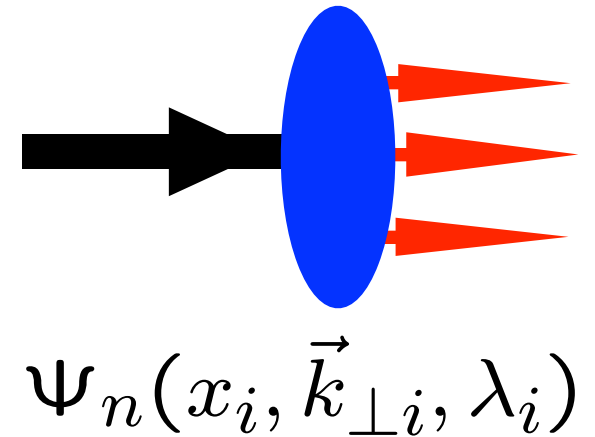
$$U(\zeta, S, L) = \kappa^2 \zeta^2 + \kappa^2 (L + S - 1/2)$$

U is the exact QCD potential
Conjecture: 'H'-diagrams generate U?



AdS/QCD and Light-Front Holography

- A first, semi-classical approximation to nonperturbative QCD
- Hadron Spectroscopy and LF Dynamics
- Color Confinement Potential
- Running QCD Coupling $\alpha(Q^2)$ at All Scales Q^2
- What sets the QCD Mass Scale?
- Connection of Hadron Masses to $\Lambda_{\overline{MS}}$



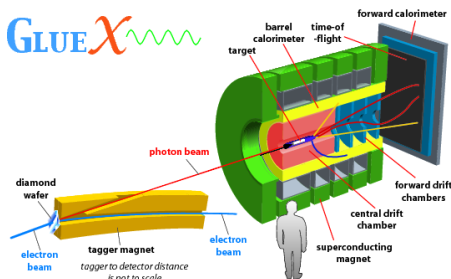
Dilaton-Modified AdS/QCD

$$ds^2 = e^{\varphi(z)} \frac{R^2}{z^2} (\eta_{\mu\nu} x^\mu x^\nu - dz^2)$$

- Soft-wall dilaton profile breaks conformal invariance

$$e^{\varphi(z)} = e^{+\kappa^2 z^2}$$

- Color Confinement
- Introduces confinement scale κ

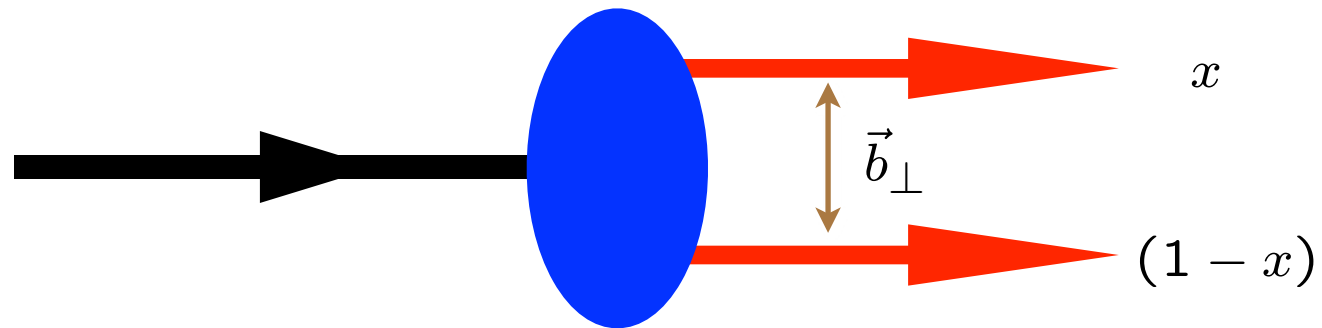


*Novel Nuclear
Photo- and Electroproduction Physics*

JLab, April 29, 2016

Stan Brodsky

SLAC
NATIONAL ACCELERATOR LABORATORY

$LF(3+1) \longleftrightarrow AdS_5$
 $\psi(x, \vec{b}_\perp) \longleftrightarrow \phi(z)$
 $\zeta = \sqrt{x(1-x)} \vec{b}_\perp^2 \longleftrightarrow z$


$$\psi(x, \zeta) = \sqrt{x(1-x)} \zeta^{-1/2} \phi(\zeta)$$

Light Front Holography: Unique mapping derived from equality of LF and AdS formula for EM and gravitational current matrix elements

Meson Spectrum in Soft Wall Model

Pion: Negative term for $J=0$ cancels positive terms from LFKÉ and potential



- Effective potential: $U(\zeta^2) = \kappa^4 \zeta^2 + 2\kappa^2(J - 1)$

- LF WE

$$\left(-\frac{d^2}{d\zeta^2} - \frac{1 - 4L^2}{4\zeta^2} + \kappa^4 \zeta^2 + 2\kappa^2(J - 1) \right) \phi_J(\zeta) = M^2 \phi_J(\zeta)$$

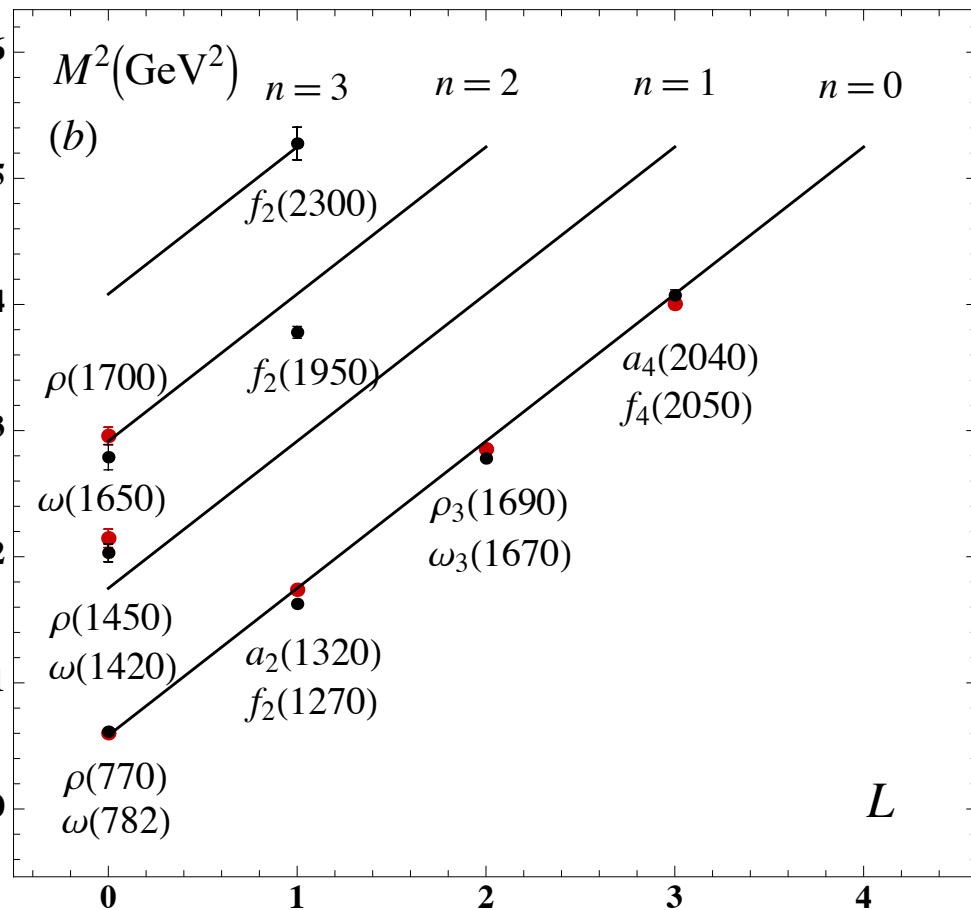
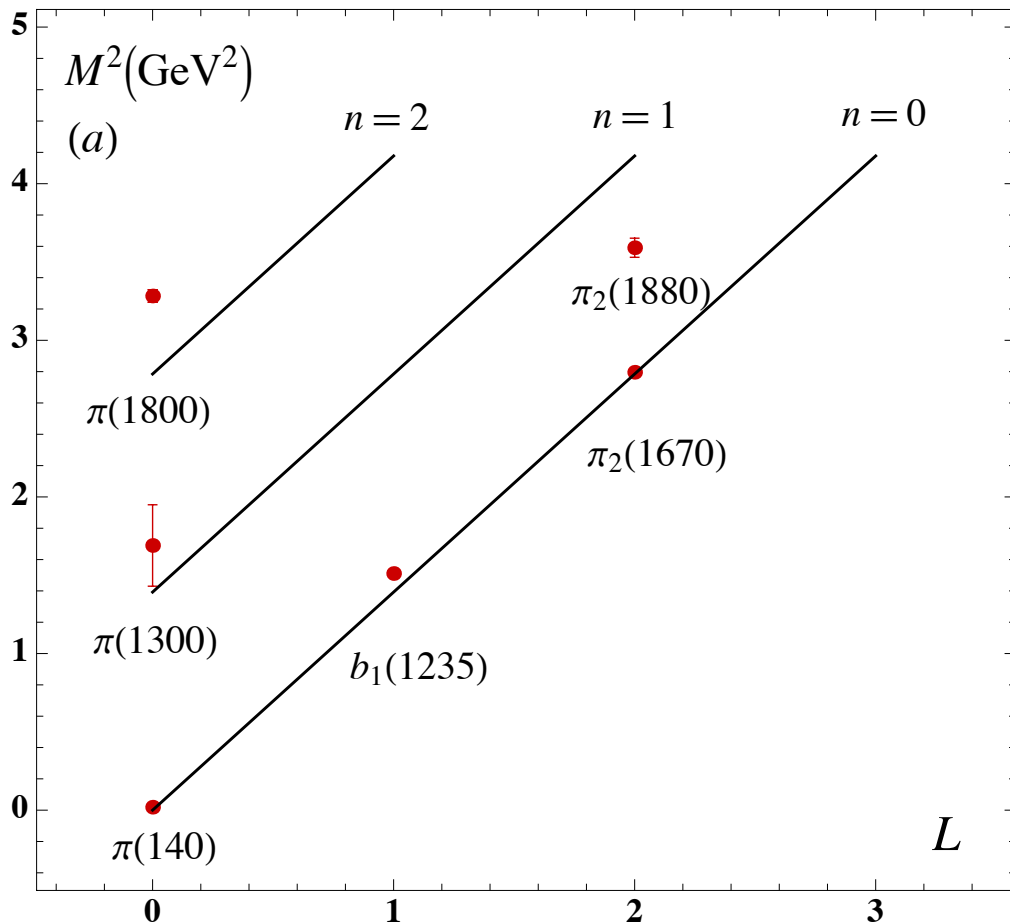
- Normalized eigenfunctions $\langle \phi | \phi \rangle = \int d\zeta \phi^2(z)^2 = 1$

$$\phi_{n,L}(\zeta) = \kappa^{1+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{1/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^L(\kappa^2 \zeta^2)$$

- Eigenvalues

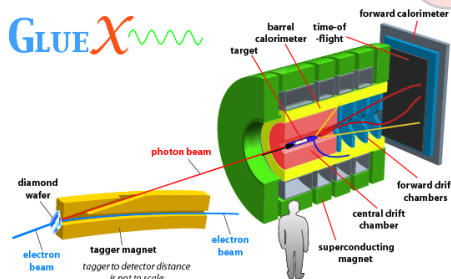
$$\mathcal{M}_{n,J,L}^2 = 4\kappa^2 \left(n + \frac{J+L}{2} \right)$$

Prediction from AdS/QCD



$$m_u = m_d = 0$$

$$M^2(n, L, S) = 4\kappa^2(n + L + S/2)$$



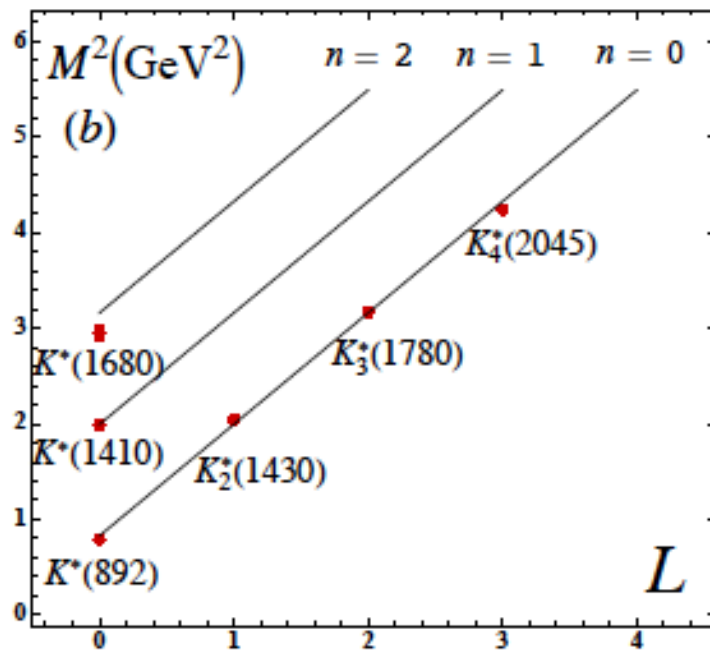
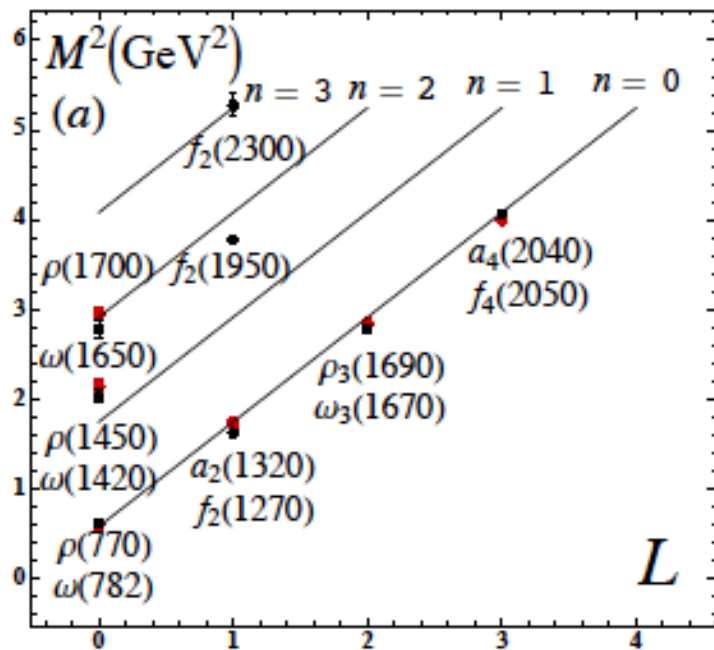
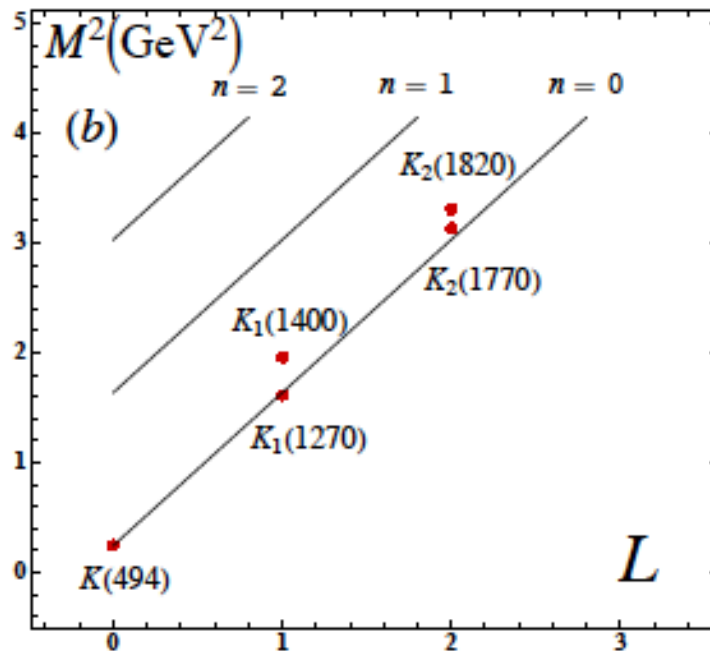
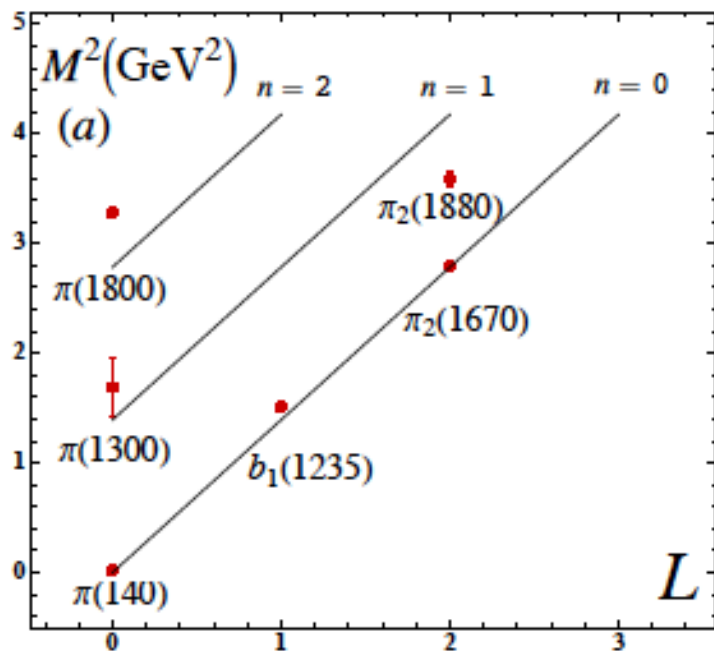
*Novel Nuclear
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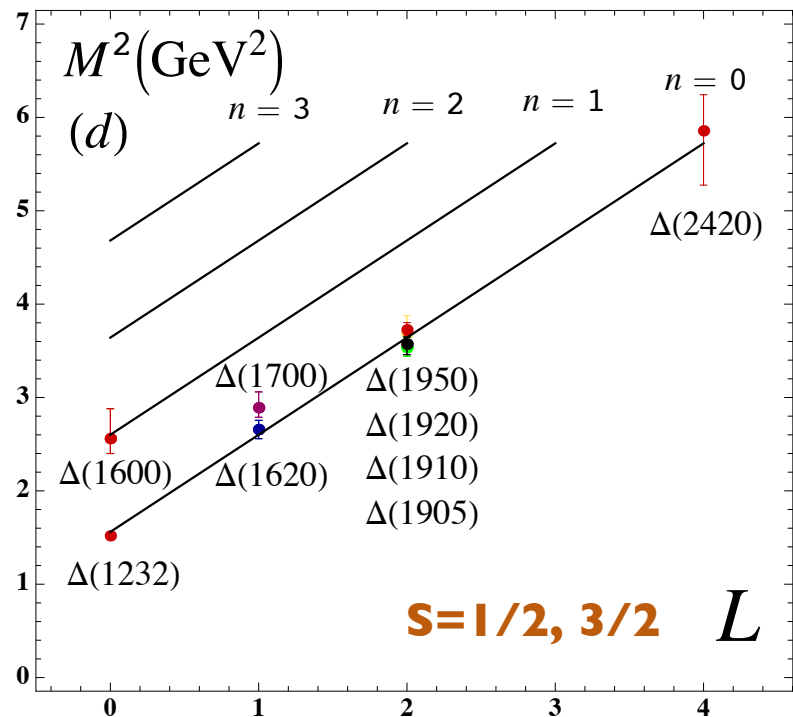
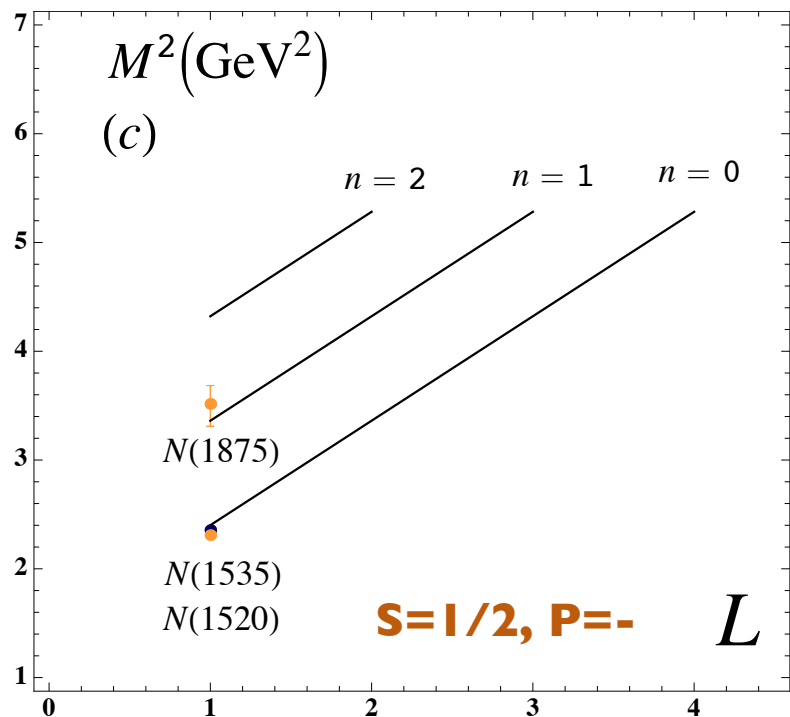
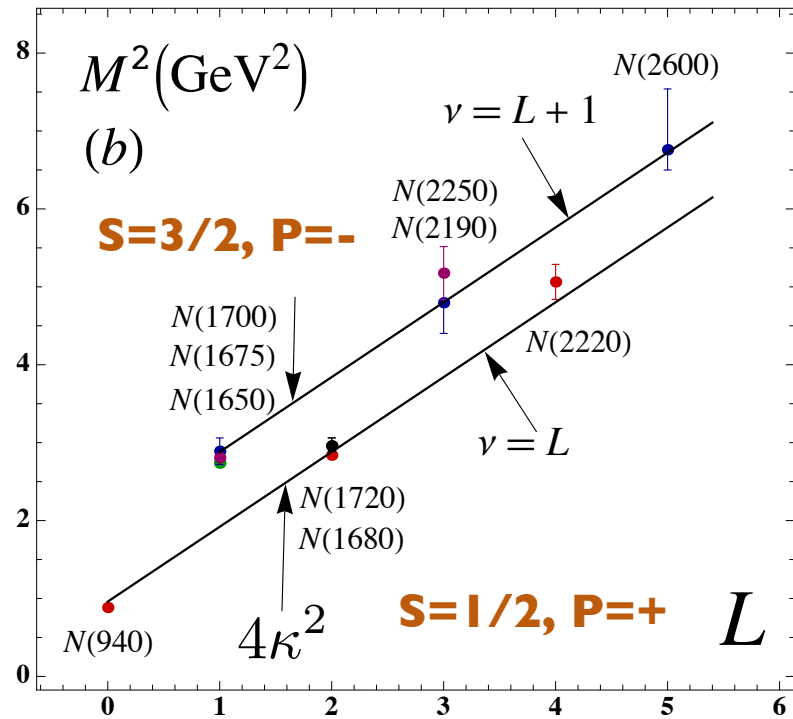
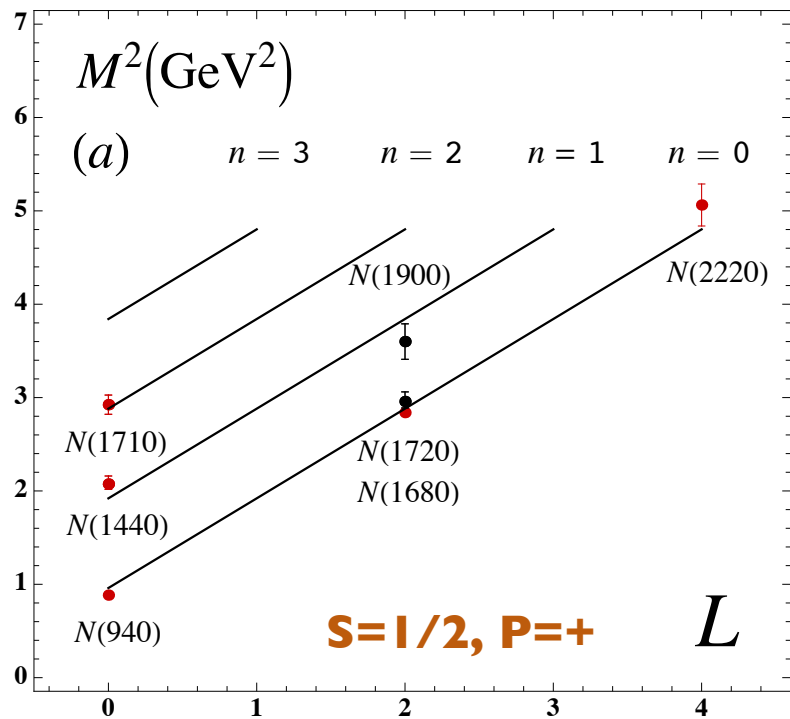
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$$M^2 = M_0^2 + \left\langle X \left| \frac{m_q^2}{x} \right| X \right\rangle + \left\langle X \left| \frac{m_{\bar{q}}^2}{1-x} \right| X \right\rangle$$





LF Holography

Baryon Equation

$$\left(-\partial_\zeta^2 + \kappa^4 \zeta^2 + 2\kappa^2(L_B + 1) + \frac{4L_B^2 - 1}{4\zeta^2}\right)\psi_J^+ = M^2\psi_J^+ \quad \text{G}_{22}$$

$$\left(-\partial_\zeta^2 + \kappa^4 \zeta^2 + 2\kappa^2 L_B + \frac{4(L_B + 1)^2 - 1}{4\zeta^2}\right)\psi_J^- = M^2\psi_J^- \quad \text{G}_{11}$$

$$M^2(n, L_B) = 4\kappa^2(n + L_B + 1)$$

S=1/2, P=+

both chiralities

Meson Equation

$$\left(-\partial_\zeta^2 + \kappa^4 \zeta^2 + 2\kappa^2(J - 1) + \frac{4L_M^2 - 1}{4\zeta^2}\right)\phi_J = M^2\phi_J \quad \text{G}_{11}$$

$$M^2(n, L_M) = 4\kappa^2(n + L_M)$$

Same κ !

S=0, I=I Meson is superpartner of S=1/2, I=I Baryon

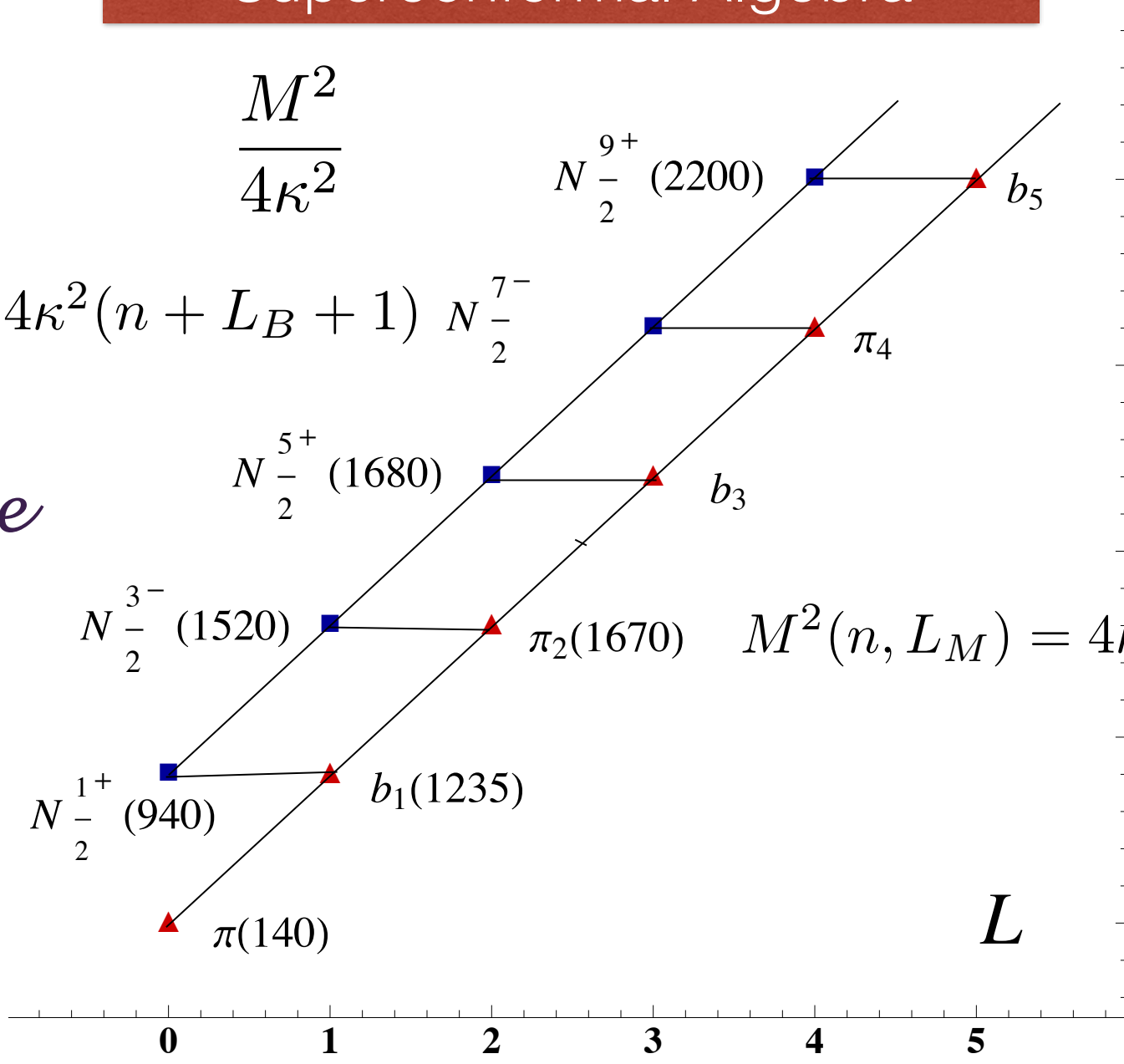
Meson-Baryon Degeneracy for $L_M=L_B+1$

Superconformal Algebra

$$\frac{M^2}{4\kappa^2}$$

$$M^2(n, L_B) = 4\kappa^2(n + L_B + 1) N_{\frac{7}{2}}^{7-}$$

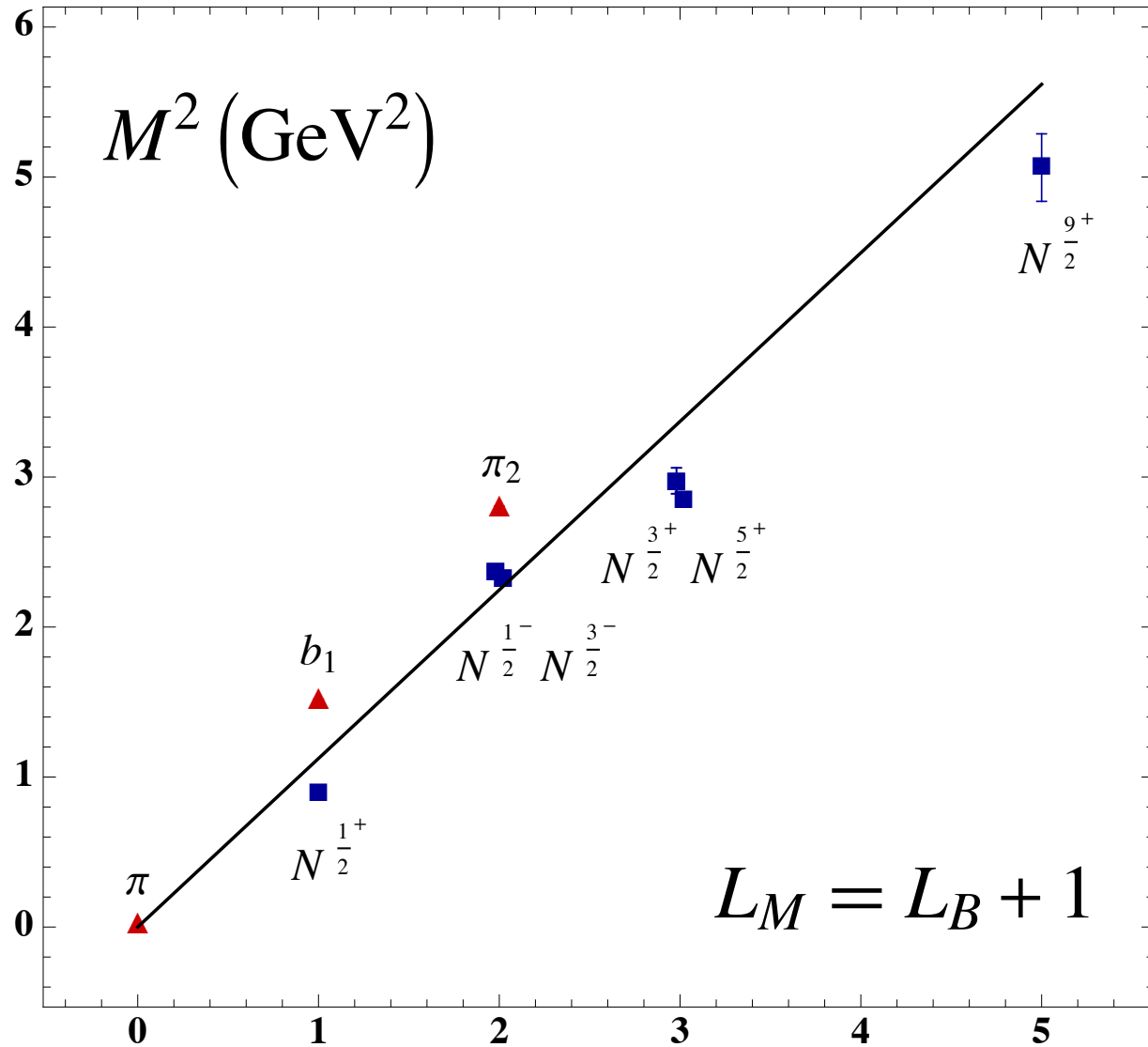
Same slope



$$M^2(n, L_M) = 4\kappa^2(n + L_M)$$

Meson-Baryon
Mass Degeneracy
for $L_M=L_B+1$

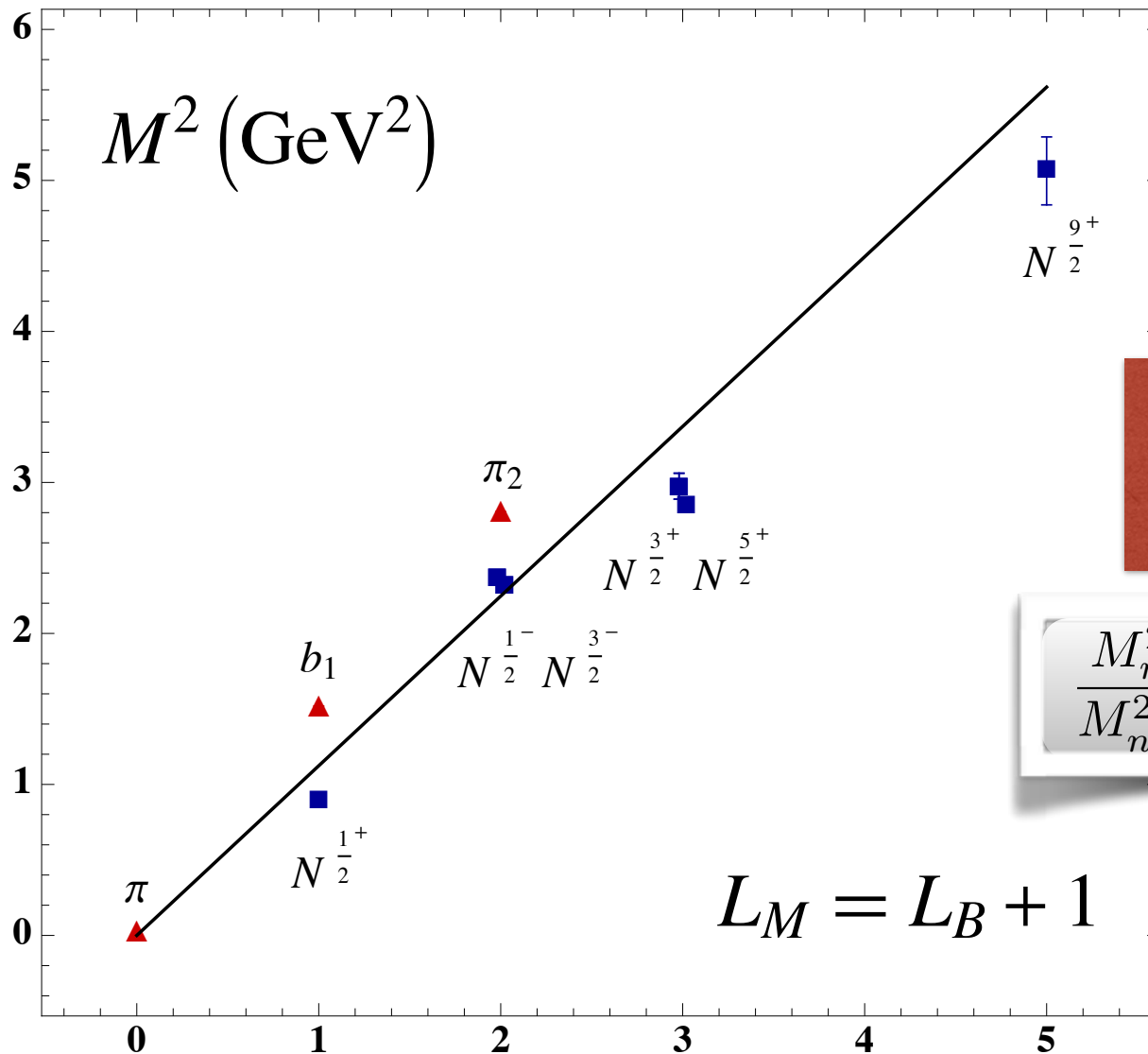
Superconformal AdS Light-Front Holographic QCD (LFHQCD): Identical meson and baryon spectra!



**Meson-Baryon
Mass Degeneracy
for $L_M=L_B+1$**

$S=0, I=I$ Meson is superpartner of $S=1/2, I=I$ Baryon

**Superconformal AdS Light-Front Holographic QCD (LFHQCD):
Identical meson and baryon spectra!**



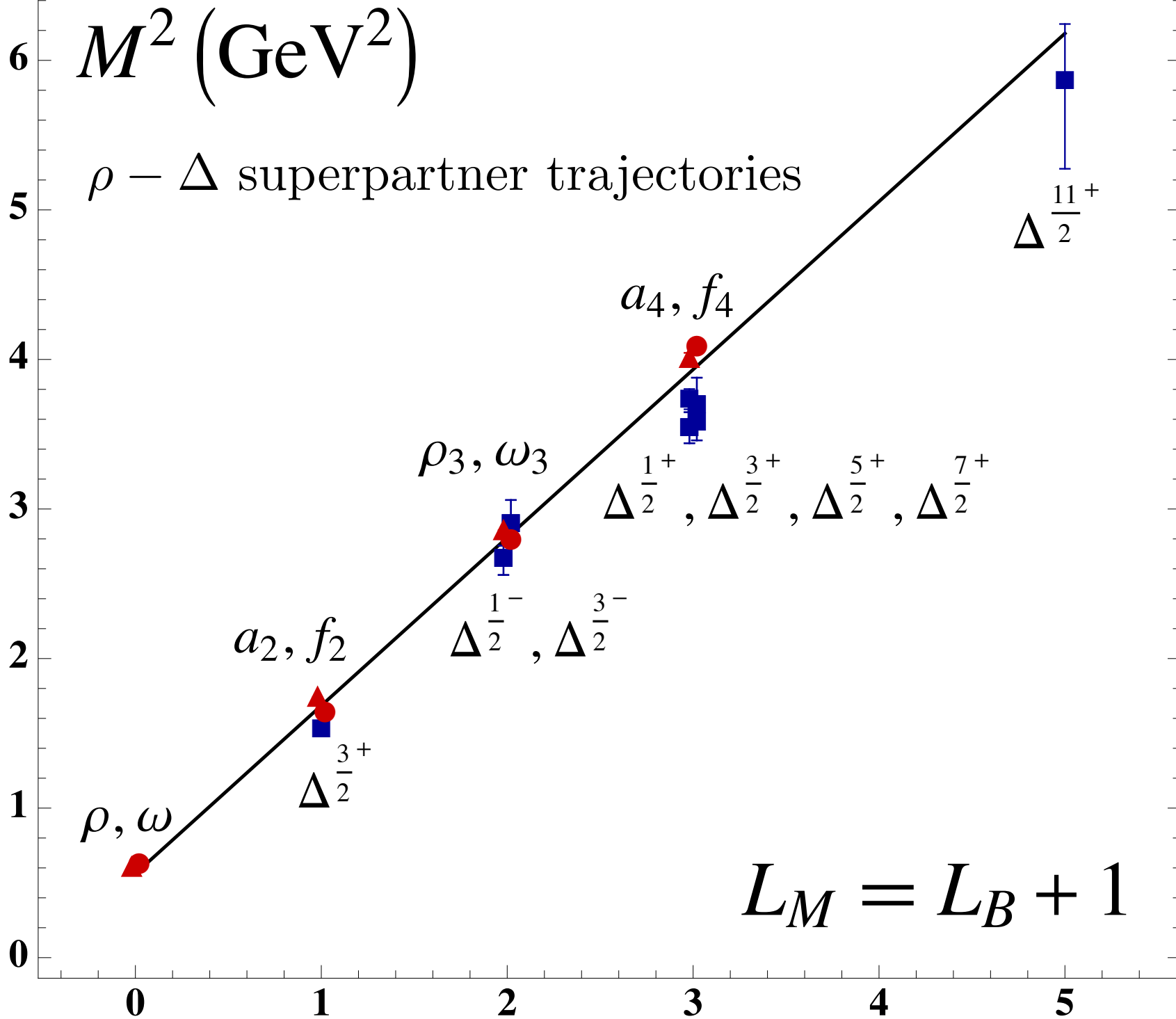
**Meson-Baryon
Mass Degeneracy
for $L_M=L_B+1$**

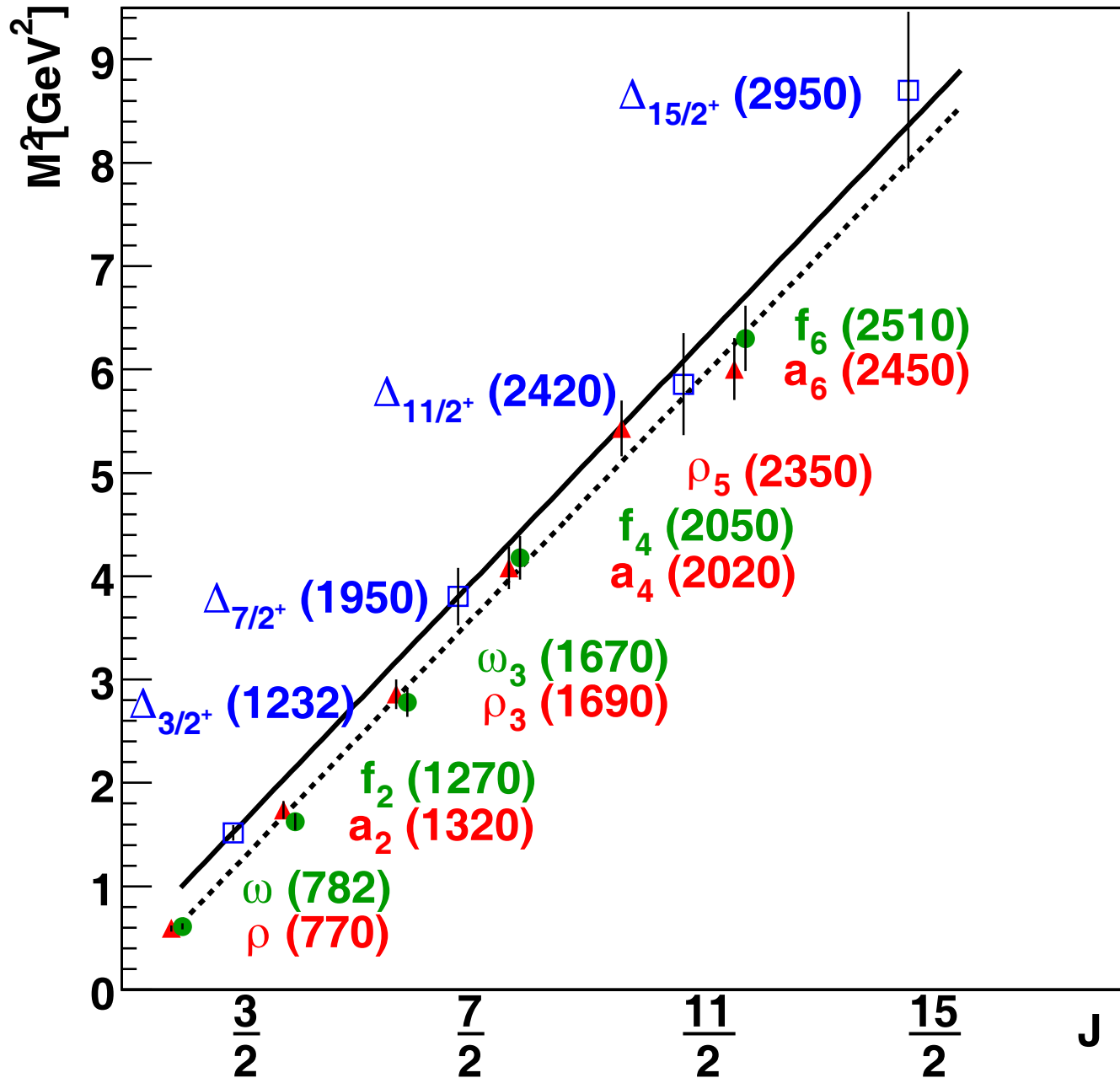
$$\frac{M_{meson}^2}{M_{nucleon}^2} = \frac{n + L_M}{n + L_B + 1}$$

$S=0, I=1$ Meson is superpartner of $S=1/2, I=1$ Baryon

M^2 (GeV²)

$\rho - \Delta$ superpartner trajectories



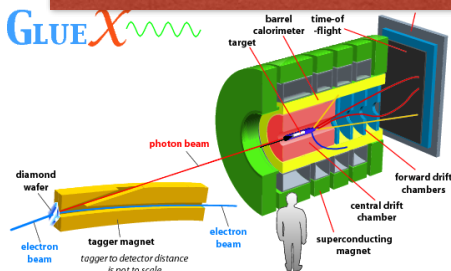


The leading Regge trajectory: Δ resonances with maximal J in a given mass range.
Also shown is the Regge trajectory for mesons with $J = L + S$.

Some Features of AdS/QCD

- **Regge spectroscopy—same slope in n, L for mesons,**
- **Chiral features for $m_q=0$: $m_\pi=0$, chiral-invariant proton**
- **Hadronic LFWFs : Single dynamical LF radial variable ξ**
- **Counting Rules**
- **Connection between hadron masses and $\Lambda_{\overline{MS}}$**

**Superconformal AdS Light-Front Holographic QCD (LFHQCD)
Meson-Baryon Mass Degeneracy for $L_M=L_B+1$**



*Novel Nuclear
Photo- and Electroproduction Physics*

Stan Brodsky

JLab, April 29, 2016

Bjorken sum rule defines effective charge

$$\alpha_{g1}(Q^2)$$

$$\int_0^1 dx [g_1^{ep}(x, Q^2) - g_1^{en}(x, Q^2)] \equiv \frac{g_a}{6} \left[1 - \frac{\alpha_{g1}(Q^2)}{\pi} \right]$$

- **Can be used as standard QCD coupling**
- **Well measured**
- **Asymptotic freedom at large Q^2**
- **Computable at large Q^2 in any pQCD scheme**
- **Universal β_0, β_1**

$$\alpha_s^{AdS}(Q)/\pi = e^{-Q^2/4\kappa^2}$$

Running Coupling from Modified AdS/QCD

Deur, de Teramond, sjb

- Consider five-dim gauge fields propagating in AdS₅ space in dilaton background $\varphi(z) = \kappa^2 z^2$

$$S = -\frac{1}{4} \int d^4x dz \sqrt{g} e^{\varphi(z)} \frac{1}{g_5^2} G^2$$

- Flow equation

$$\frac{1}{g_5^2(z)} = e^{\varphi(z)} \frac{1}{g_5^2(0)} \quad \text{or} \quad g_5^2(z) = e^{-\kappa^2 z^2} g_5^2(0)$$

where the coupling $g_5(z)$ incorporates the non-conformal dynamics of confinement

- YM coupling $\alpha_s(\zeta) = g_{YM}^2(\zeta)/4\pi$ is the five dim coupling up to a factor: $g_5(z) \rightarrow g_{YM}(\zeta)$
- Coupling measured at momentum scale Q

$$\alpha_s^{AdS}(Q) \sim \int_0^\infty \zeta d\zeta J_0(\zeta Q) \alpha_s^{AdS}(\zeta)$$

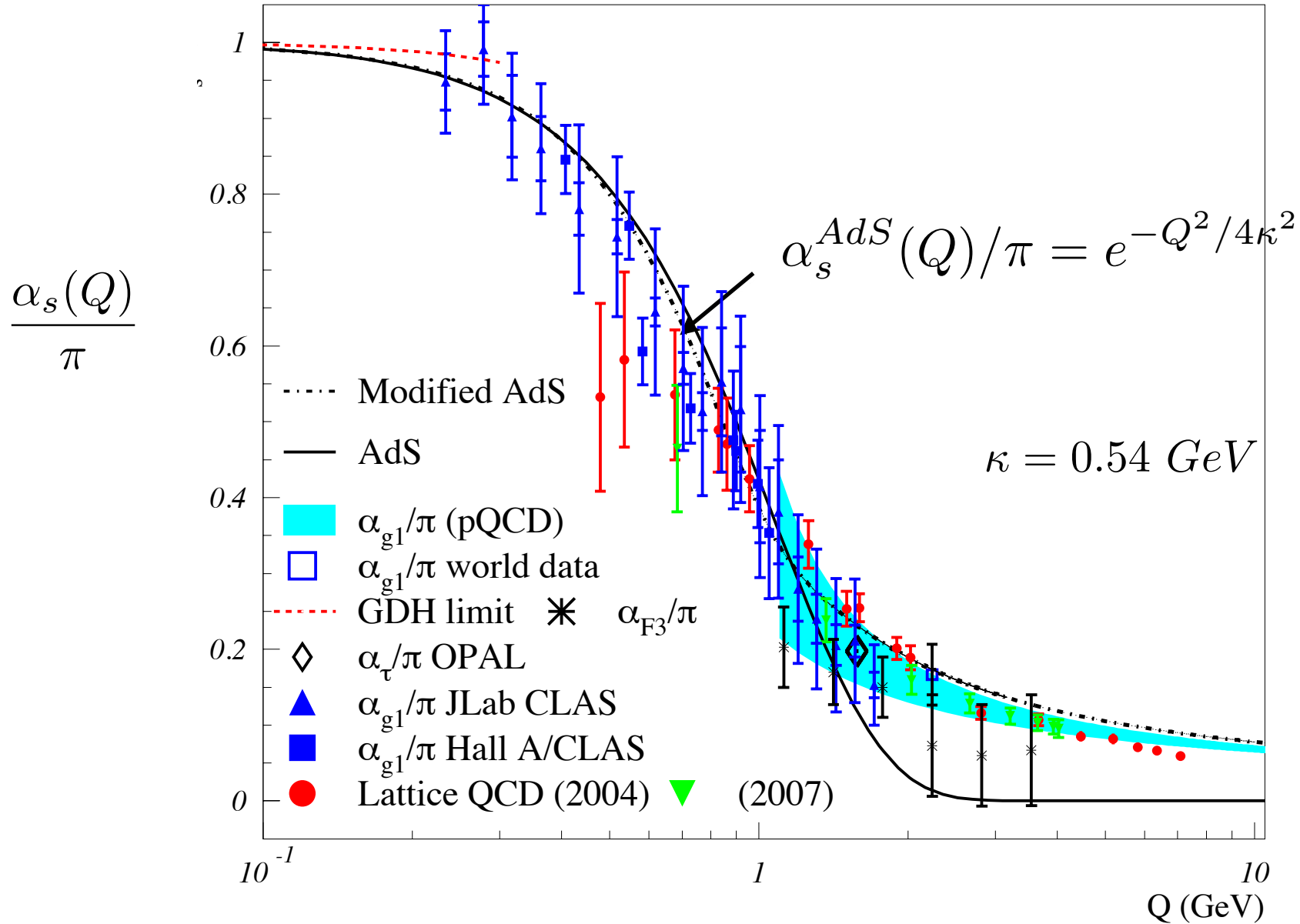
- Solution

$$\alpha_s^{AdS}(Q^2) = \alpha_s^{AdS}(0) e^{-Q^2/4\kappa^2}.$$

where the coupling α_s^{AdS} incorporates the non-conformal dynamics of confinement

Running Coupling from Light-Front Holography and AdS/QCD

Analytic, defined at all scales, IR Fixed Point



AdS/QCD dilaton captures the higher twist corrections to effective charges for $Q < 1 \text{ GeV}$

$$e^{\varphi} = e^{+\kappa^2 z^2}$$

Deur, de Teramond, sjb

$$m_\rho = \sqrt{2}\kappa$$

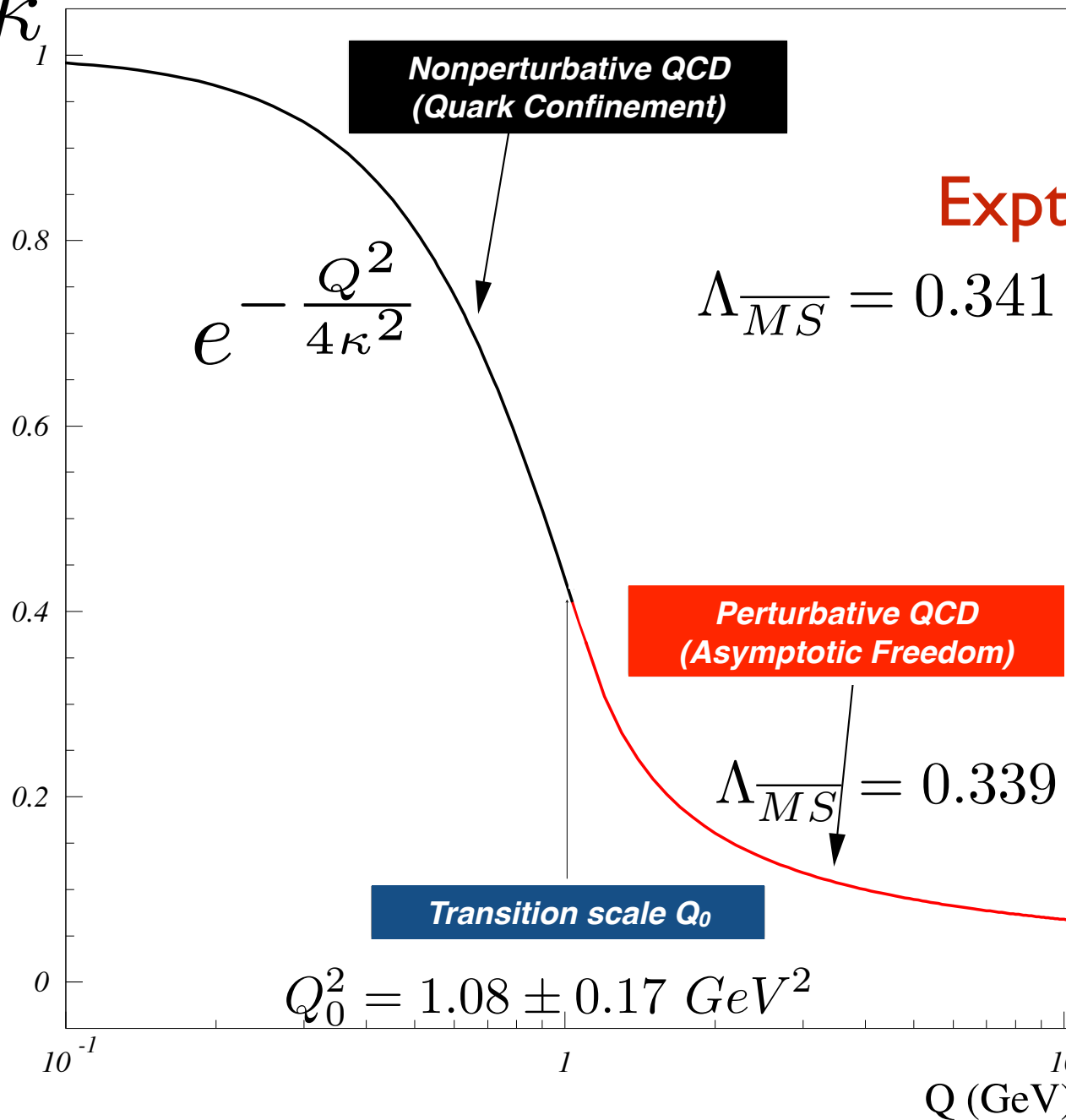
$$m_p = 2\kappa_1$$

$$\frac{\alpha_{g_1}^s(Q^2)}{\pi}$$

$$\lambda \equiv \kappa^2$$

All-Scale QCD Coupling

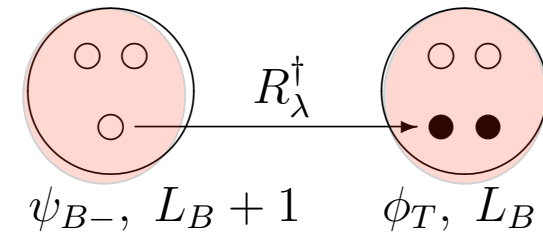
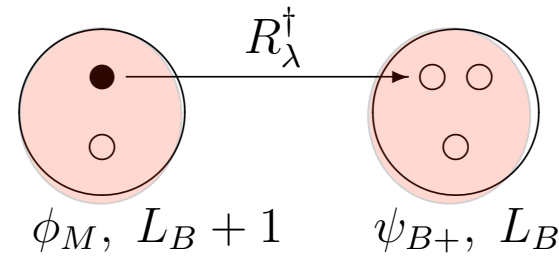
Deur, de Tèramond, sjb



Superconformal Algebra

2X2 Hadronic Multiplets $\begin{pmatrix} \phi_M(L_M = L_B + 1) & \psi_{B-}(L_B + 1) \\ \psi_{B+}(L_B) & \phi_T(L_T = L_B) \end{pmatrix}$

- quark-antiquark meson ($L_M = L_{B+I}$)
- quark-diquark baryon (L_B)
- quark-diquark baryon (L_{B+I})
- diquark-antidiquark tetraquark ($L_T = L_B$)
- Universal Regge slopes $\lambda = \kappa^2$



$$M_H^2/\lambda = \underbrace{(2n + L_H + 1)}_{\text{kinetic}} + \underbrace{(2n + L_H + 1)}_{\text{potential}} + \underbrace{2(L_H + s) + 2\chi}_{\text{contribution from AdS and superconformal algebra}} + \left\langle \sum_i \frac{m_i^2}{x_i} \right\rangle$$

$$\chi(\text{mesons}) = -1$$

$$\chi(\text{baryons, tetraquarks}) = +1$$

Universal Hadronic Decomposition

$$\frac{\mathcal{M}_H^2}{\lambda} = (1 + 2n + L) + (1 + 2n + L) + (2L + 2S + 4|B| - 2)$$

$$\lambda = \kappa^2$$

- **Universal quark light-front kinetic energy**

$$\Delta\mathcal{M}_{LFKE}^2 = \lambda(1 + 2n + L)$$

- **Universal quark light-front potential energy**

$$\Delta\mathcal{M}_{LFPE}^2 = \lambda(1 + 2n + L)$$

- **Universal Constant Contribution from AdS and Superconformal Quantum Mechanics**

$$\Delta\mathcal{M}_{spin}^2 = \lambda(2L + 2S + 4|B| - 2)$$

hyperfine spin-spin

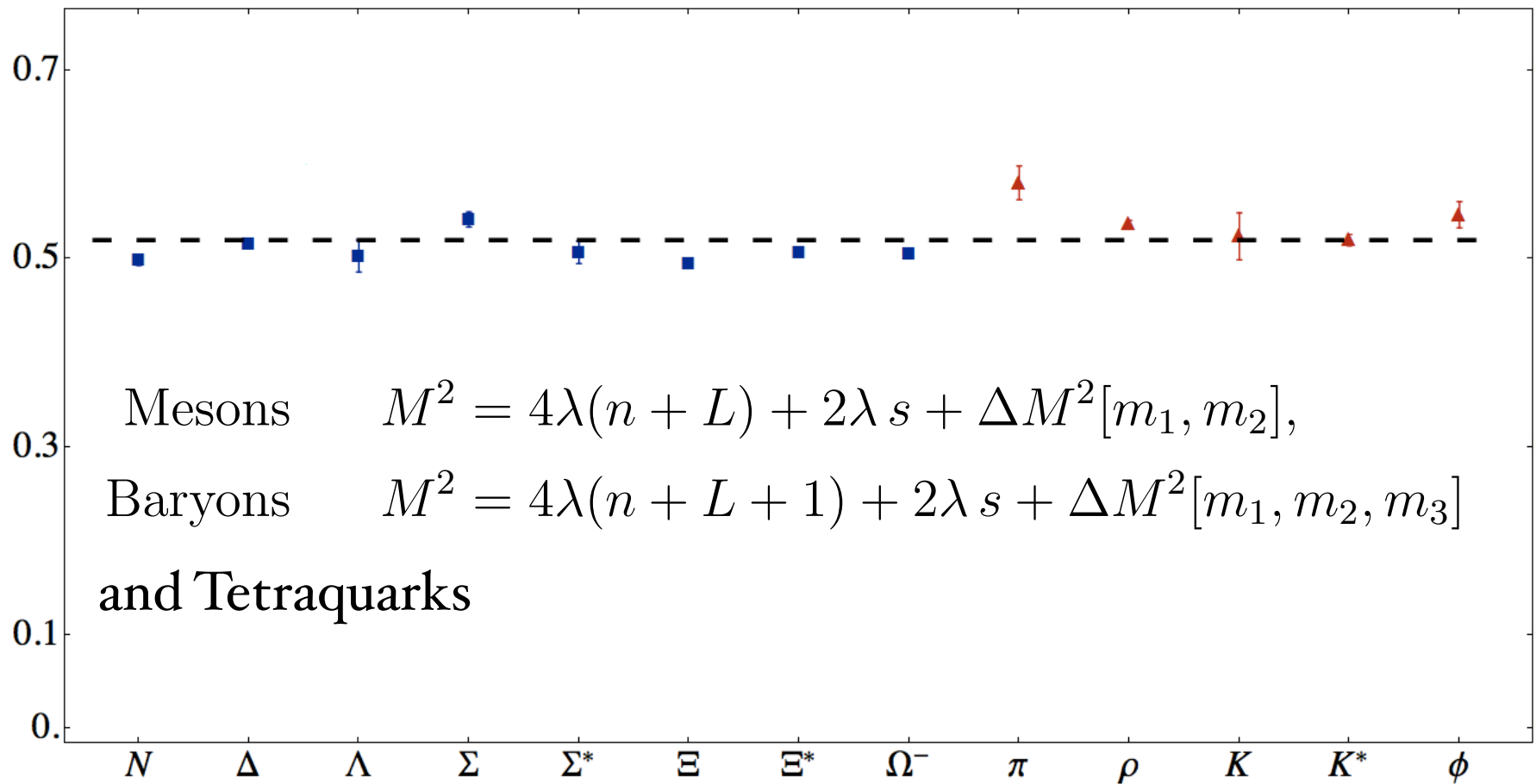
- plus $\Delta\mathcal{M}_{quark\ mass}^2 = \sum_q \frac{m_q^2}{x_q}$

Equal:
Virial
Theorem

$$\kappa = \sqrt{\lambda}$$

- Universal Regge slopes

$$M_H^2 = 4\lambda(n + L) + \dots$$



Interpretation of Mass Scale κ

- Does not affect conformal symmetry of QCD action
- Self-consistent regularization of IR divergences
- Determines all mass and length scales for zero quark mass
- Compute scheme-dependent $\Lambda_{\overline{MS}}$ determined in terms of κ
- Value of κ itself not determined -- place holder
- Need external constraint such as f_π

$$\kappa = \sqrt{\lambda}$$

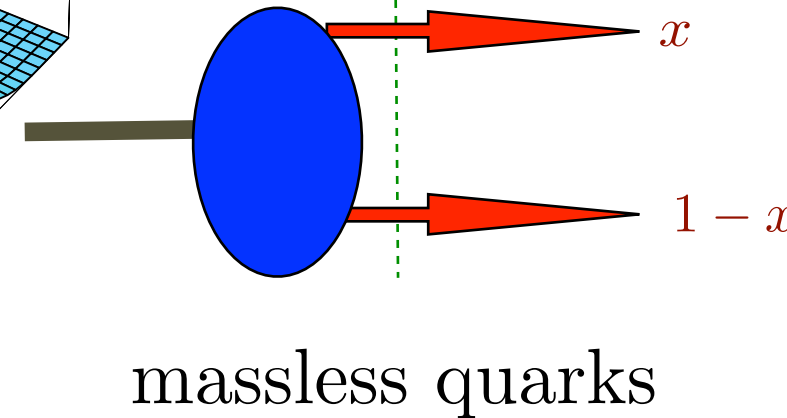
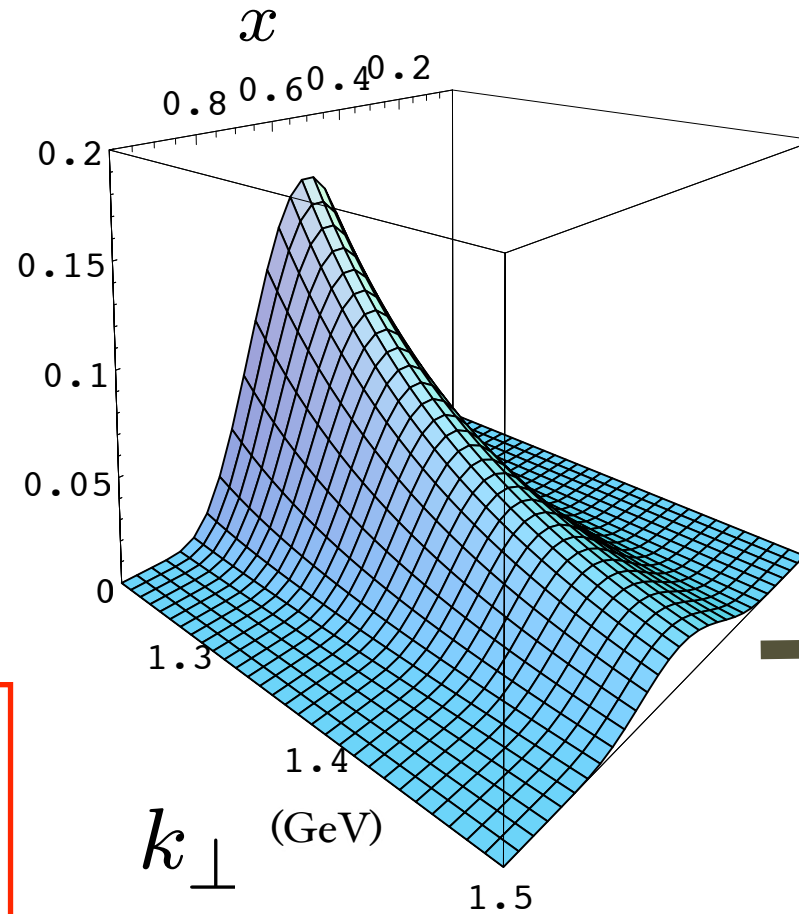
Prediction from AdS/QCD: Meson LFWF

$$e^{\varphi(z)} = e^{+\kappa^2 z}$$

de Teramond,
Cao, sjb

“Soft Wall”
model

$$\psi_M(x, k_{\perp}^2)$$



Note coupling

$$k_{\perp}^2, x$$

$$\psi_M(x, k_{\perp}) = \frac{4\pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k_{\perp}^2}{2\kappa^2 x(1-x)}}$$

$$\phi_{\pi}(x) = \frac{4}{\sqrt{3}\pi} f_{\pi} \sqrt{x(1-x)}$$

$$f_{\pi} = \sqrt{P_{q\bar{q}}} \frac{\sqrt{3}}{8} \kappa = 92.4 \text{ MeV}$$

Same as DSE!

Provides Connection of Confinement to Hadron Structure

AdS/QCD Holographic Wave Function for the ρ Meson and Diffractive ρ Meson Electroproduction

J. R. Forshaw*

*Consortium for Fundamental Physics, School of Physics and Astronomy, University of Manchester,
Oxford Road, Manchester M13 9PL, United Kingdom*

R. Sandapen†

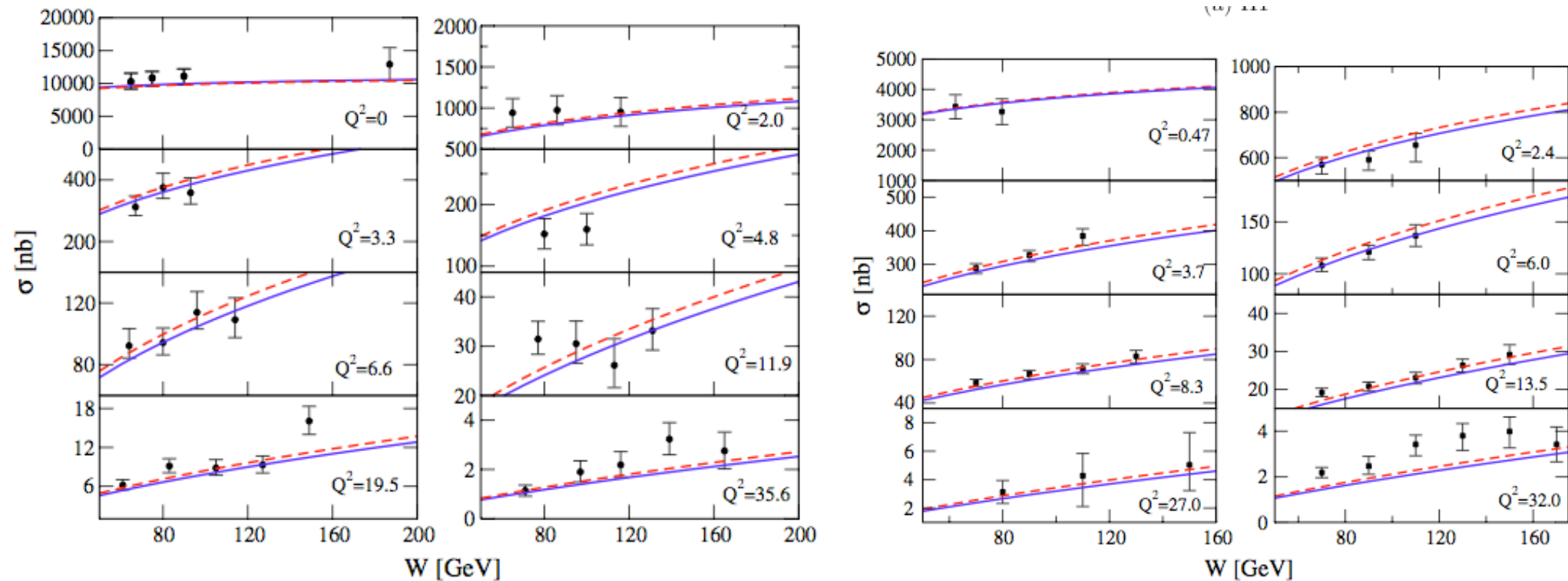
Département de Physique et d'Astronomie, Université de Moncton, Moncton, New Brunswick E1A3E9, Canada

(Received 5 April 2012; published 20 August 2012)

We show that anti-de Sitter/quantum chromodynamics generates predictions for the rate of diffractive ρ -meson electroproduction that are in agreement with data collected at the Hadron Electron Ring Accelerator electron-proton collider.

$$\psi_M(x, k_{\perp}) = \frac{4\pi}{\kappa \sqrt{x(1-x)}} e^{-\frac{k_{\perp}^2}{2\kappa^2 x(1-x)}}$$

AdS/QCD Holographic Wave Function for the ρ Meson and Diffractive ρ Meson Electroproduction

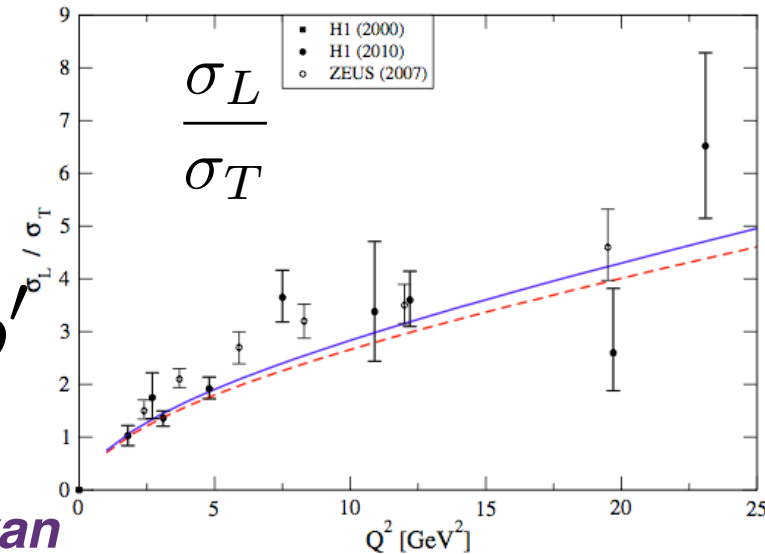


(b) ZEUS

**J. R. Forshaw,
R. Sandapen**

$$\gamma^* p \rightarrow \rho^0 p'$$

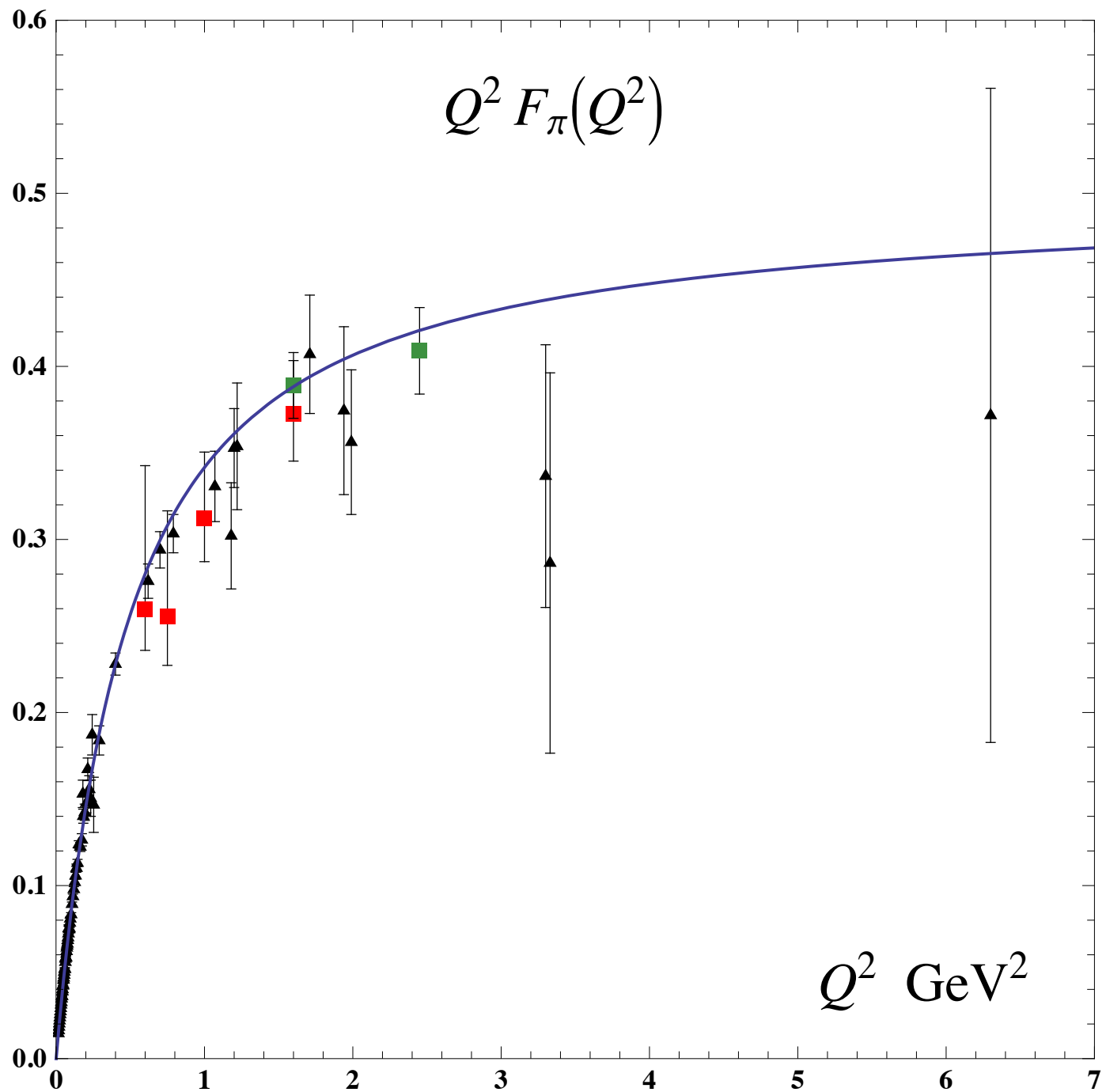
**Nuclear effects:
Sergey Gevorkyan**



*Prediction from
Light-Front Holography*

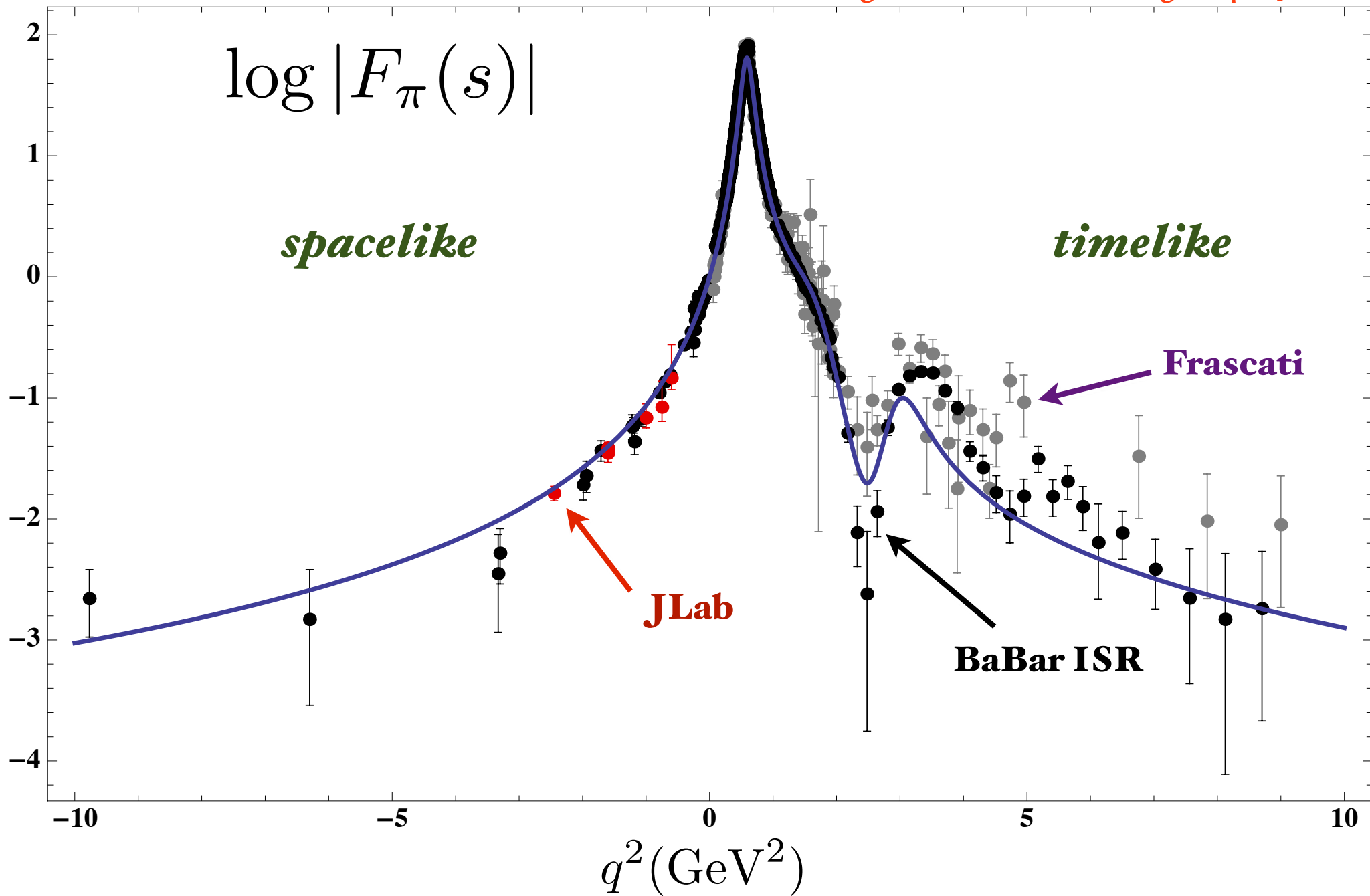
$$\psi_M(x, k_\perp) = \frac{4\pi}{\kappa\sqrt{x(1-x)}} e^{-\frac{k_\perp^2}{2\kappa^2 x(1-x)}}$$

Pion Form Factor predicted from AdS/QCD and Light-Front Holography

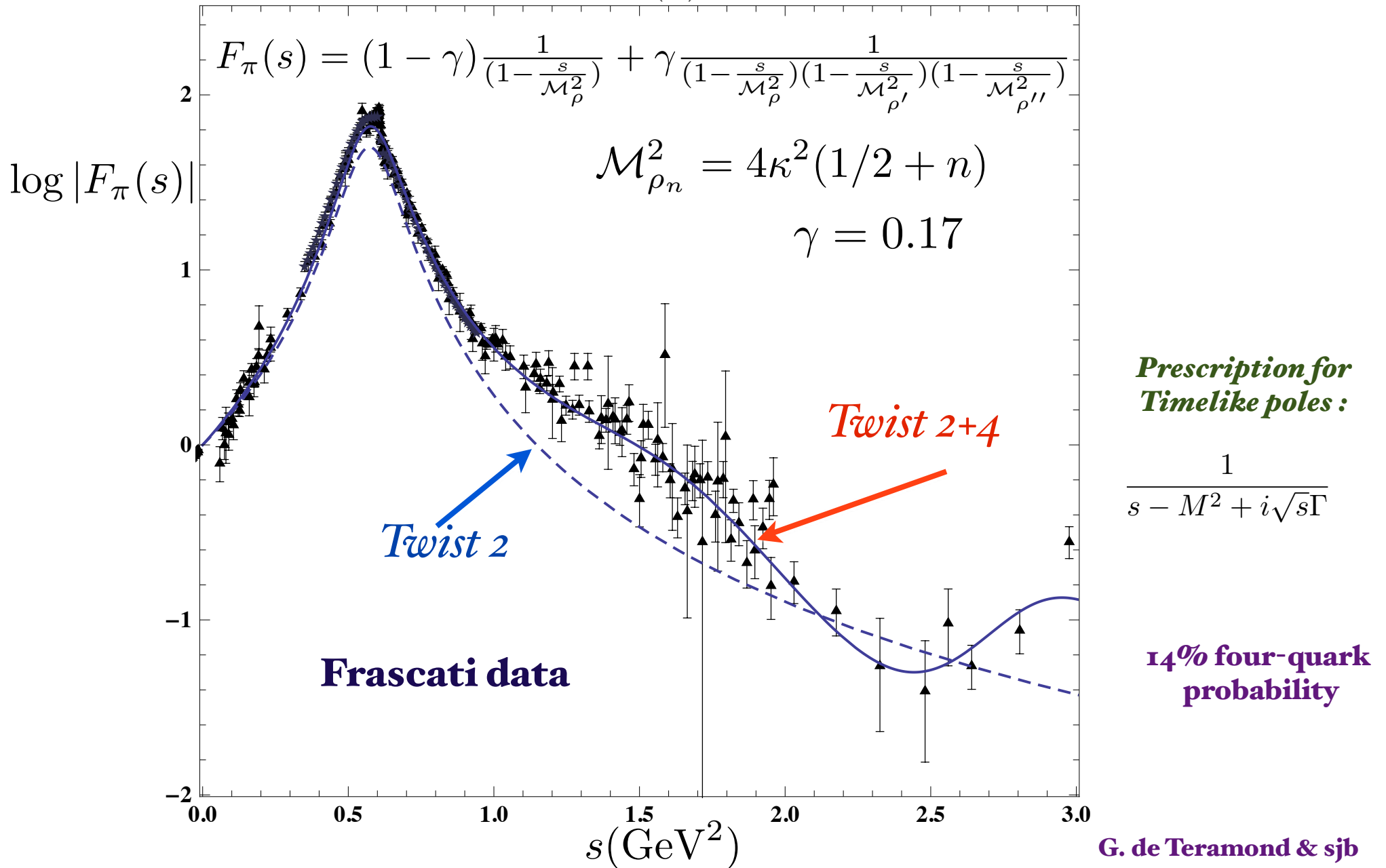


Counting Rules from Leading Twist Obeyed

Pion Form Factor from AdS/QCD and Light-Front Holography



Timelike Pion Form Factor from AdS/QCD and Light-Front Holography



- Compute Dirac proton form factor using SU(6) flavor symmetry

$$F_1^p(Q^2) = R^4 \int \frac{dz}{z^4} V(Q, z) \Psi_+^2(z)$$

- Nucleon AdS wave function

$$\Psi_+(z) = \frac{\kappa^{2+L}}{R^2} \sqrt{\frac{2n!}{(n+L)!}} z^{7/2+L} L_n^{L+1}(\kappa^2 z^2) e^{-\kappa^2 z^2/2}$$

- Normalization ($F_1^p(0) = 1$, $V(Q=0, z) = 1$)

$$R^4 \int \frac{dz}{z^4} \Psi_+^2(z) = 1$$

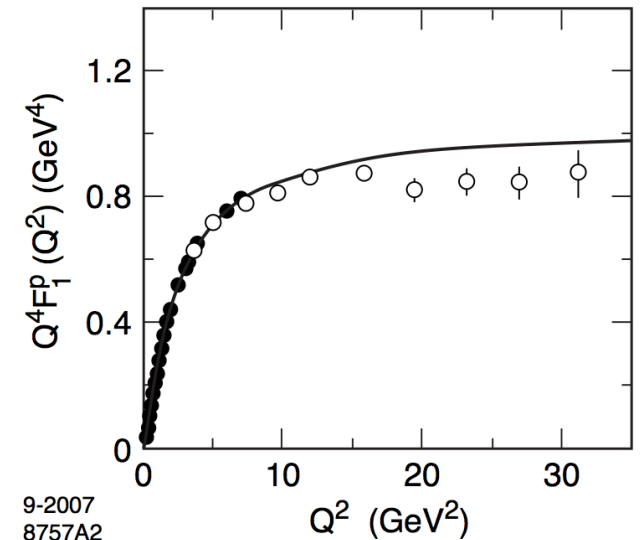
- Bulk-to-boundary propagator [Grigoryan and Radyushkin (2007)]

$$V(Q, z) = \kappa^2 z^2 \int_0^1 \frac{dx}{(1-x)^2} x^{\frac{Q^2}{4\kappa^2}} e^{-\kappa^2 z^2 x/(1-x)}$$

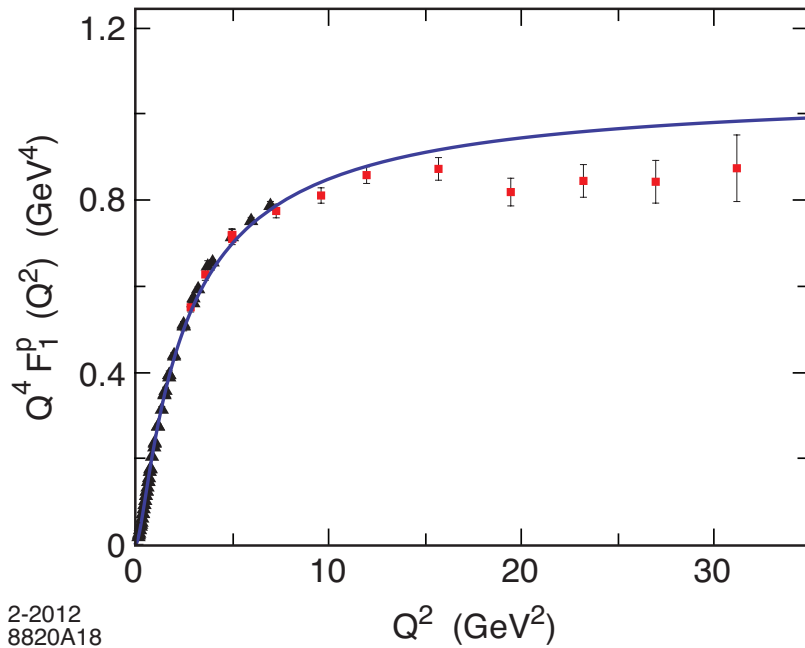
- Find

$$F_1^p(Q^2) = \frac{1}{\left(1 + \frac{Q^2}{\mathcal{M}_\rho^2}\right) \left(1 + \frac{Q^2}{\mathcal{M}_{\rho'}^2}\right)}$$

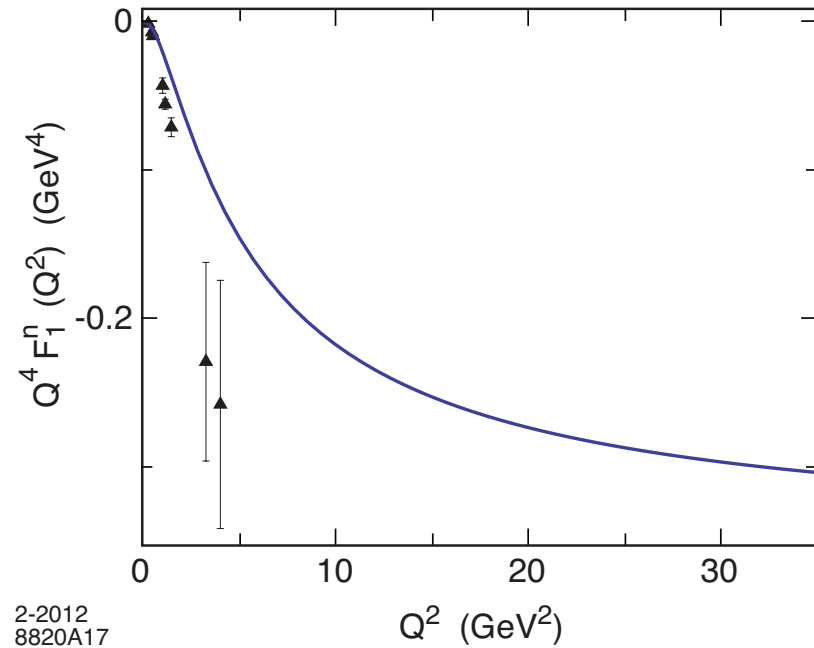
with $\mathcal{M}_{\rho n}^2 \rightarrow 4\kappa^2(n + 1/2)$



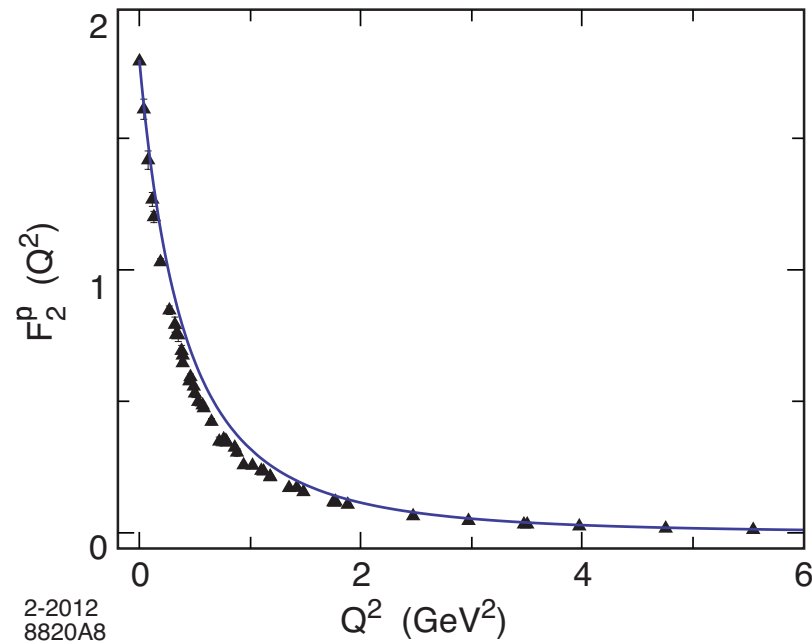
Using $SU(6)$ flavor symmetry and normalization to static quantities



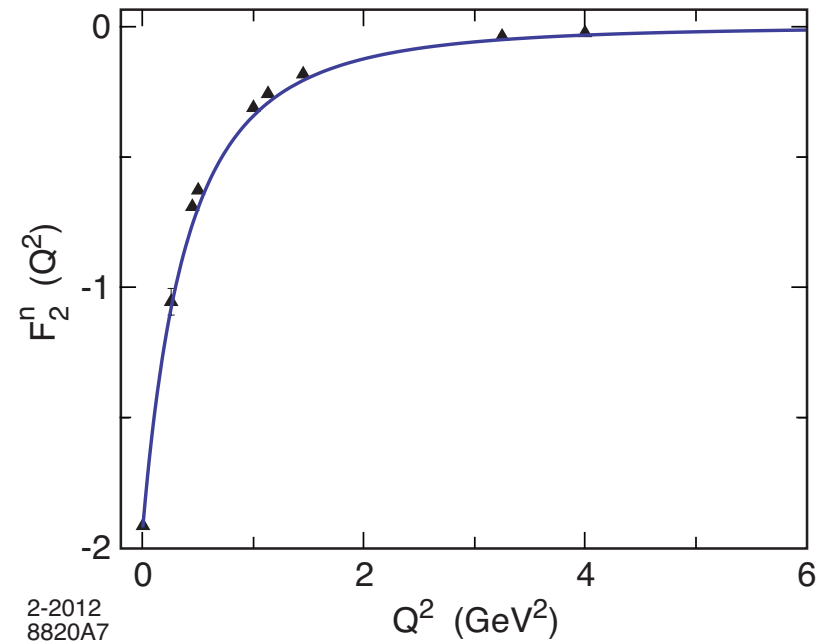
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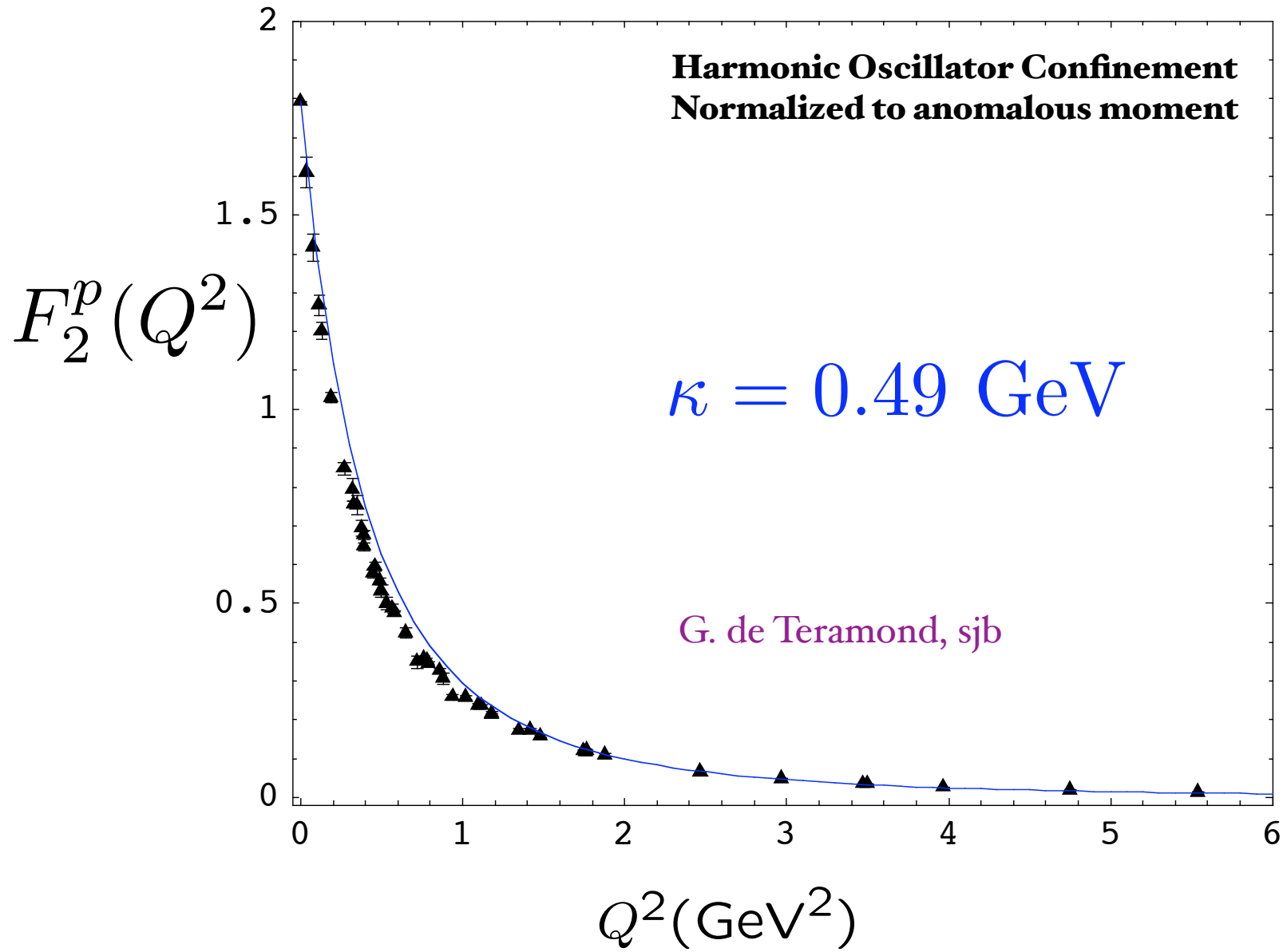
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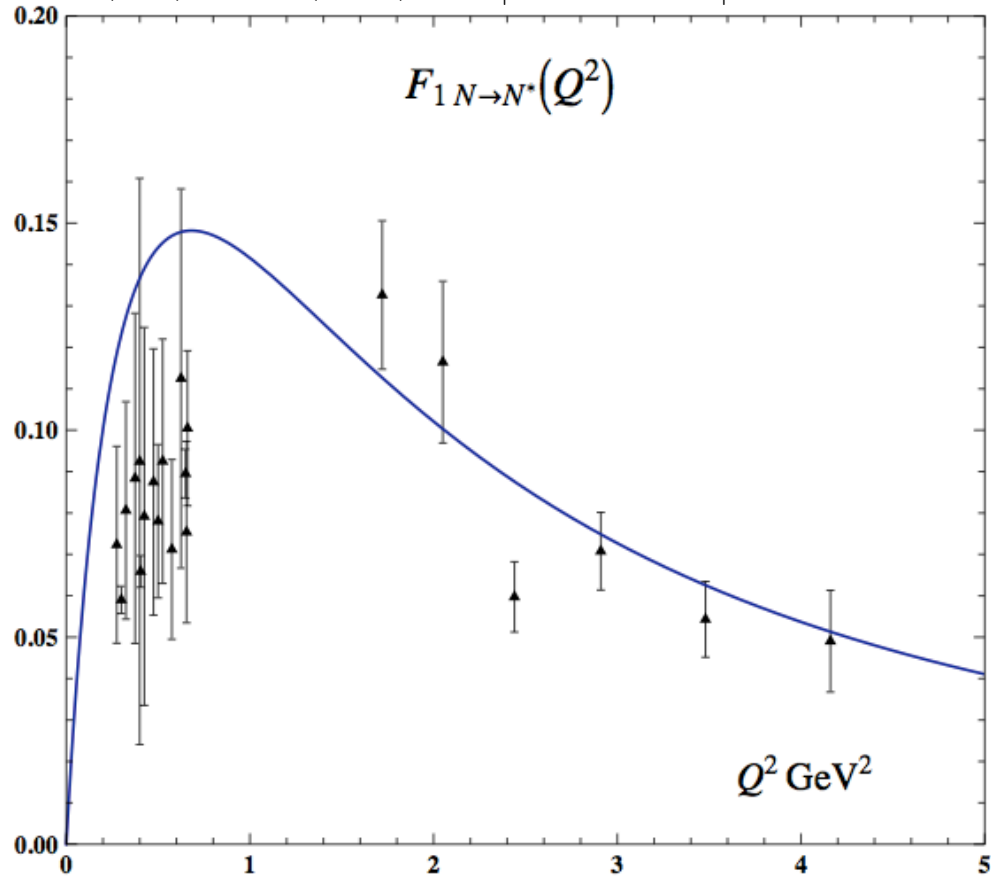
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Spacelike Pauli Form Factor

From overlap of $L = 1$ and $L = 0$ LFWFs



$N(940) \rightarrow N^*(1440): \Psi_+^{n=0,L=0} \rightarrow \Psi_+^{n=1,L=0}$



Data from I. Aznauryan, *et al.* CLAS (2009)

$$F_{1N \rightarrow N^*}^p(Q^2) = \frac{2\sqrt{2}}{3} \frac{\frac{Q^2}{M_P^2}}{\left(1 + \frac{Q^2}{\mathcal{M}_\rho^2}\right) \left(1 + \frac{Q^2}{\mathcal{M}_{\rho'}^2}\right) \left(1 + \frac{Q^2}{\mathcal{M}_{\rho''}^2}\right)}$$

with $\mathcal{M}_{\rho_n}^2 \rightarrow 4\kappa^2(n + 1/2)$

Predictions from AdS Holographic QCD

Dosch, Deur, de Teramond,
sjb

- Zero-Mass pion for zero quark mass

$$M_{\pi}^2(n, L) = 4\kappa^2(n + L)$$

- Regge Spectroscopy

- Same slope in n, L

- LFWFs, Distribution Amplitudes

$$\phi_{\pi}(x) \propto f_{\pi} \sqrt{x(1-x)}$$

- Form Factors, Structure Functions, GPDs

- Non-perturbative running coupling

$$\alpha_s(Q^2) \propto e^{-\frac{Q^2}{4\kappa^2}}$$

- Meson-Baryon Supersymmetry for $L_M = L_{B+1}$

$$\lambda = \kappa^2$$

Interpretation of Mass Scale \mathcal{K}

- Does not affect conformal symmetry of QCD action
- Self-consistent regularization of IR divergences
- Determines all mass and length scales for zero quark mass
- Compute scheme-dependent $\Lambda_{\overline{MS}}$ determined in terms of \mathcal{K}
- Value of \mathcal{K} itself not determined -- place holder
- Need external constraint such as f_π

Tests of AdS/QCD and LF Holography

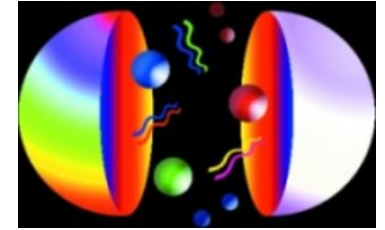
JLab 12 GeV

- Spacelike-Transition Form Factors $F_{\pi \rightarrow b_1}(Q^2)$ $F_{p \rightarrow N^*}(Q^2)$
- Supersymmetric QCD Relations: Spectra, Dynamics
- Baryons: q + diquark $[q]_{3C} [qq]_{\bar{3}C}$
- Pentaquarks: diquark-antidiquark $[qq]_{\bar{3}C} [\bar{q}\bar{q}]_{3C}$

Fermionic Modes and Baryon Spectrum

[Hard wall model: GdT and S. J. Brodsky, PRL **94**, 201601 (2005)]

[Soft wall model: GdT and S. J. Brodsky, (2005), arXiv:1001.5193]



From Nick Evans

- Nucleon LF modes

$$\psi_+(\zeta)_{n,L} = \kappa^{2+L} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{3/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^{L+1}(\kappa^2 \zeta^2)$$

$$\psi_-(\zeta)_{n,L} = \kappa^{3+L} \frac{1}{\sqrt{n+L+2}} \sqrt{\frac{2n!}{(n+L)!}} \zeta^{5/2+L} e^{-\kappa^2 \zeta^2 / 2} L_n^{L+2}(\kappa^2 \zeta^2)$$

- Normalization

$$\int d\zeta \psi_+^2(\zeta) = \int d\zeta \psi_-^2(\zeta) = 1$$

*Chiral Symmetry
of Eigenstate!*

- Eigenvalues

$$\mathcal{M}_{n,L,S=1/2}^2 = 4\kappa^2 (n+L+1)$$

- “Chiral partners”

$$\frac{\mathcal{M}_{N(1535)}}{\mathcal{M}_{N(940)}} = \sqrt{2}$$

Features of Supersymmetric Equations

- $J = L + S$ baryon simultaneously satisfies both equations of G with L , $L+1$ for same mass eigenvalue
 - $J^z = L^z + 1/2 = (L^z + 1) - 1/2$ $S^z = \pm 1/2$
 - Baryon spin carried by quark orbital angular momentum: $\langle J^z \rangle = L^z + 1/2$
 - Mass-degenerate meson “superpartner” with $L_M = L_B + 1$. *“Shifted meson-baryon Duality”*
- Meson and baryon have same κ !

Counting Rules Obeyed

AdS/QCD and Light-Front Holography

$$\mathcal{M}_{n,J,L}^2 = 4\kappa^2 \left(n + \frac{J+L}{2} \right)$$

- **Zero mass pion for $m_q=0$ ($n=J=L=0$)**
- **Regge trajectories: equal slope in n and L**
- **Form Factors at high Q^2 : Dimensional counting**
 $[Q^2]^{n-1} F(Q^2) \rightarrow \text{const}$
- **Space-like and Time-like Meson and Baryon Form Factors**
- **Running Coupling for NPQCD** $\alpha_s(Q^2) \propto e^{-\frac{Q^2}{4\kappa^2}}$
- **Meson Distribution Amplitude** $\phi_\pi(x) \propto f_\pi \sqrt{x(1-x)}$

Features of AdS/QCD

de Tèramond, Dosch, Deur, sjb

- **Color confining potential $\kappa^4 \zeta^2$ and universal mass scale from dilaton**

$$e^{\phi(z)} = e^{\kappa^2 z^2} \quad \alpha_s(Q^2) \propto \exp -Q^2/4\kappa^2$$

- **Dimensional transmutation** $\Lambda_{\overline{MS}} \leftrightarrow \kappa \leftrightarrow m_H$

- **Chiral Action remains conformally invariant despite mass scale** *DAFF*

- **Light-Front Holography: Duality of AdS and independent LF QCD** **frame-**

- **Reproduces observed Regge spectroscopy — slope in n, L, and J for mesons and baryons** **same**

- **Massless pion for massless quark**

- **Supersymmetric meson-baryon dynamics and spectroscopy:**

$$\mathbf{L}_M = \mathbf{L}_B + \mathbf{I}$$

*Superconformal Quantum
Mechanics*

Fubini and Rabinovici

Tests of AdS/QCD and LF Holography at JLab 12 GeV

- **Compare Spacelike-Transition Form Factors, Counting Rules**

$$F_{\pi \rightarrow b_1}(Q^2) \quad \text{vs.} \quad F_{p \rightarrow N^*}(Q^2)$$

- **Supersymmetric QCD Relations: Spectra, Dynamics**

- **Baryons: q + diquark:** $[q]_{3C} [qq]_{\bar{3}C}$

- **Tetraquarks: diquark-antidiquark?:** $[qq]_{\bar{3}C} [\bar{q}\bar{q}]_{3C}$

contribution from 2-dim

light-front harmonic oscillator

contribution from AdS and

superconformal algebra

$$M_H^2/\lambda = \underbrace{(2n + L_H + 1)}_{\text{kinetic}} + \underbrace{(2n + L_H + 1)}_{\text{potential}} + \underbrace{2(L_H + s) + 2\chi}_{\text{superconformal algebra}}$$

Tony Zee

"Quantum Field Theory in a Nutshell"

Dreams of Exact Solvability

“In other words, if you manage to calculate m_P it better come out proportional to Λ_{QCD} since Λ_{QCD} is the only quantity with dimension of mass around.

Light-Front Holography:

Similarly for m_ρ .

$$m_p \simeq 3.21 \Lambda_{\overline{MS}}$$

$$m_\rho \simeq 2.2 \Lambda_{\overline{MS}}$$

Put in precise terms, if you publish a paper with a formula giving m_ρ/m_P in terms of pure numbers such as 2 and π , the field theory community will hail you as a conquering hero who has solved QCD exactly.”

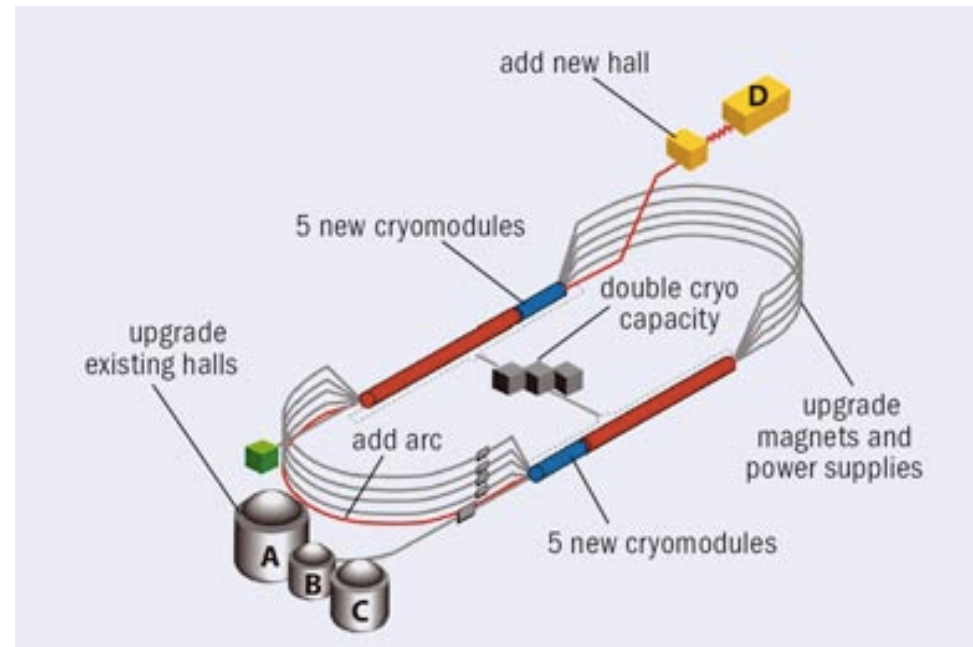
$$(m_q = 0)$$

$$m_\pi = 0$$

$$\frac{m_\rho}{m_P} = \frac{1}{\sqrt{2}}$$

$$\frac{\Lambda_{\overline{MS}}}{m_\rho} = 0.455 \pm 0.031$$

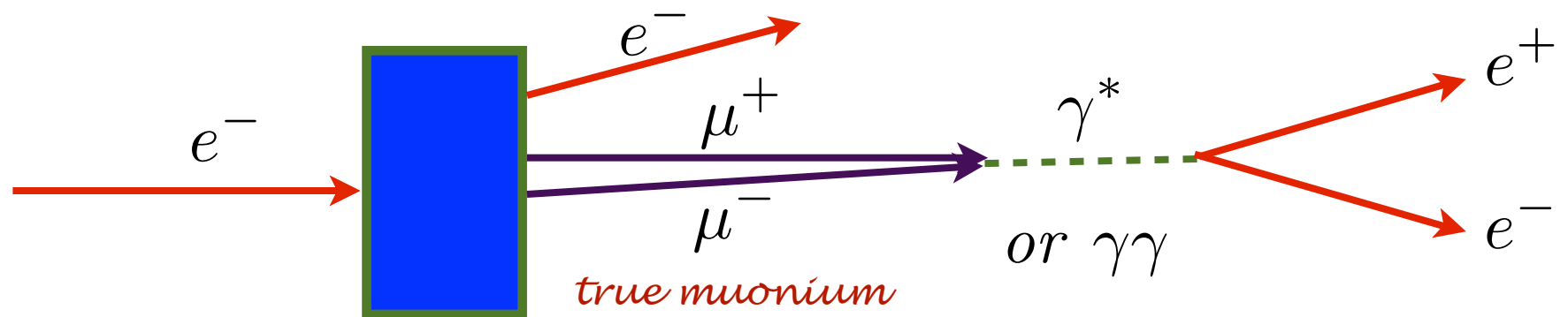
- *Test Meson-Baryon Supersymmetry*
- *Intrinsic Heavy Quarks*
- *Charm at Threshold*
- *Novel Heavy-Quark Resonances at Threshold*
- *Tetraquarks and Nuclear-Bound Quarkonium*
- *Exclusive and Inclusive Sivers Effect.*
- *Breakdown of pQCD Leading-Twist Factorization*
- *Non-Universal antishadowing*
- *Color Transparency*
- *Hidden Color*
- *$J=0$ Fixed Pole in DVCS*
- *Diffraction DIS*



QED:
Measure Lamb Shift of
“True Muonium” $[\mu^+ \mu^-]$

● Production of True Muonium $[\mu^+\mu^-]$

$$eZ \rightarrow eZ[\mu^+\mu^-]_nS \quad q_{min} \simeq \frac{M_{\mu^+\mu^-}^2}{\nu} \sim 10 \text{ MeV}$$



- Produces all Rydberg Levels
- Analytic connection to continuum production -- enhanced by SSS at threshold
- Gap extends in cm multiplied by Lorentz boost
- Excite/De-excite levels with external fields, lasers

Production of True Muonium $[\mu^+\mu^-]$

PRL 102, 213401 (2009)

PHYSICAL REVIEW LETTERS

week ending
29 MAY 2009

Production of the Smallest QED Atom: True Muonium ($\mu^+\mu^-$)

Stanley J. Brodsky*

SLAC National Accelerator Laboratory, Stanford University, Stanford, California 94309, USA

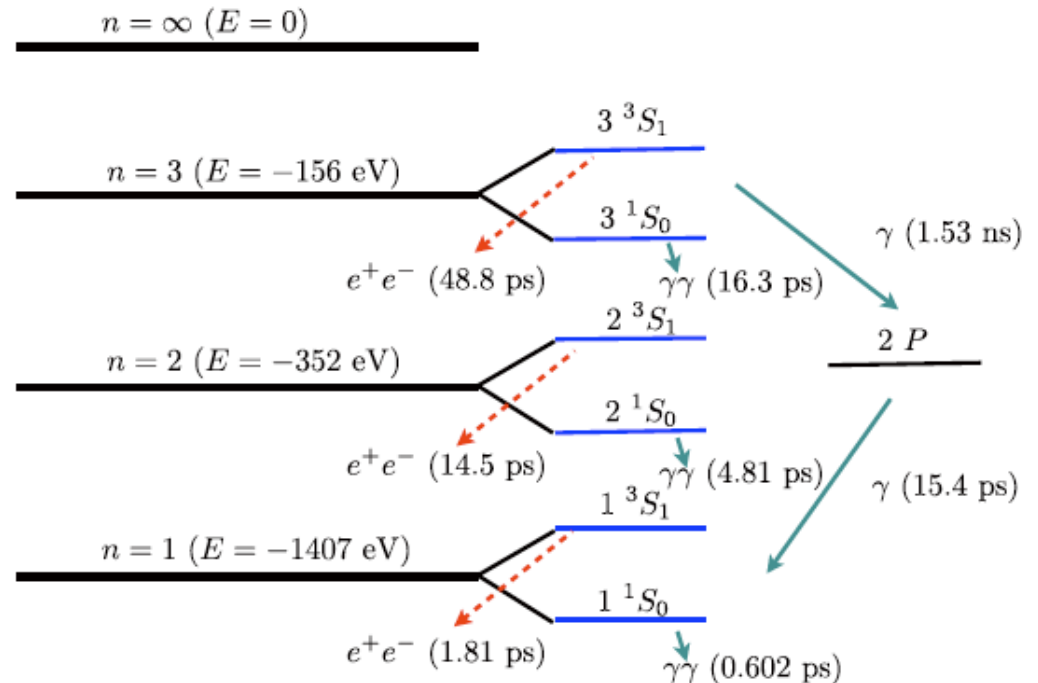
Richard F. Lebed†

Department of Physics, Arizona State University, Tempe, Arizona 85287-1504, USA

(Received 22 April 2009; published 26 May 2009)

Rydberg Levels and Decays

$$\begin{aligned} \tau(n^3S_1 \rightarrow e^+e^-) &= \frac{6\hbar n^3}{\alpha^5 mc^2}, & \tau(n^1S_0 \rightarrow \gamma\gamma) &= \frac{2\hbar n^3}{\alpha^5 mc^2}, \\ \tau(2P \rightarrow 1S) &= \left(\frac{3}{2}\right)^8 \frac{2\hbar}{\alpha^5 mc^2}, & \tau(3S \rightarrow 2P) &= \left(\frac{5}{2}\right)^9 \frac{4\hbar}{3\alpha^5 mc^2}, \\ \frac{\tau(n^3S_1 \rightarrow e^+e^-)}{\tau(n^1S_0 \rightarrow \gamma\gamma)} &= 3, & \frac{\tau(2P \rightarrow 1S)}{\tau(n^1S_0 \rightarrow \gamma\gamma)} &= \left(\frac{3}{2}\right)^8 \frac{1}{n^3} = \frac{25.6}{n^3}, \\ \frac{\tau(3S \rightarrow 2P)}{\tau(2P \rightarrow 1S)} &= \left(\frac{5}{3}\right)^9 = 99.2. \end{aligned}$$



Production of bound triplet $\mu^+\mu^-$ system in collisions of electrons with atoms.

[N. Arteaga-Romero](#), [C. Carimalo](#), ([Paris U., VI-VII](#)) , [V.G. Serbo](#), ([Paris U., VI-VII](#) & [Novosibirsk State U.](#)) . Jan 2000. 10pp.

Published in **Phys.Rev. A62:032501, 2000.**

e-Print: [hep-ph/0001278](#)

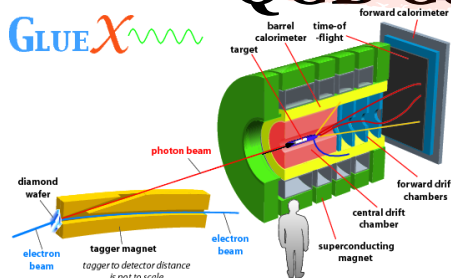
Light-Front vacuum can simulate empty universe

Shrock, Tandy, Roberts, sjb

- **Independent of observer frame**
- **Causal**
- **Lowest invariant mass state $M=0$.**
- **Trivial up to $k^+=0$ zero modes-- already normal-ordering**
- **Higgs theory consistent with trivial LF vacuum (Srivastava, sjb)**
- **QCD and AdS/QCD: “In-hadron” condensates (Maris, Tandy Roberts) -- GMOR satisfied.**
- **QED vacuum; no loops**
- **Zero cosmological constant from QED, QCD, EW**

QCD Myths

- **Anti-Shadowing is Universal**
- **ISI and FSI are higher twist effects and universal**
- **High transverse momentum hadrons arise only from jet fragmentation -- baryon anomaly!**
- **Heavy quarks only from gluon splitting**
- **Renormalization scale cannot be fixed**
- **QCD condensates are vacuum effects**
- **QCD gives 10^{42} to the cosmological constant**
- **QCD Confinement and Mass Scale from $\Lambda_{\overline{MS}}$**



*Novel Nuclear
Photo- and Electroproduction Physics*

JLab, April 29, 2016

Stan Brodsky

Hot Topics in QCD

- *Intrinsic Heavy Quarks*
- *Breakdown of pQCD Leading-Twist Factorization*
- *Top/anti-Top asymmetry*
- *Non-universal antishadowing*
- *Demise of QCD Vacuum Condensates*
- *Elimination of the QCD Renormalization Scale Ambiguity*
- *AdS/QCD and Light-Front Holography*

*Crucial to Understand QCD to High Precision to
Illuminate New Physics*

Set multiple renormalization scales -- Lensing, DGLAP, ERBL Evolution ...

Choose renormalization scheme; e.g. $\alpha_s^R(\mu_R^{\text{init}})$

Choose μ_R^{init} ; arbitrary initial renormalization scale

Identify $\{\beta_i^R\}$ – terms using n_f – terms
through the PMC – BLM correspondence principle

Shift scale of α_s to μ_R^{PMC} to eliminate $\{\beta_i^R\}$ – terms

Conformal Series

Result is independent of μ_R^{init} and scheme at fixed order

Principle of Maximum Conformality

PMC/BLM

No renormalization scale ambiguity!

*Result is independent of
Renormalization scheme
and initial scale!*

QED Scale Setting at $N_C=0$

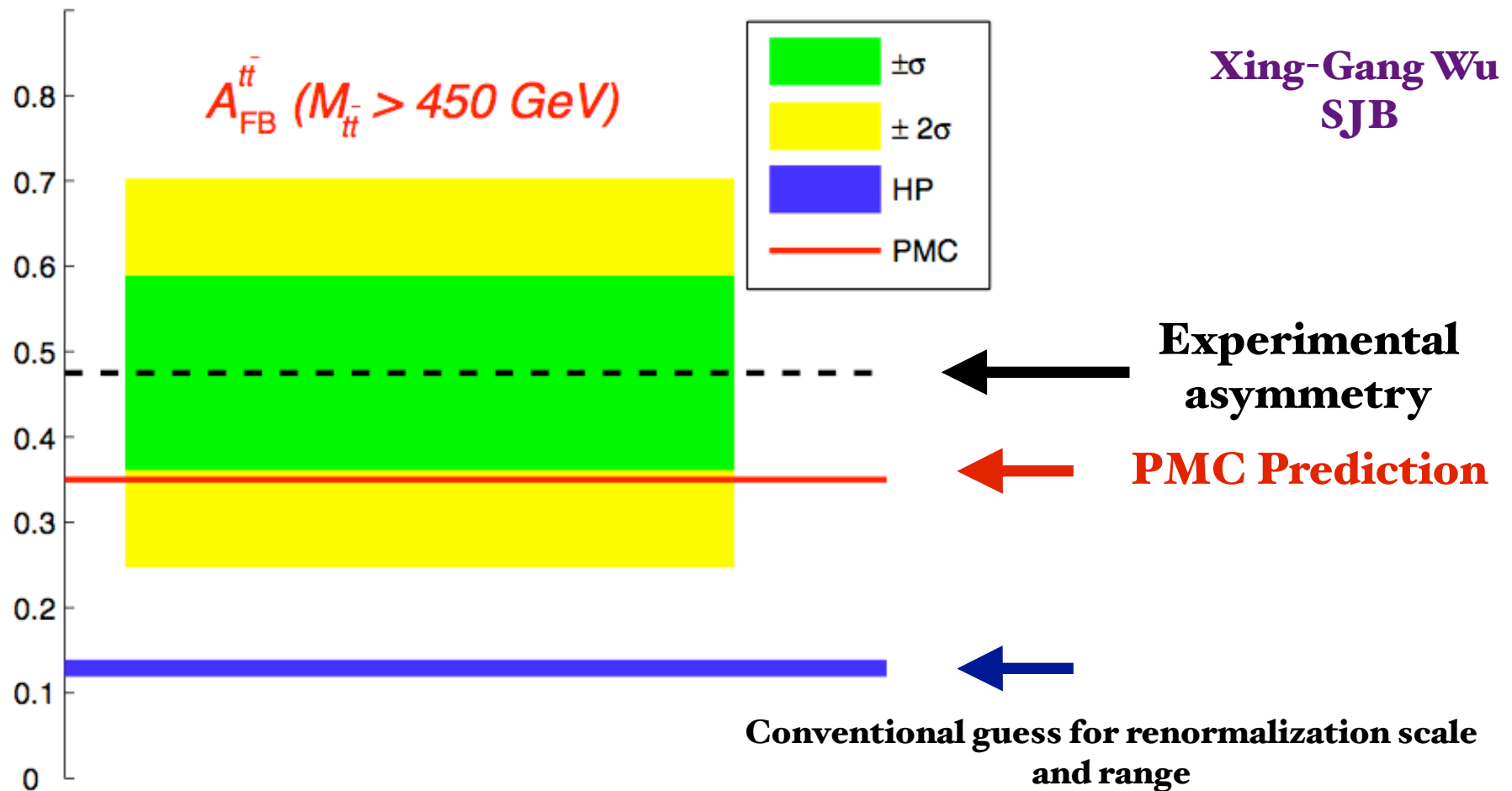
**Eliminates unnecessary
systematic uncertainty**

Scale fixed at each order

**δ -Scheme automatically
identifies β -terms!**

*Xing-Gang Wu, Martin Mojaza
Leonardo di Giustino, Sfb*

The Renormalization Scale Ambiguity for Top-Pair Production Eliminated Using the 'Principle of Maximum Conformality' (PMC)

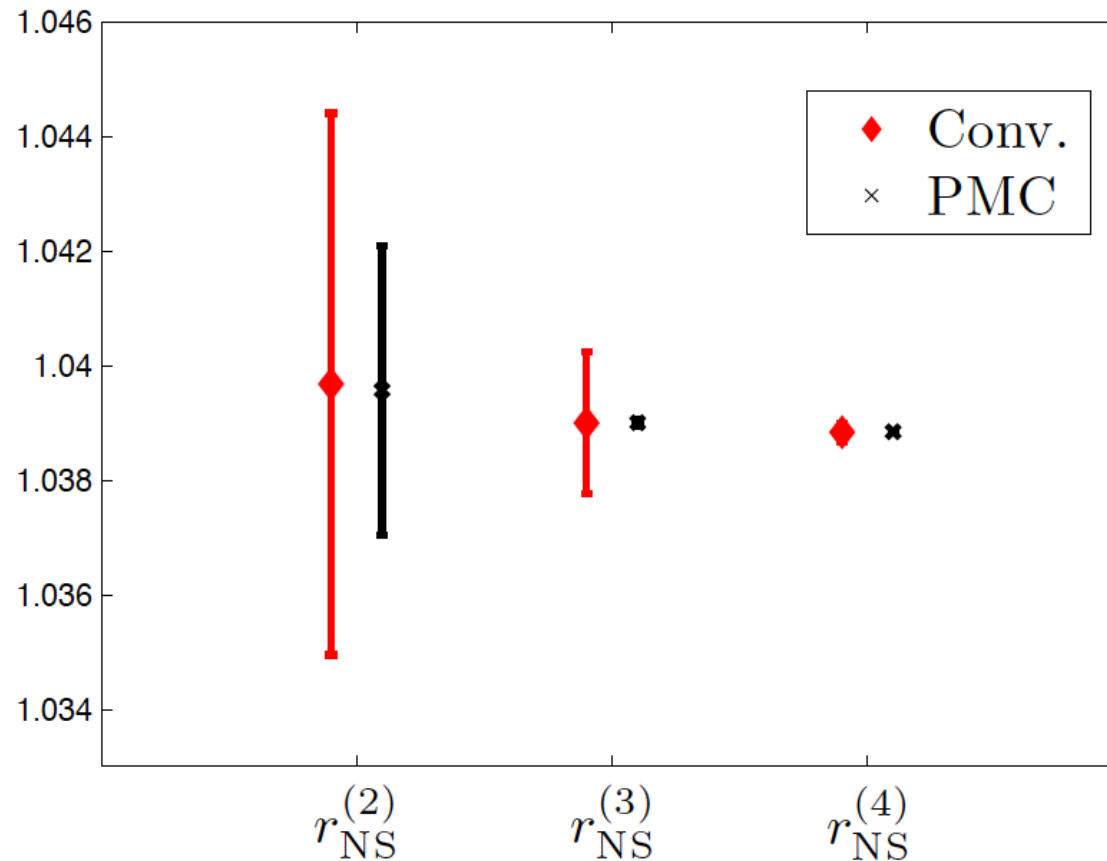


Top quark forward-backward asymmetry predicted by pQCD NNLO within 1σ of CDF/D0 measurements using PMC/BLM scale setting

Reanalysis of the Higher Order Perturbative QCD corrections to Hadronic Z Decays using the Principle of Maximum Conformality

S-Q Wang, X-G Wu, sjb

P.A. Baikov, K.G. Chetyrkin, J.H. Kuhn, and J. Ritinger,
Phys. Rev. Lett. 108, 222003 (2012).



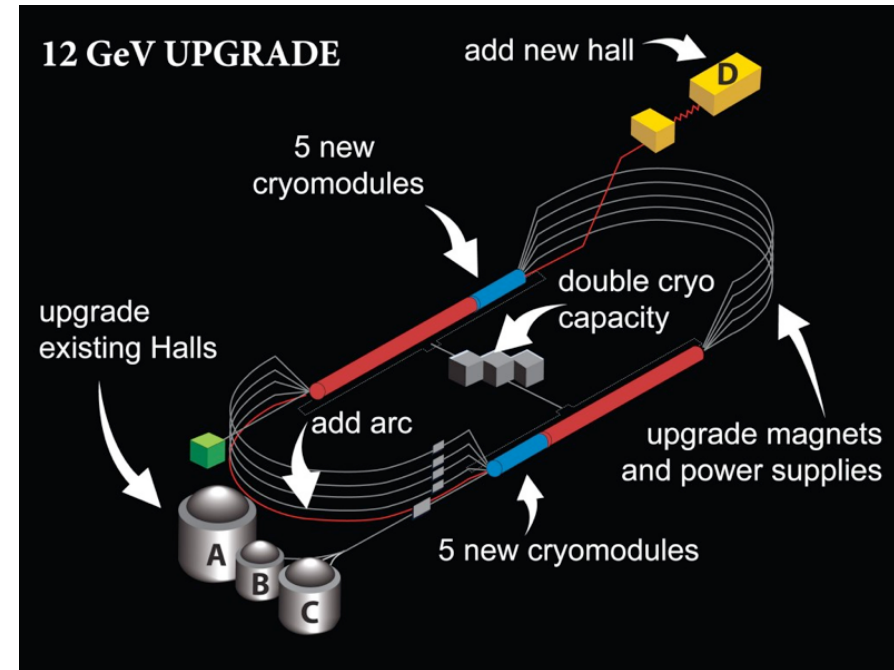
The values of $r_{NS}^{(n)} = 1 + \sum_{i=1}^n C_i^{NS} a_s^i$ and their errors $\pm |C_n^{NS} a_s^n|_{MAX}$. The diamonds and the crosses are for conventional (Conv.) and PMC scale settings, respectively. The central values assume the initial scale choice $\mu_r^{\text{init}} = M_Z$.

JLab 12 GeV: An Exotic Charm Factory!

- **Charm quarks at high x -- allows charm states to be produced with minimal energy**
- **Charm produced at low velocities in the target -- the target rapidity domain $x_F \sim -1$**
- **Charm at threshold -- maximal domain for producing exotic states containing charm quarks**
- **Attractive QCD Van der Waals interaction -- “nuclear-bound quarkonium”**
- **Dramatic Spin Correlations in the threshold Domain**
- **Strong SSS Threshold Enhancement**

Novel QCD Phenomena at JLab 12 GeV and the EIC

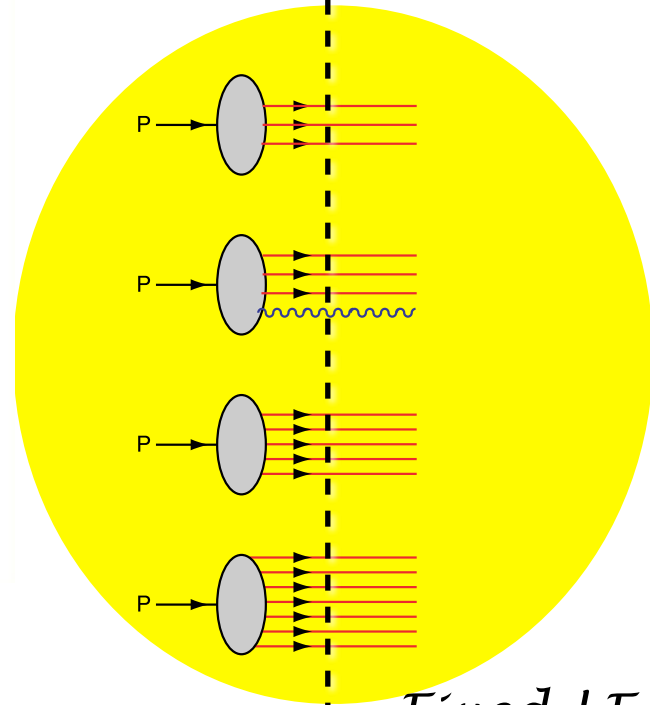
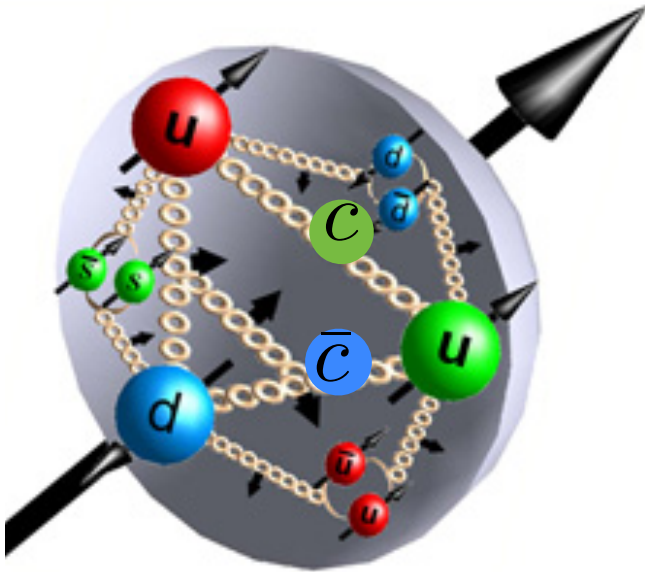
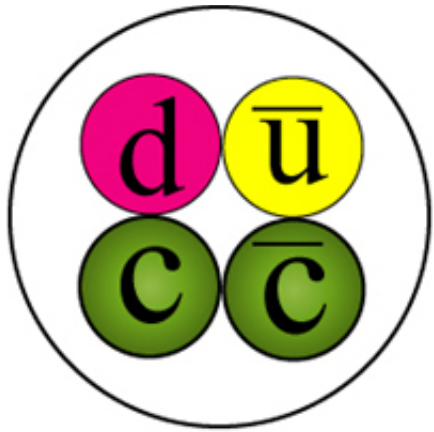
- Intrinsic Heavy Quarks
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- Hidden Color
- $J=0$ Fixed pole in DVCS



Illuminate New Hadronic Physics

Tests of Novel QCD Phenomena at JLab

Exotic Hadrons



Fixed LF time
 $\tau = t + z/c$

Stan Brodsky

SLAC
NATIONAL ACCELERATOR LABORATORY

Jefferson Lab

May 26, 2015

